

Hooke's Law:

$$F = -kx$$

SHM:

$$\begin{aligned}x(t) &= A \cos(\omega t) \\v(t) &= \frac{dx(t)}{dt} \\a(t) &= \frac{dv(t)}{dt} = \frac{d^2x(t)}{dt^2} \\T &= \frac{1}{f} = \frac{2\pi}{\omega} \\\omega &= \sqrt{\frac{k}{m}} = \sqrt{\frac{g}{l}} \\E &= \frac{1}{2}kA^2 = K + U = \frac{1}{2}mv^2 + \frac{1}{2}kx^2\end{aligned}$$

Damped Oscillation:

$$\begin{aligned}x(t) &= A \exp(-bt/2m) \cos(\omega t + \phi) \\\omega &= \sqrt{\frac{k}{m} - \left(\frac{b}{2m}\right)^2}\end{aligned}$$

Waves:

$$\begin{aligned}y(x, t) &= f(x \mp vt) = A \sin(kx \mp \omega t) \\k &= \frac{2\pi}{\lambda} \\\omega &= \frac{2\pi}{T} \\v &= \frac{\lambda}{T} \\v &= \sqrt{\frac{T}{\mu}} \\E &= \frac{1}{2}\mu\omega^2 A^2 \lambda \\P &= \frac{1}{2}\mu\omega^2 A^2 v\end{aligned}$$

Doppler Shift:

(source and observer moving towards each other)

$$f' = f \left(\frac{v + v_0}{v - v_s} \right)$$

Standing Waves:

$$y(x, t) = \left[2A \sin(kx) \right] \cos(\omega t)$$

Path/Phase difference:

$$\Delta r = \frac{\Delta \phi}{2\pi} \lambda$$

String/Open-End Pipe:

$$f_n = \frac{v}{\lambda_n} = n \frac{v}{2L} = n f_1 \quad n = 1, 2, \dots$$

Closed-End Pipe:

$$f_n = \frac{v}{\lambda_n} = (2n - 1) \frac{v}{4L} = n f_1 \quad n = 1, 2, \dots$$

Beats:

$$f_b = |f_1 - f_2|$$

Radiation Pressure :

$$\begin{aligned}P &= S/c && \text{(black body)} \\P &= 2S/c && \text{(Mirror)}\end{aligned}$$

Polarizers:

$$I = I_0 \cos^2 \theta$$

Geometric Optics:**Reflection**

$$\theta = \theta'$$

Refraction

$$\begin{aligned}\frac{\sin \theta_1}{\sin \theta_2} &= \frac{v_1}{v_2} \\ n &= \frac{c}{v} \\ n_1 \lambda_1 &= n_2 \lambda_2 \\ n_1 \sin \theta_1 &= n_2 \sin \theta_2\end{aligned}$$

Magnification

$$M = \frac{h'}{h} = -\frac{q}{p}$$

Mirror and lens equation

$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

Image formed by refraction

$$\begin{aligned}\frac{n_1}{p} + \frac{n_2}{q} &= \frac{n_2 - n_1}{R} \\ \frac{n_1}{p} &= -\frac{n_2}{q}\end{aligned}$$

Lenses

$$\frac{1}{f} = (n - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

Interference:

$$\begin{aligned}\frac{\delta}{\lambda} &= \frac{\phi}{2\pi} \\ \delta &= m\lambda \quad m = 0, 1, 2, \dots \quad \text{Constructive} \\ \delta &= \left(m + \frac{1}{2} \right) \lambda \quad m = 0, 1, 2, \dots \quad \text{Destructive}\end{aligned}$$

Double Slit Experiment

$$\begin{aligned}\delta &= d \sin \theta_{\text{bright}} = m\lambda \quad m = 0, 1, 2, \dots \\ \delta &= d \sin \theta_{\text{dark}} = \left(m + \frac{1}{2} \right) \lambda \quad m = 0, 1, 2, \dots \\ y_{\text{bright}} &= L \tan \theta_{\text{bright}}\end{aligned}$$

$$\begin{aligned}y_{\text{dark}} &= L \tan \theta_{\text{dark}} \\ I_{\text{max}} &= \cos^2 \left[\frac{\pi d \sin \theta}{\lambda} \right]\end{aligned}$$

Single Slit Diffraction

$$\sin \theta_{\text{dark}} = m \frac{\lambda}{a} \quad m = 0, 1, 2, \dots$$

Circular Aperture

$$\theta_{\text{min}} \approx 1.22 \frac{\lambda}{D}$$

Diffraction Grating

$$d \sin \theta_{\text{bright}} = m\lambda \quad m = 0, 1, 2, \dots$$

Quantum Physics:

Blackbody

$$\begin{aligned}P &= \sigma AT^4 \\ \lambda_{\text{max}} T &= 2.898 \times 10^{-3} m \cdot K\end{aligned}$$

Photoelectric Effect

$$\begin{aligned}E &= hf \\ K_{\text{max}} &= hf - \phi = e\Delta V_s \\ \lambda_c &= \frac{c}{f_c} = \frac{hc}{\phi}\end{aligned}$$

Compton Effect

$$\lambda' - \lambda_0 = \frac{h}{m_e c} (1 - \cos \theta)$$

de Broglie Wavelength

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

Uncertainty Principle

$$\Delta x \cdot \Delta p \geq \frac{\hbar}{2}$$

Atomic Physics:

Bohr's Atom

$$\begin{aligned}E_n &= -\frac{13.606\text{eV}}{n^2} \quad ; \quad n = 1, 2, 3, \dots \\r_n &= n^2 a_0 \quad \text{where} \quad a_0 = 0.0529\text{nm} \\|\mathbf{L}| &= \sqrt{l(l+1)}\hbar \quad ; \quad l = 1, 2, \dots, n-1 \\L_z &= m_l \hbar \quad ; \quad m_l = -l, (-l+1), \dots, l \\|\mathbf{S}| &= \sqrt{s(s+1)}\hbar \\S_z &= m_s \hbar = \pm \hbar/2\end{aligned}$$

Rydberg Equation

$$\frac{1}{\lambda} = R_H \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right) \quad ; \quad R_H = 1.097 \times 10^7 \text{m}^{-1}$$

Selection Rule:

$$\Delta l = \pm 1 \quad ; \quad \Delta m_l = 0, \pm 1$$

Multi-electron Atoms

$$E_n \approx -\frac{(13.606\text{eV})Z_{eff}^2}{n^2}$$

Nuclear Physics:

$$\begin{aligned}r &= r_0 A^{1/3} \quad ; \quad r_0 = 1.2 \times 10^{-15}\text{m} \\E_b(\text{MeV}) &= [ZM(H) + Nm_n - M({}_Z^AX)] \\&\times 931.494\text{MeV}/u\end{aligned}$$

Radioactivity

$$\begin{aligned}N(t) &= N_0 e^{-\lambda t} \\t_{1/2} &= \frac{\ln 2}{\lambda} = \frac{0.639}{\lambda} \\Q &= (M_X - M_Y - M_\alpha) \times 931.494\text{MeV}/u\end{aligned}$$

Derivatives:

$$\begin{aligned}\frac{d}{dx}(\sin ax) &= a \cos(ax) \\\frac{d}{dx}(\cos ax) &= -a \sin(ax)\end{aligned}$$

Trigonometry:

$$\theta \ll 1 \quad \text{rad.} \rightarrow \tan \theta \approx \sin \theta \approx \theta$$

Sine Values

$$\begin{aligned}\sin 5^\circ &= 0.087 \\\sin 10^\circ &= 0.174 \\\sin 15^\circ &= 0.259 \\\sin 20^\circ &= 0.342 \\\sin 25^\circ &= 0.423 \\\sin 30^\circ &= 0.500 \\\sin 35^\circ &= 0.574 \\\sin 40^\circ &= 0.643 \\\sin 45^\circ &= 0.707 \\\sin 50^\circ &= 0.766 \\\sin 55^\circ &= 0.819 \\\sin 60^\circ &= 0.866 \\\sin 65^\circ &= 0.906 \\\sin 70^\circ &= 0.940 \\\sin 75^\circ &= 0.966 \\\sin 80^\circ &= 0.984 \\\sin 85^\circ &= 0.996\end{aligned}$$

Cosine Values

$$\sin^2 \theta + \cos^2 \theta = 1$$

Units:

$$\begin{aligned}[^{\circ}\text{C}] &= [^{\circ}\text{K}] - 273.15 \\1 \text{ eV} &= 1.60217646 \times 10^{-19} \text{ J}\end{aligned}$$