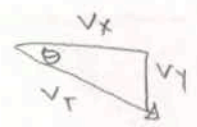


free to choose, but keep your positive and negative signs consistent!!!  
 here say going down is negative.



How long does it take to hit the ground? Interested in y motion and y velocity, not x.

$$v_{y0} = v_T \sin \theta$$

$$v_{y0} = 10 \frac{m}{s} \sin 30 = 5 \frac{m}{s} \rightarrow \text{but going down so } \underline{v_{y0} = -5 \frac{m}{s}}!$$

$$a = -9.8 \frac{m}{s^2}$$

$$y_f = -30 \text{ m}$$

$$y_0 = 0 \text{ m}$$

$$v_{y0} = -5 \frac{m}{s}$$

} see how they are all negative? what does that mean...?

$$y_f - y_0 = v_{y0} t + \frac{1}{2} a t^2$$

$$(-30 - 0) \text{ m} = -5 \frac{m}{s} \cdot t + \frac{1}{2} (-9.8 \frac{m}{s^2}) t^2$$

$$4.9 \frac{m}{s^2} t^2 + 5 \frac{m}{s} t - 30 \text{ m} = 0$$

(leave aside units for now, will get t in units of s)

$$4.9 t^2 + 5 t - 30 = 0$$

looks like

$$at^2 + bt + c = 0$$

which has 2 solutions  $\rightarrow t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

and  $\frac{-b + \sqrt{b^2 - 4ac}}{2a}$

negative time, don't count that

positive time makes sense, go with it.

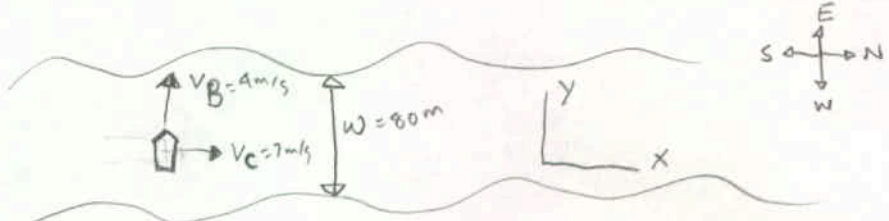
$$a = 4.9, \quad b = 5, \quad c = -30$$

$$t = \frac{-b + \sqrt{b^2 - 4ac}}{2a} \quad (\text{seconds})$$

$$t = \frac{-5 + \sqrt{25 + 4(4.9)(30)}}{2(4.9)} \text{ s} = \frac{-5 + \sqrt{613}}{9.8} \text{ s}$$

$$t = 2.0 \text{ s}$$

2.)



How far does the boat go downstream, ie - what is its total X displacement?

width of river =  $w$

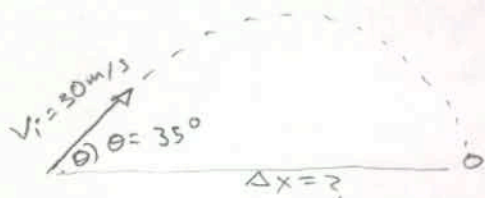
time it takes to cross river =  $t = \frac{w}{V_B}$

in time  $t$ , how far does the boat travel in the  $x$ -direction, aka downstream?

$$\Delta x = t \cdot V_C$$

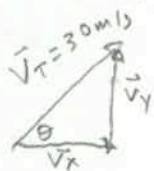
$$\Delta x = \frac{w \cdot V_C}{V_B} = 80 \cdot \frac{7}{4} \text{ m} = 140 \text{ m}$$

3.



How far does ball travel in X direction?

- ① • Split your velocity into x, y components.
- ② • Determine how long it is in the air (with  $V_y$ )
- ③ • Plug that time into your velocity, distance equation for  $\Delta x$



$$\textcircled{1} \quad \vec{V}_x = V_T \cos \theta = 30 \text{ m/s} \cos(35^\circ) = 24.6 \text{ m/s}$$

$$\vec{V}_y = V_T \sin \theta = 30 \text{ m/s} \sin(35^\circ) = 17.2 \text{ m/s}$$

- ② time to reach top of arc

$$\rightarrow t_1 \Rightarrow$$

$$v_{yf} = v_{y0} + a_y t$$

$$-v_{y0} = a_y t$$

$$t_1 = \frac{-v_{y0}}{a_y} = \frac{17.2 \text{ m/s}}{9.8 \text{ m/s}^2} = 1.76 \text{ s}$$

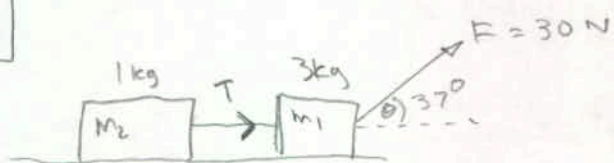
$t_2$  is time to fall down =  $t_1$

$$\text{total } t, \quad t = t_1 + t_2 = 2 \cdot 1.76 \text{ s} = 3.52 \text{ s in the air}$$

- ③  $\Delta x = v_x t$

$$\Delta x = 24.6 \frac{\text{m}}{\text{s}} \cdot 3.52 \text{ s} = 86 \text{ m}$$

4.



$$F = ma$$

$$F_x = m_T a_x$$

$$F_x = F \cos 37 = 23.96 \text{ N}$$

$$m_T = m_1 + m_2$$

$$a_x = \frac{F_x}{m_T} = \frac{23.96 \text{ N}}{1 \text{ kg} + 3 \text{ kg}} = 5.99 \text{ m/s}^2$$

the boxes are both accelerating at  $5.99 \text{ m/s}^2$  since the rope is taut.

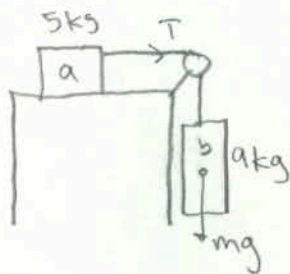
the only thing touching box of  $m_2$  is the rope, so it must be the force in the rope - the tension - that is pulling it.

$$F_a = m_2 a_2$$

$$T = m_2 a_2$$

$$T = 1 \text{ kg} \cdot 5.99 \text{ m/s}^2 = 5.99 \text{ N} \approx 6 \text{ N}$$

5.



$$F_y = m_b g$$

$$F_y = 9 \text{ kg} \times 9.8 \text{ m/s}^2$$

$$F_y = 88.2 \text{ N}$$

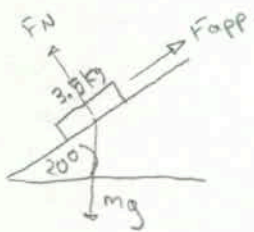
$$a = \frac{F}{m_T} = \frac{88.2 \text{ N}}{(5+9) \text{ kg}} = 6.3 \text{ m/s}^2$$

(both blocks accelerate at the same rate.)

$$T = m_a a$$

$$T = 5 \text{ kg} (6.3 \text{ m/s}^2) \approx 32 \text{ N}$$

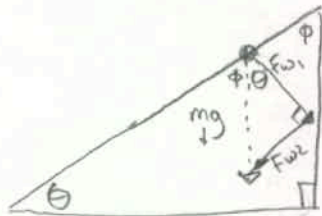
6.

Forces acting on box  $\rightarrow$ 

$$w = mg$$

 $F_{app}$   
 $F_{normal} \sim$  (not important)

velocity along the ramp is constant.

Therefore there is no acceleration along the ramp and the net force  $= 0$ Break gravitational force  $= mg$  into component vectors, one acting parallel to  $F_{app}$ 

$$F_{w1} = mg \cos \theta \quad (= \text{normal force, not important here since there is no friction})$$

$$F_{w2} = mg \sin \theta$$

On the surface of the ramp

$$\Sigma F = F_{app} + F_{w2}$$

$$\Sigma F = F_{app} - F_{w2} = 0$$

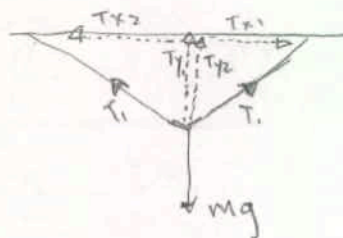
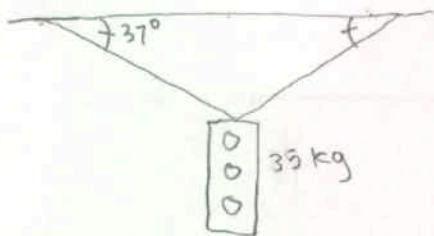
(acts in opposite direction)

$$F_{app} = F_{w2}$$

$$F_{app} = mg \sin \theta = 3.5 \text{ kg} \cdot 9.8 \frac{\text{m}}{\text{s}^2} \cdot \sin(20^\circ)$$

$$F_{app} = 11.7 \text{ N}$$

7.



Each Tension can be split into 2 components  $T_x$  and  $T_y$ . The  $T_x$ s cancel each other out since they point in opposite directions and have equal magnitude, (same magnitude because same angle.) The  $T_y$ s add up since they act in the same direction.

$$\text{Therefore, } \sum F_y = 2T_y - mg$$

where  $g = +9.8 \text{ m/s}^2$  (the magnitude of gravitational acceleration,) and the minus sign indicates it acts oppositely to  $T_y$ .

But since nothing is moving

$$\sum F_y = 0 = 2T_y - mg$$

$$2T_y = mg$$

$$T_y = \frac{mg}{2}$$

use trig

$$\sin \theta = \frac{T_y}{T}$$

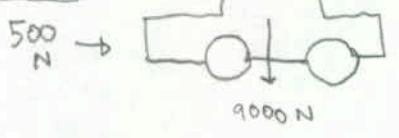
$$T = \frac{T_y}{\sin \theta}$$

$$T = \frac{mg}{2 \sin \theta} = \frac{(35 \text{ kg})(9.8 \text{ m/s}^2)}{2 \sin(37)}$$

$$T = 285 \text{ N}$$



8.



9000 N automobile.

N means force. In this case it is weight.

$$W = mg$$

$$9000 \text{ N} = m(9.8 \text{ m/s}^2)$$

$$m = 918 \text{ kg}$$

$$F_x = 500 \text{ N}$$

$$F_x = ma_x$$

$$918 \text{ kg} a_x = 500 \text{ N}$$

$$a_x = \frac{500 \text{ N}}{918 \text{ kg}} = .54 \text{ m/s}^2$$