

A photograph of a traditional wooden water wheel in a lush green forest. The wheel is made of dark wood and has several buckets attached to its rim. Water is flowing from a pipe at the top into the buckets. In the background, there is a log cabin with a thatched roof and a window with a white frame. The scene is surrounded by dense foliage and trees.

Physics 1A, Lecture 10: Work and Energy

Summer Session 1, 2011

The quiz will commence at 9:33 AM.

Key Questions: (Discuss with neighbors before quiz)

- 1) What is Hooke's Law?
- 2) What are the units of Kinetic and Potential energy?
- 3) How does Kinetic energy depend on velocity?
- 4) What is gravitational Potential Energy?
- 5) How can you calculate Work when Force depends on displacement?

Reading Quiz #8-1

Hooke's Law is a model for

- A. the force of gravity
- B. the force of friction
- C. the potential energy due to gravity
- D. the force of a spring
- E. the normal force

Reading Quiz #8-2

What are the units of Kinetic and Potential energy?

- A. The Joule, $J = \text{kg m/s}^2$
- B. The Joule, $J = \text{kg m}^2/\text{s}^2$
- C. The Newton, $N = \text{kg m/s}$
- D. The Newton, $N = \text{kg m/s}^2$
- E. The Watt, $W = \text{kg m}^2/\text{s}^3$

Reading Quiz #8-3

How does Kinetic energy depend on velocity?
Kinetic Energy is...

- A. independent of velocity.
- B. inversely proportional to velocity.
- C. directly proportional to velocity.
- D. inversely proportional to velocity squared.
- E. directly proportional to velocity squared.

Reading Quiz #8-4

What is gravitational Potential Energy?

A. Tells you how fast something is falling towards the earth

B. The energy an object has by being a certain vertical distance from a reference point.

C. It is always proportional to the Kinetic Energy

D. It can only be increased by falling.

E. A vector that points in the vertical direction.

Reading Quiz #8-5

How can you calculate Work when Force depends on displacement?

A. Take an integral of Work over displacement

$$\int W \cdot dx$$

B. Take a derivative of Work with respect to displacement

$$\frac{dW}{dx}$$

C. Take an integral of Force over displacement

$$\int F \cdot dx$$

D. Take a derivative of Force with respect to displacement

$$\frac{dF}{dx}$$

E. Don't even try, it can't be done.

Announcements

- HW #4 is posted, due this Wednesday
- Solutions to extra problems . . .
- Office hours today at noon (Mayer 5623)

Announcements

- Grades are posted for clickers and reading quizzes
 - I've already found several mistakes because I had to match up 3-digit codes with people by hand 😞
 - I will be re-uploading the grades next weekend.
 - These serial codes are not matched up with students:
- #01463B7C
- #058DC941
- #05F89F62
- #08DBF122
- #0E9D69FA
- #1AA4B00E
- #1C45DE87
- #1CC3EA35
- #1E6BDAAF
- #21AE46C9
- #2364BBFC
- #26B7CC5D

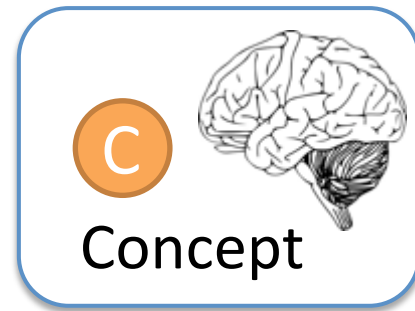
Grade adjustment

- First two quizzes will be adjusted with a horizontal shift to the right.
 - Quiz #1 (add 10%)
 - Quiz #2 (add 20%)

Anonymous Poll

- Did it help to work on problems with your neighbors in lecture last week?
 - A) Yes, otherwise the lecture would have gone too fast and I wouldn't get what you were talking about.
 - B) Yes, but I think it took up too much class time.
 - C) It didn't help or hurt, but I enjoyed the break.
 - D) No, the problems were either too easy or too hard to solve in the time that you gave us, and it took up too much class time.
 - E) No, my neighbors are clueless.

Energy / Money analogy



Types of Energy

- Kinetic Energy
- Potential Energy
 - Work

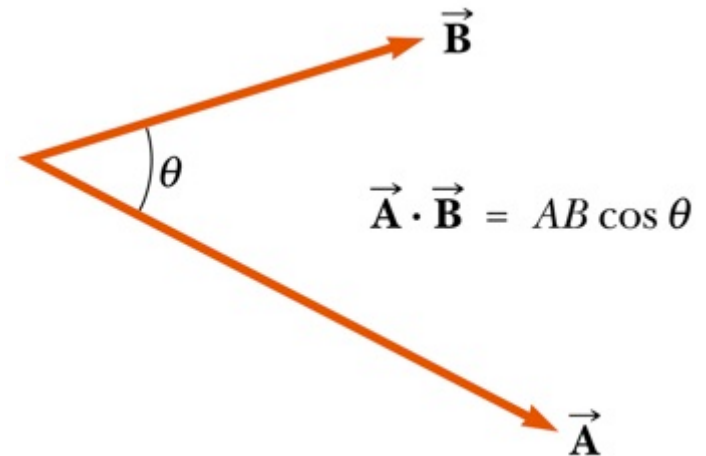
Types of Money

- Cash
- Money in bank account
 - A paycheck or bill

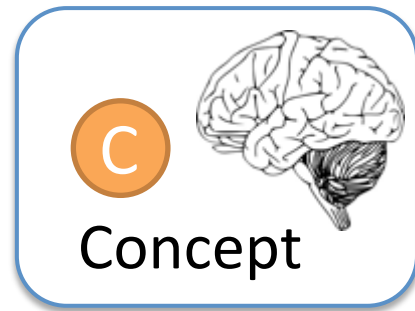
Math review:

Scalar product of two vectors

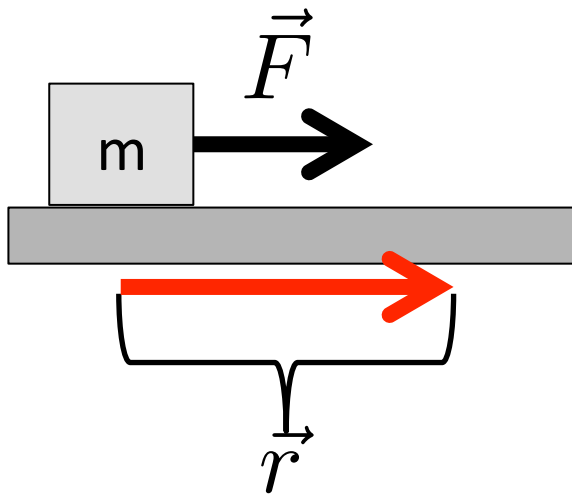
- Two vectors in any direction
- Find component of \vec{A} in the direction of \vec{B} and multiply by $|\vec{B}|$.
- Tells you a measure of how much two vectors lie along the same axis pointing in the same direction
- Input: Two vector
- Output: One scalar



Work by a constant force

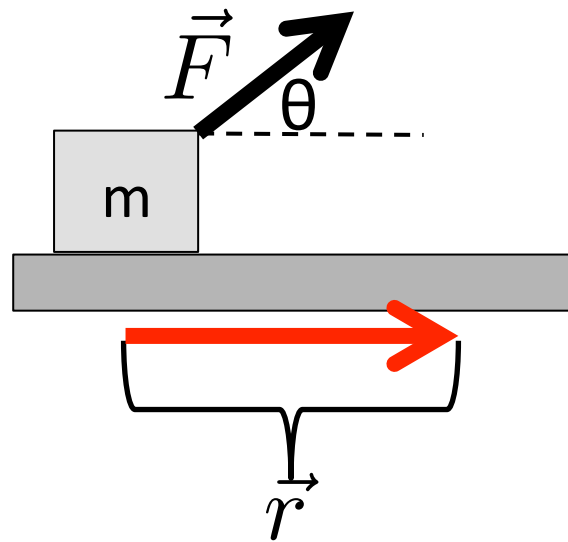


Force in direction of displacement:



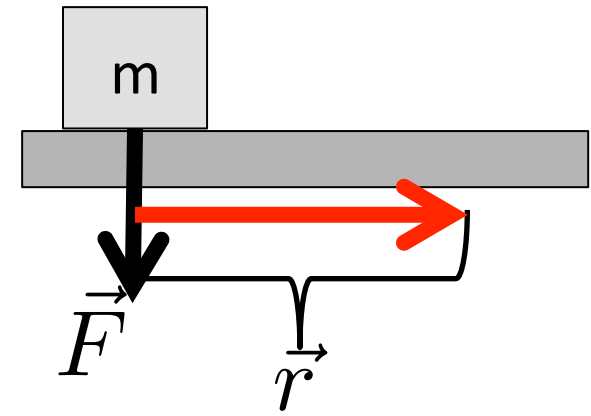
$$W = \vec{F} \cdot \vec{r}$$
$$W = |F| \cdot |r|$$

Force at an angle:



$$W = \vec{F} \cdot \vec{r}$$
$$W = |F| \cdot |r| \cos \theta$$

Force perpendicular to displacement:



$$W = \vec{F} \cdot \vec{r}$$
$$W = 0$$

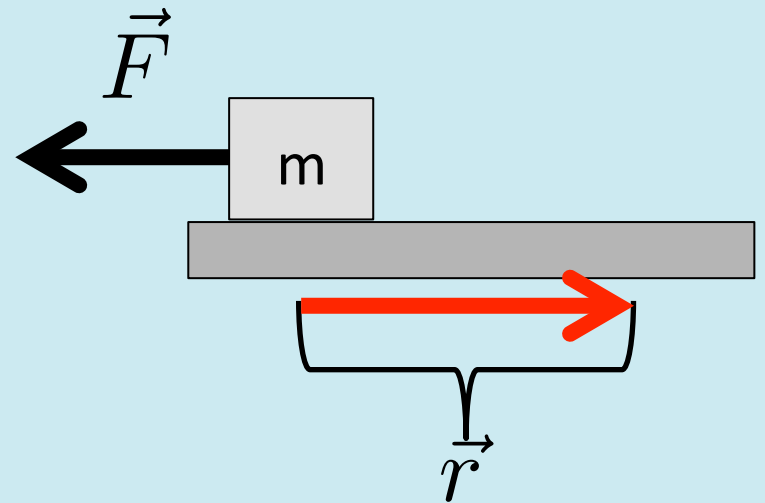
Clicker Question 8-1

- What is the work done by the force?

A) Zero

B) $W = |F| \cdot |r|$

C) $W = -|F| \cdot |r|$



Clicker Question 8-2

A box is being pushed horizontally by a force F and there is kinetic friction. What is the sign of the work done by the normal force on the box?

A) Zero

B) Positive

C) Negative

Clicker Question 8-3

A box is being pushed horizontally by a force F and there is kinetic friction. What is the sign of the work done by the friction force on the box?

A) Zero

B) Positive

C) Negative

Clicker Question 8-4

A box is being pushed by a force F which is not able to overcome the force of static friction. What is the sign of the work done by the force F on the box?

A) Zero

B) Positive

C) Negative

Types of energy

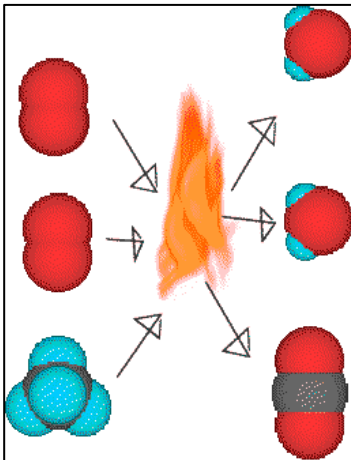
Heat



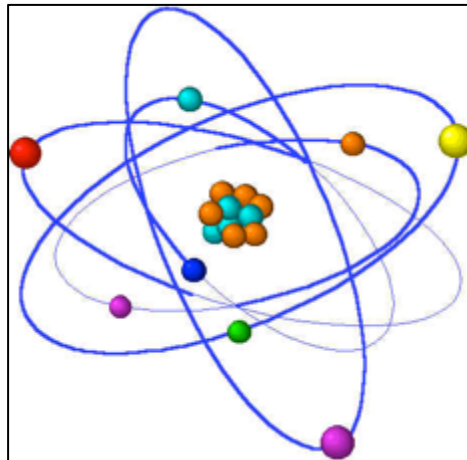
Mechanical



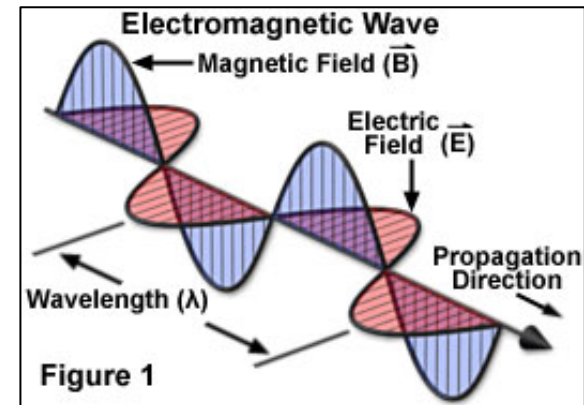
Chemical



Atomic or Nuclear



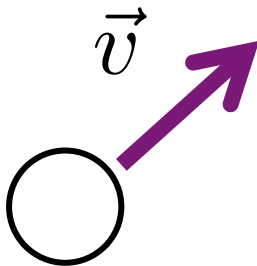
Electromagnetic



Kinetic and Potential Energy

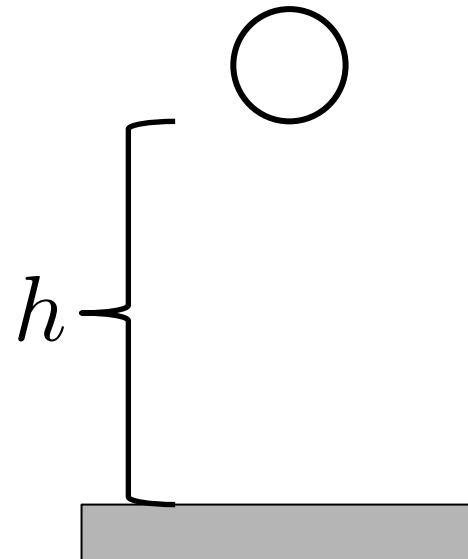
Translational
Kinetic Energy

$$KE = \frac{1}{2}mv^2$$



Gravitational
Potential Energy

$$PE_g = mgh$$



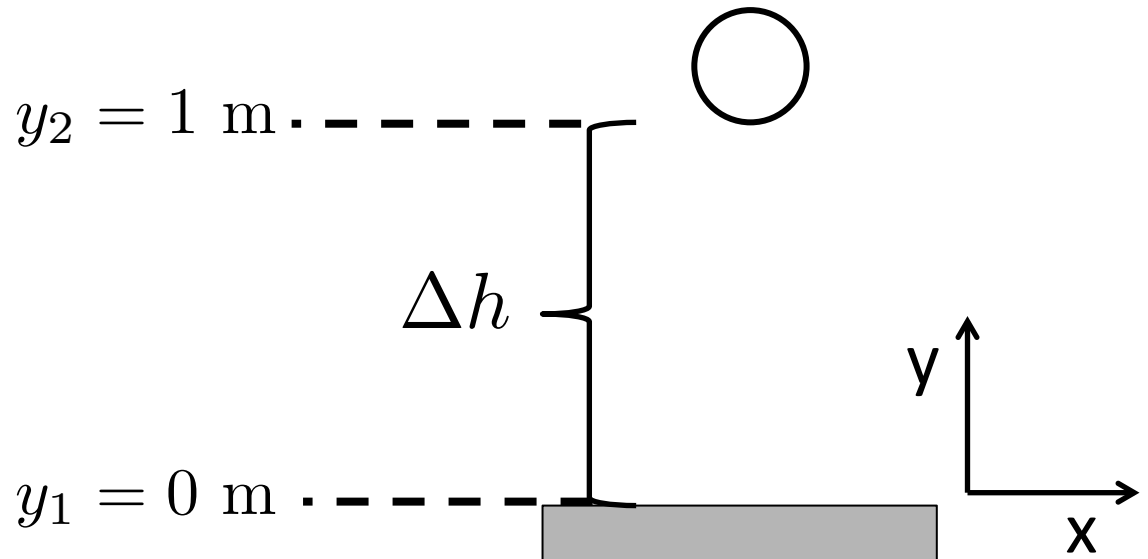
Kinetic and Potential Energy

(shouldn't depend on where you define the origin of your coordinate system)

Change in Gravitational Potential Energy

$$\Delta PE_g = mg\Delta h$$

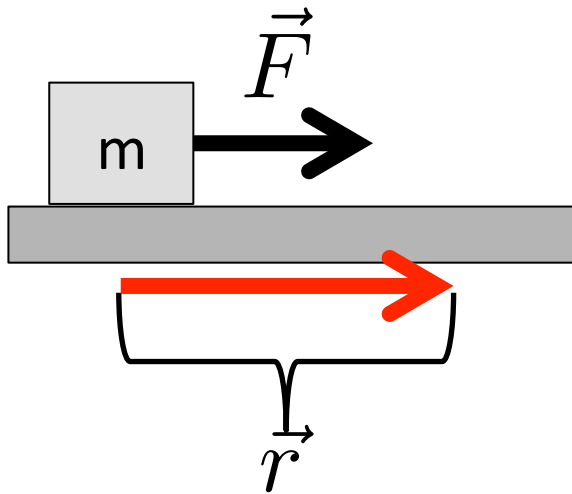
$$\begin{aligned}\Delta h &= y_2 - y_1 \\ &= 1 \text{ m}\end{aligned}$$



Kinetic Energy and Work

$$W = \Delta KE$$

- You push a box of mass m from rest a distance r across a frictionless floor with a constant force F . What is the final velocity of the box?



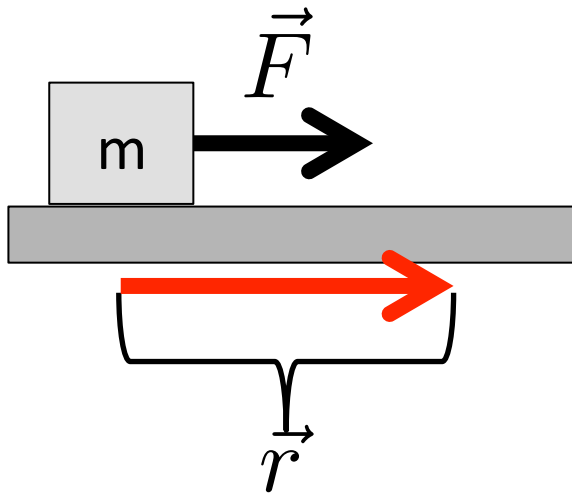
$$W = Fr$$

$$\Delta KE = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_0^2$$

$$\frac{1}{2}mv_f^2 = Fr \rightarrow v_f = \sqrt{\frac{2Fr}{m}}$$

Kinetic Energy and Work

- You push a box of mass m from rest a distance r across a frictionless floor with a constant force F . What is the final velocity of the box?

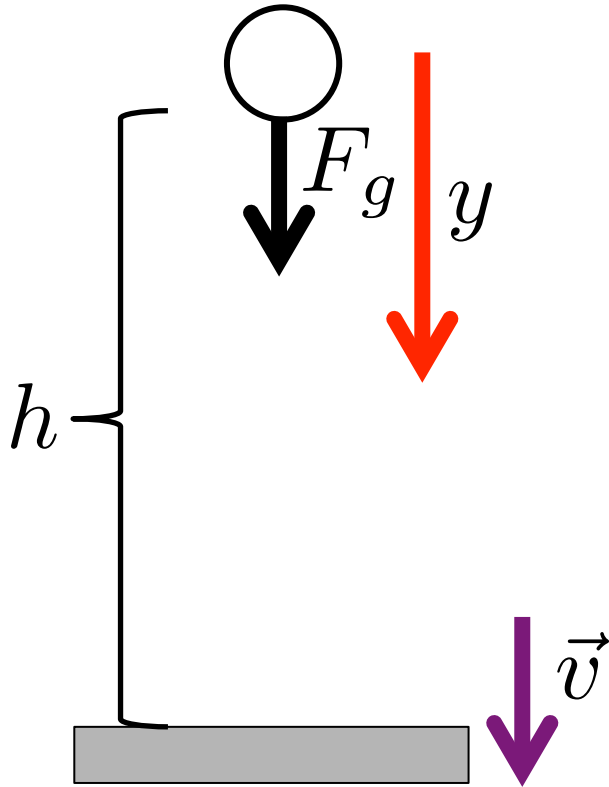


$$F = ma$$

$$v_f^2 = v_0^2 + 2ar$$

$$v_f^2 = \frac{2Fr}{m} \rightarrow v_f = \sqrt{\frac{2Fr}{m}}$$

Potential Energy and Work

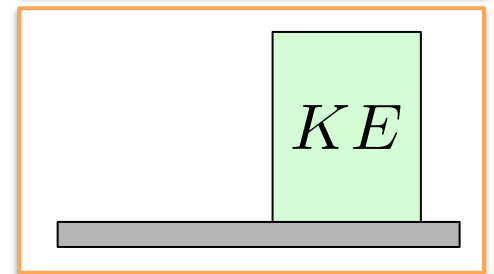
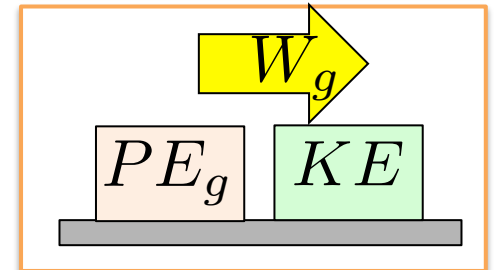
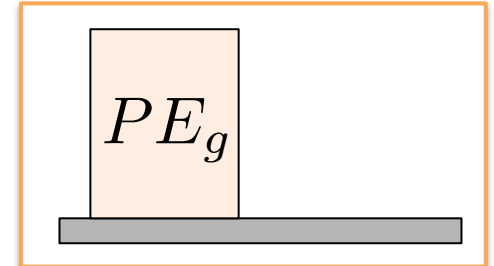


$$PE_g = mgh$$

$$W = -\Delta PE$$

$$W = \Delta KE$$

$$KE = \frac{1}{2}mv^2$$



Conservation of energy

$$E_{tot} = KE + PE$$

$$W = -\Delta PE$$

$$\Delta E_{tot} = \Delta KE + \Delta PE$$

$$W = \Delta KE$$

$$\Delta E_{tot} = W - W = 0$$

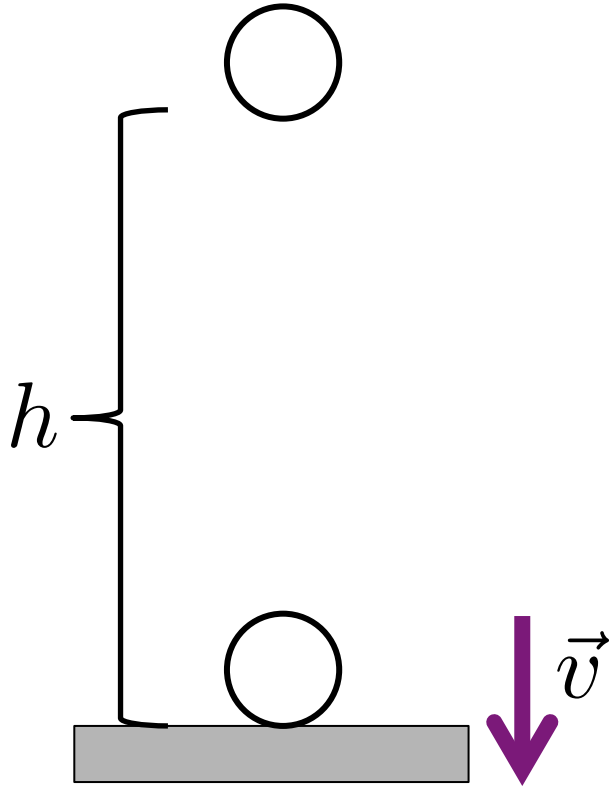
The total energy does not change over time

$$\Delta KE + \Delta PE = 0$$

Potential Energy and Work

$$\Delta KE + \Delta PE = 0$$

- You drop a ball of mass m from rest at a height of h . What is the velocity it has at the ground?



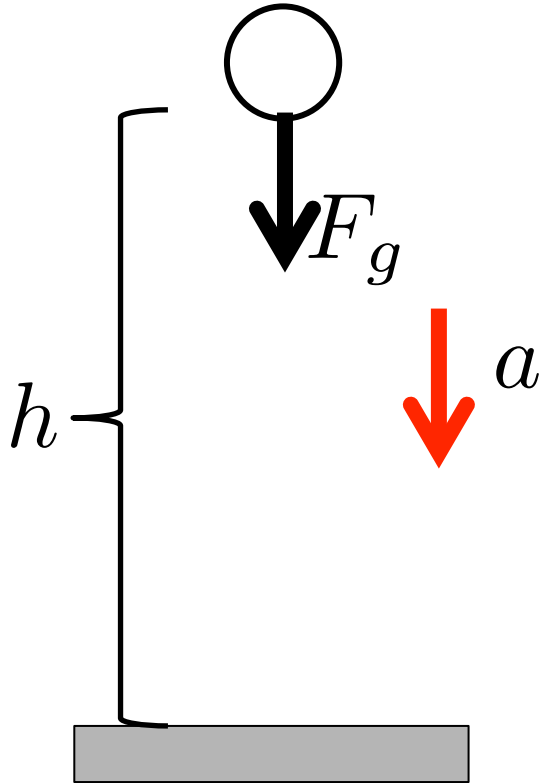
$$\begin{array}{l} \text{INITIAL} \\ PE_i = mgh \end{array}$$

$$KE_i = 0$$

$$\begin{array}{l} \text{FINAL} \\ PE_f = 0 \\ KE_f = \frac{1}{2}mv_f^2 \end{array}$$

$$\frac{1}{2}mv_f^2 = mgh \rightarrow \boxed{v_f = \sqrt{2gh}}$$

Potential Energy and Work



- You drop a ball of mass m from rest at a height of h . What is the velocity it has at the ground?

$$F_g = mg = ma$$

$$v_f^2 = \cancel{v_0^2} + 2ah$$

$$v_f^2 = 2gh \rightarrow \boxed{v_f = \sqrt{2gh}}$$

Clicker question 8-7

- Ball A and ball B have the same mass and are given the same initial velocity from the same height, but ball A is shot straight up in the air and ball B is shot horizontally. Which ball will have the larger final velocity when they land on the ground?

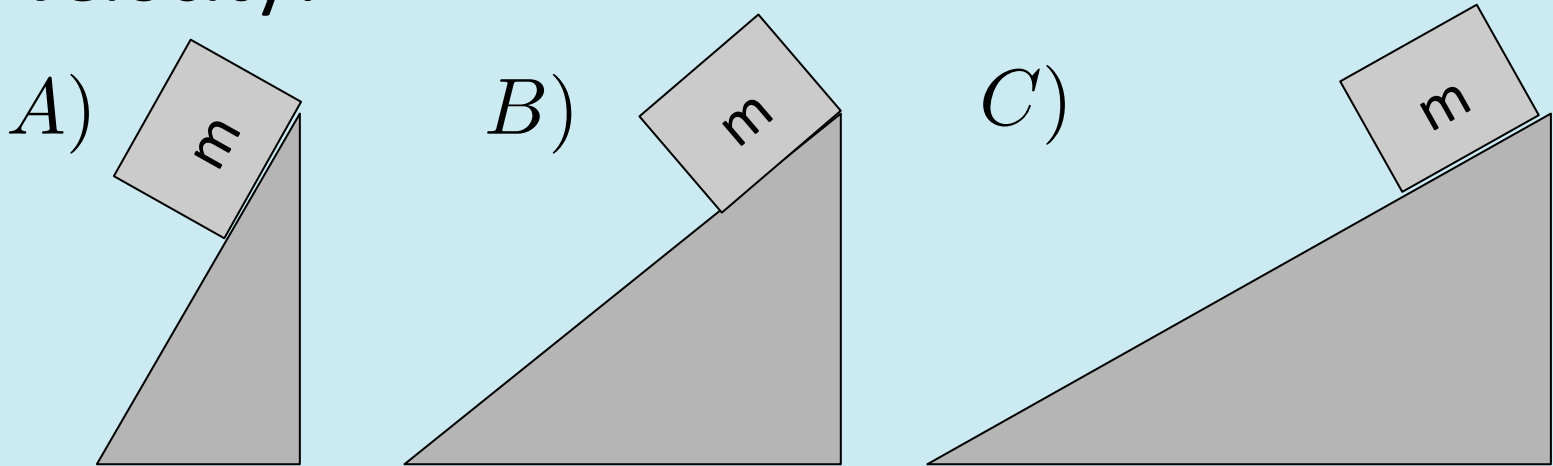
A) Ball A

B) Ball B

C) They will have the same final velocity

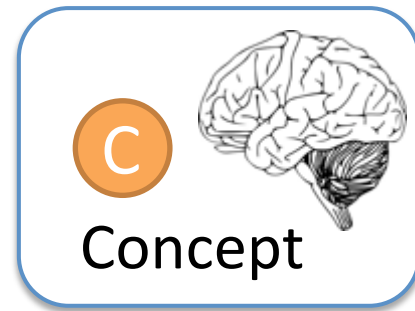
Clicker question 8-8

- All ramps are frictionless and have the same height. Which box will have the largest final velocity?



D) They will have the same final velocity

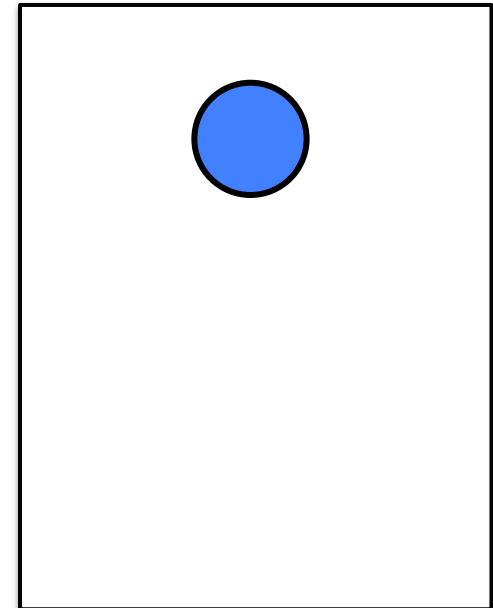
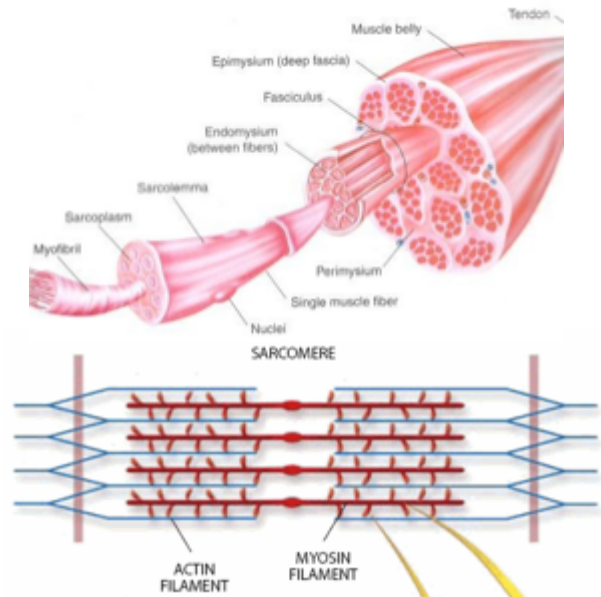
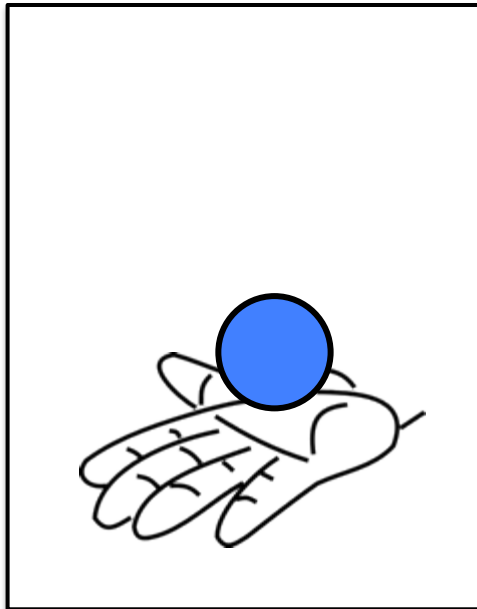
Isolated systems



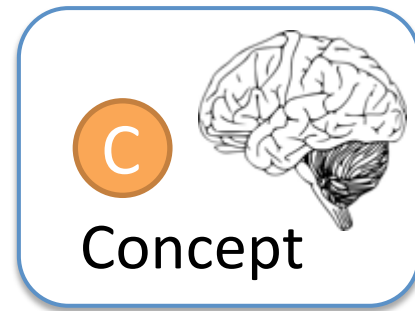
- System where total energy does not change over time (Energy is not added or dissipated away)
- Example:

Not an isolated system

An isolated system

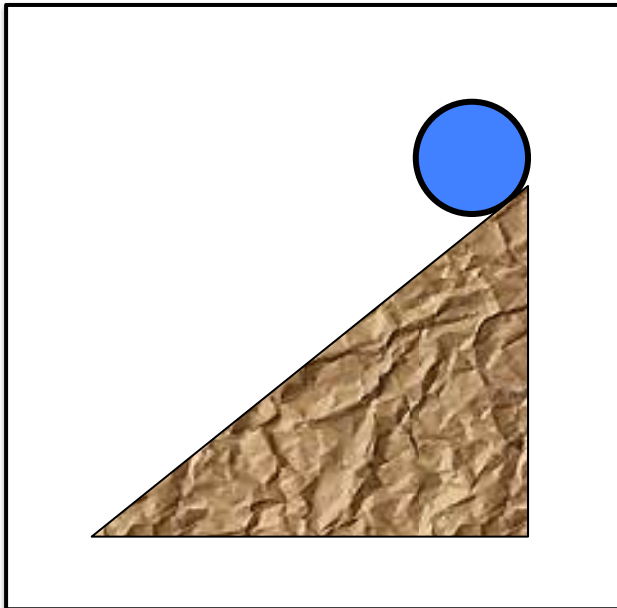


Isolated systems

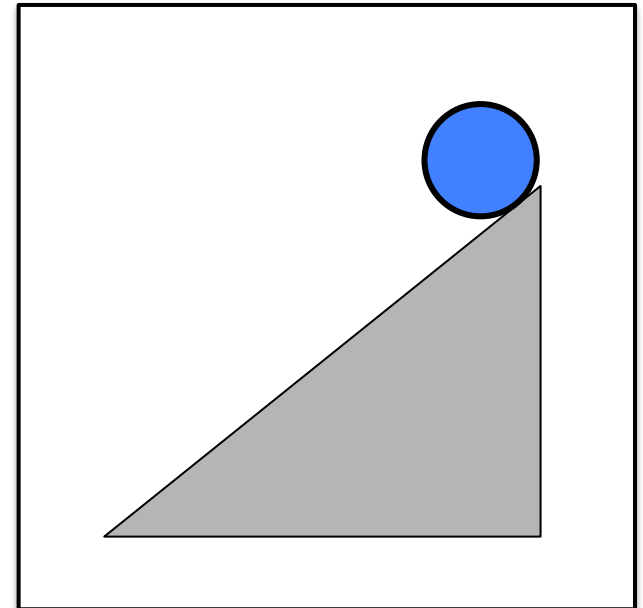


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Not an isolated system



An isolated system

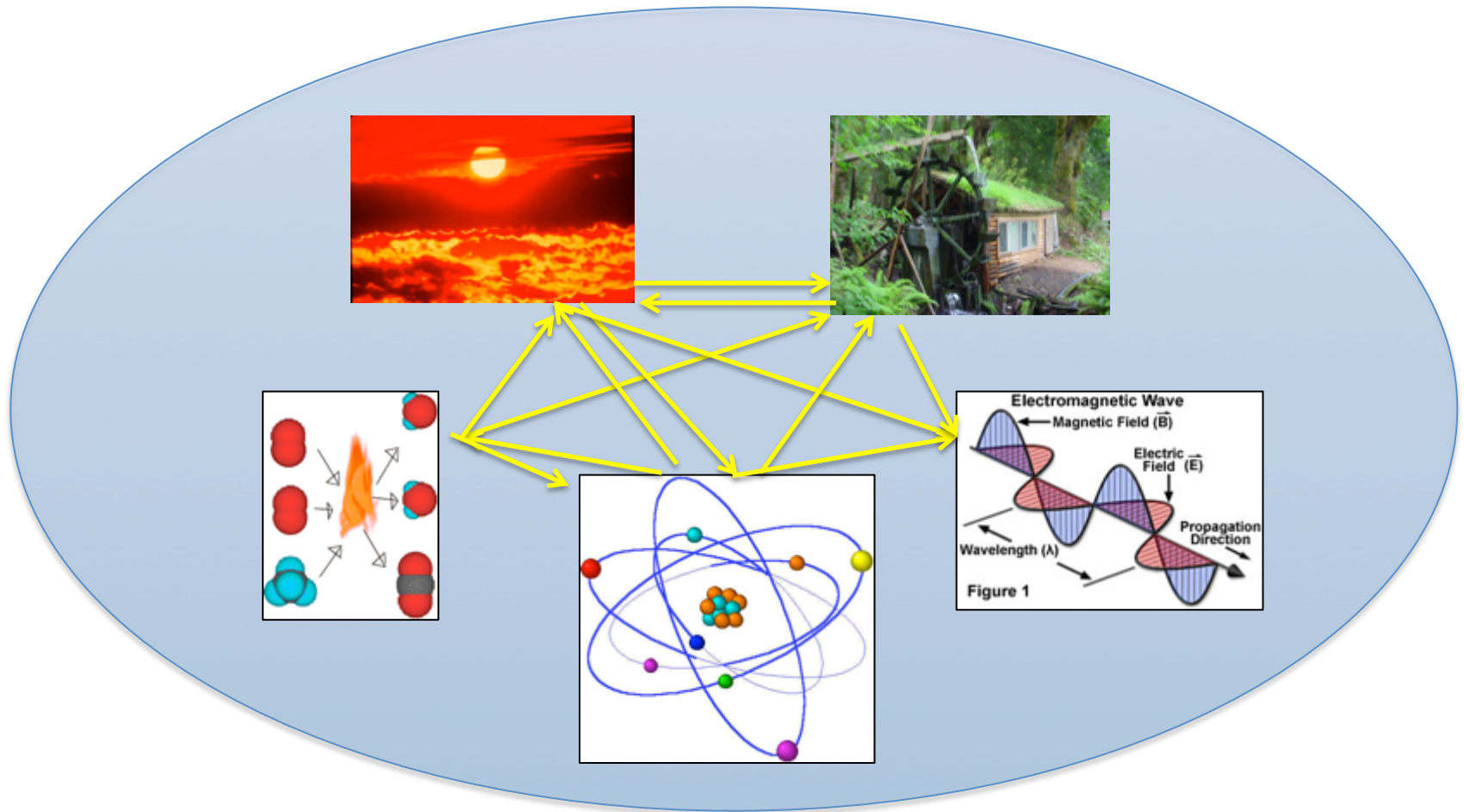


Isolated systems



Concept

- The universe is an isolated system:



Homework

- HW #4 is posted, due this Wednesday
- Reading quiz tomorrow
- Check if your grades are posted for clickers and reading quizzes