

Physics 218c

Lecture ~~48~~ 49

- { Phenomenology &
Basic Physics of
ITG/ n_i Modes

→ Some Phenomenology:

- drift waves understood since
60's, 70's

c.f. Sagdeev et al., Kadomtsev, et al.
Rosenbluth et al.

- to mid 70's:

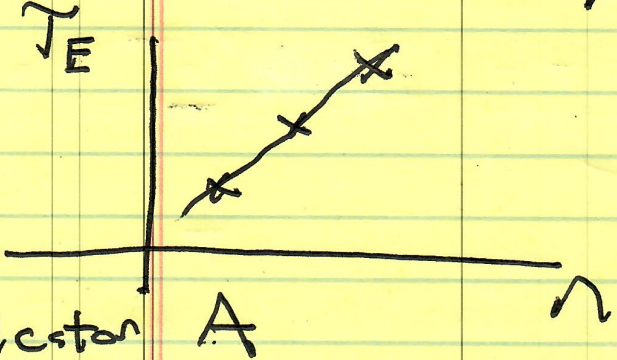
→ "real men do MHD" →
microturbulence not important
topic. ~ regarded as

- Mid-late 70's:

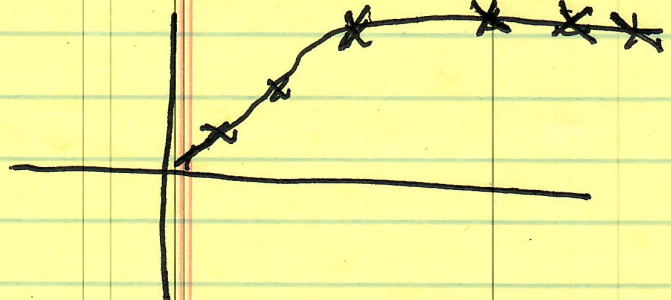
- No-Alcator + OH saturation → direct
- scattering experiments → measured turbulence in tokamaks

Ideas for LOC
 \sim STEM, CTEM
 $\sim (V_{acc}/R) C/\omega_{pe}^2$

Alcator scaling //



→ Favorable
 but then:



(see John Rice, et al recent NF)

What's happening?

$\sim v_{ei} n (T_e - T_i)$

⇒ collisions
 coupling to [ions]

→ and then

Multiple confinement regimes
 challenged simplistic views

LOC-SOC ⇒ Ohmic entrance
 rotation reversals.

$n \sim I_p$
 both tokamaks RFD

(LOC)

$T_e \sim n$

later:

$T_e \sim n a^3 \rightarrow n R^2 a$

→ explain?

SOC

Favorable
 Linear scaling
 ends

Linear Ohmic
 confinement

→ Saturated

Ohmic confinement.

Linear
 Ohmic
 Confinement

NEO

but then: Alcator-C Pellet Injection
Yuse (1984)

- ~~recall~~ recall: - edge fuelling

- density patch

$$\frac{d\langle n \rangle}{dt} = -D \cdot \nabla^2 + S_n^{edge}$$

Physics
of
 $v \ll c$?

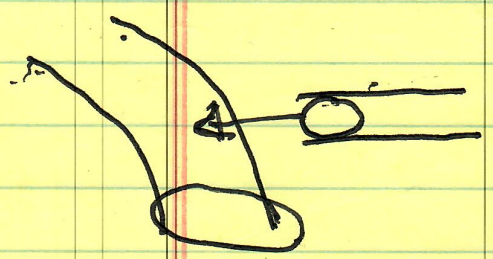
$$\nabla^2 = -D \nabla^2 + v \nabla$$

$v \ll c$

- ⇒ - difficulty in fuelling
- flat-ish n (also n -limit)

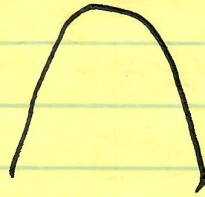
Fuelling remains major issue for ITER

⇒ peak n via pellet ?



Surprise?

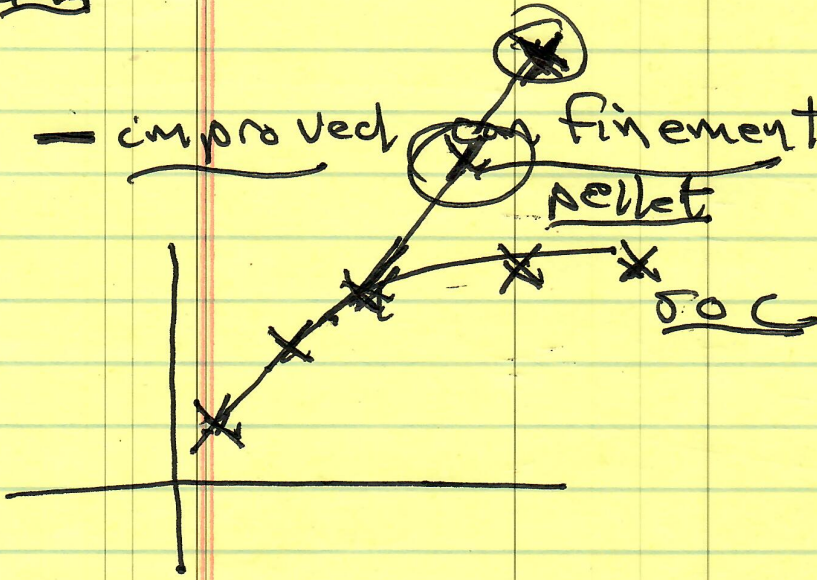
- peaked η



and

- improved confinement of energy pellet

(as "ITB")



n_B : Electron
 \rightarrow HPP $\sim 1/n$
 in post pellet

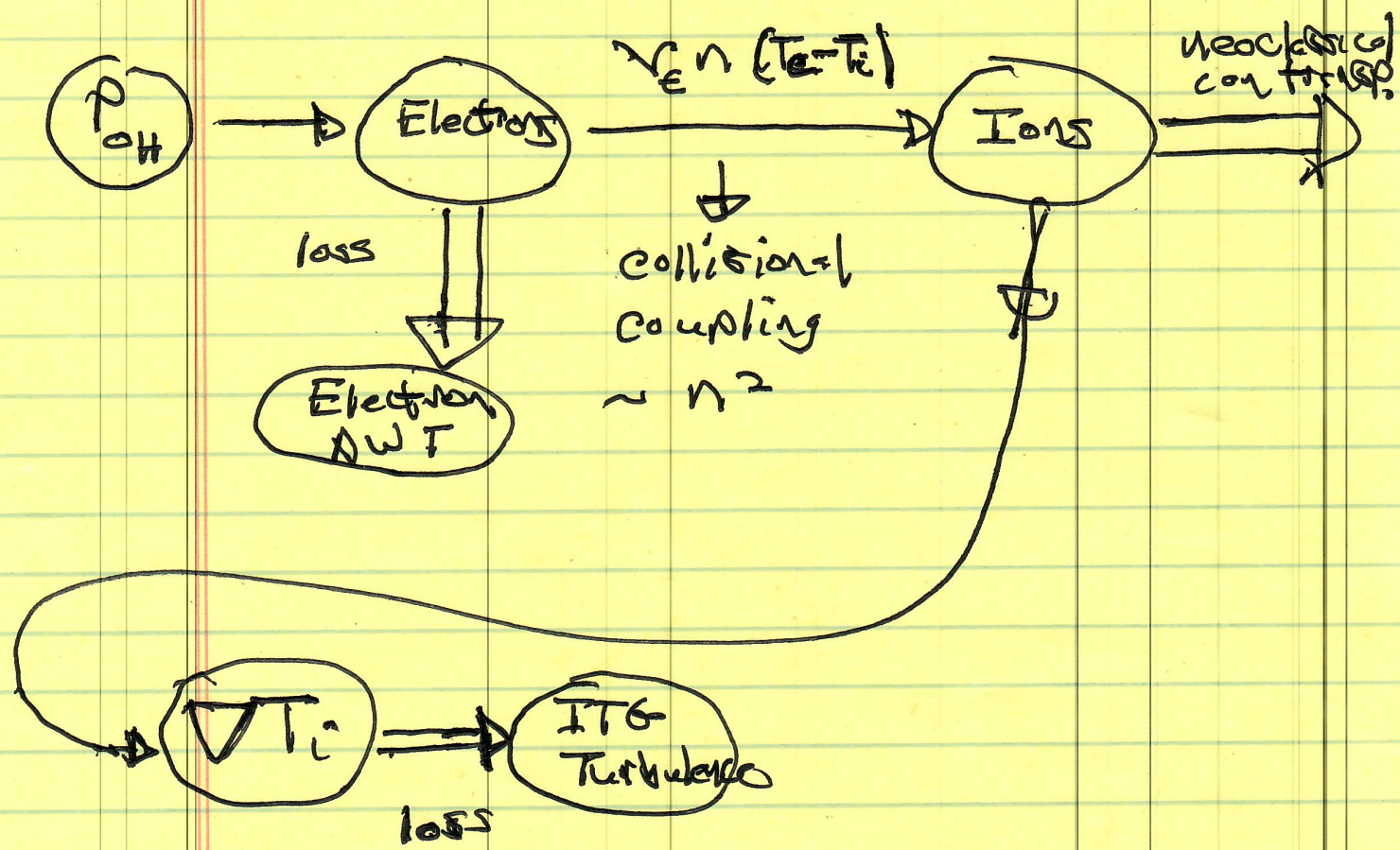
de pellet + peaked $\eta \Rightarrow$

restored LOC trend.

see also: IOC (Saturated \rightarrow Improved Ohmic Confinement)

\Rightarrow Confinement experiments indicated that peaked profiles are good \rightarrow Can improve confinement.

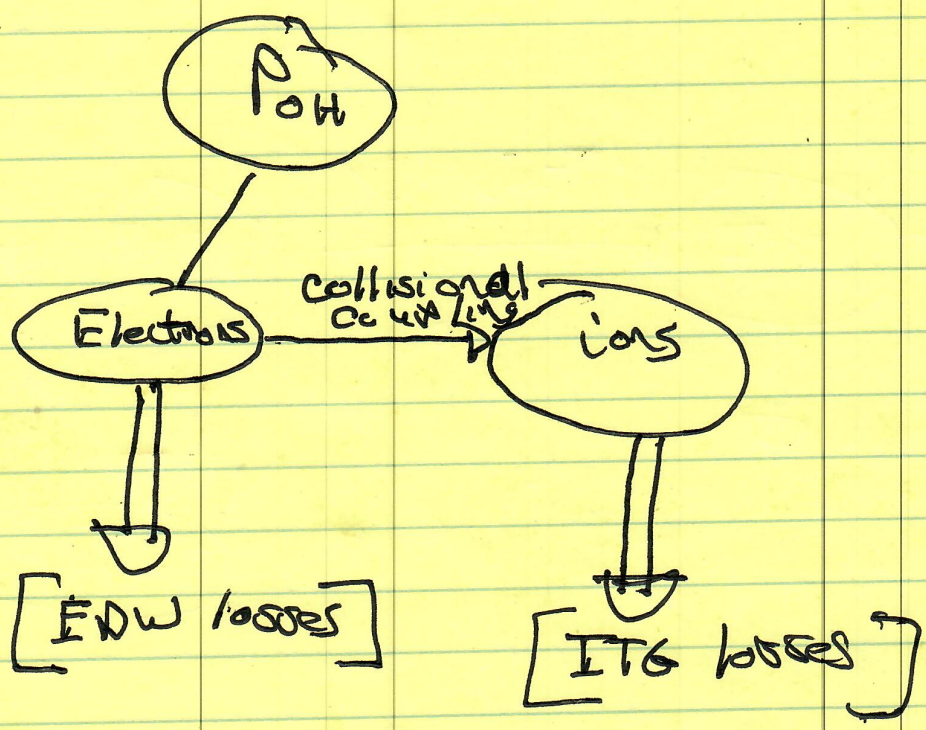
Note energetics :



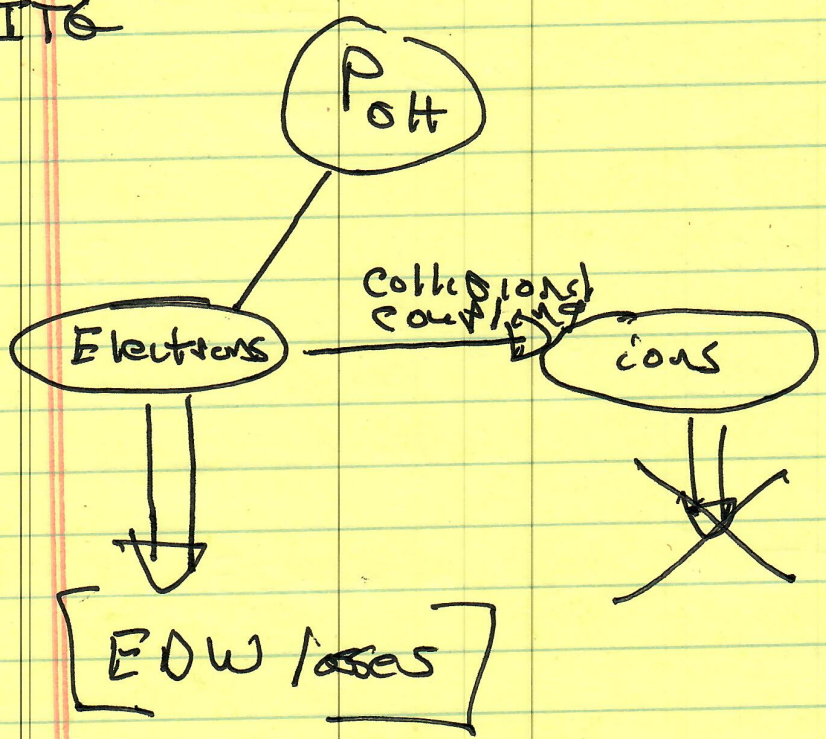
Note: Collisional coupling converts electron heating to ion ΔT_i . Free energy, and can trigger ITG loss channel.

i.e. ECH + high $n \Rightarrow$ ITG.

Now



with peaked n -profile \rightarrow eliminate ITG



c.f. $\nu_{HPP} \sim 1/n$ in peaked density profiles

→ In the meantime:

Previous:
Q-mechanics

- Mozzucatto

- Surko & Slusher

Scattering
experiments

- microturbulence happens!

- $\langle \tilde{n}^2 \rangle_{k, \omega}$

- $\omega \sim \omega_{pe}$

- $\Delta \omega_{pe} \sim \omega_{pe}$, fixed $k \Rightarrow$ strong turbulence

- crudely consistent with drift waves

⇒ drift waves not a phantom of theorists' collective imagination.

but ⇒ connection to confinement not made.

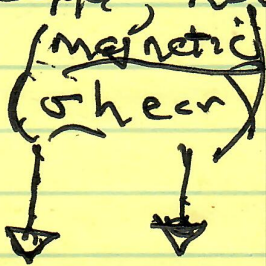
→ While all this going on

Since '60's :

→ Ion drift waves / n_i / ITS studied

- Sagdeev, Rudakov early '60s

- Coppi, Rosenbluth, Sagdeev, Trieste '67



but, since T3:

"Party Line" { C C C P and P P P L } ⇒

→ electrons anomalous

$\chi_e \gg \chi_{neoclassical}$

→ Ions neoclassical (collisional)

→ Theory of ITG was ignored until:

→ Alcator-C Pellet Injection

→ DN steepening lowers M_i

→ T_E improved

and

→ Good T_i measurements via

Charge Exchange Recombination Spectroscopy (ancestors of BES)

CHRS → Fench; Goldston (PPPL)

CHS → Groebner; Burrell (GA)

NTI → NTI-D

⇒ good T_i measurements

⇒ Transport analysis ⇒ X_i anomalies (especially NBI)

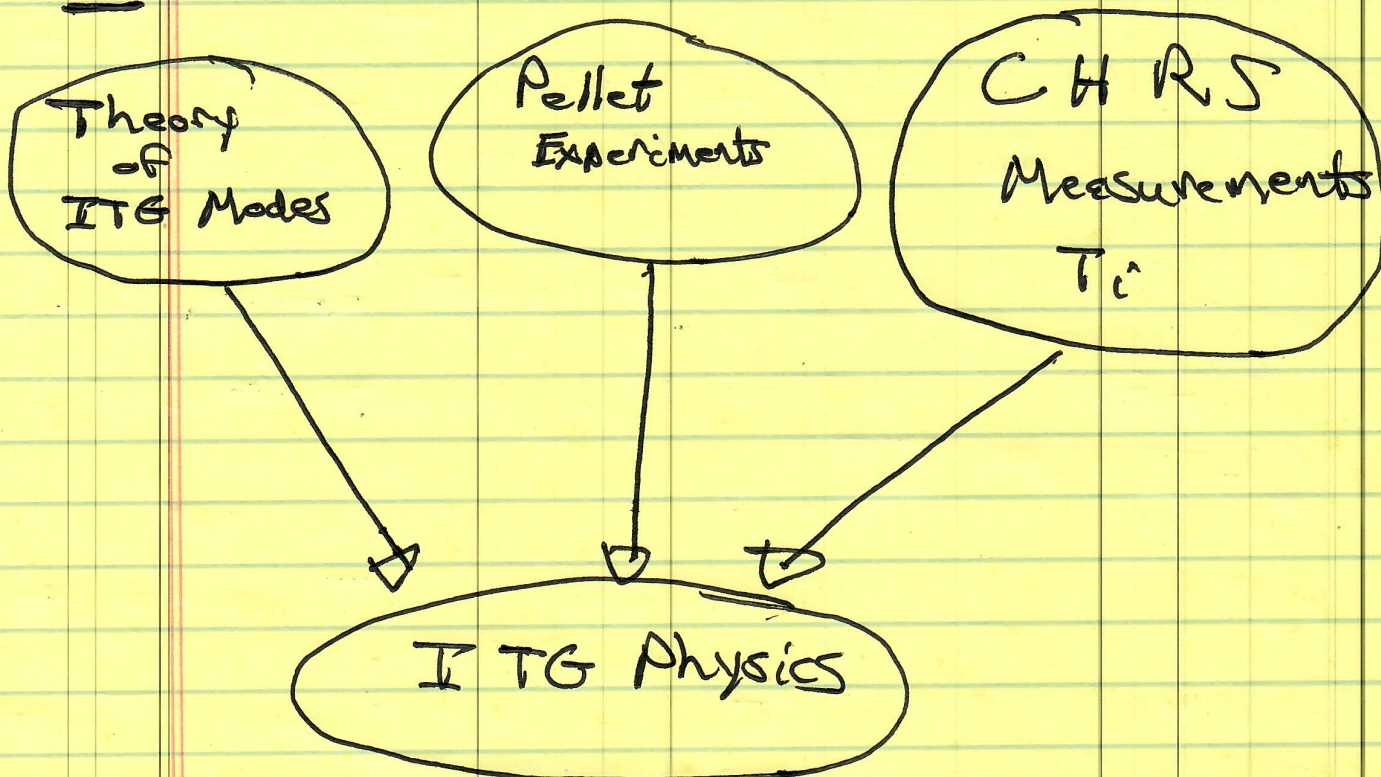
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⇒ Theorists vindicated
and

ITG taken seriously

⇒ ITG Physics!

N.B.



→ Fluid Theory / ITG / " " " " Slab sound waves

have What is simplest theory?
of ITG? $\underline{\nabla} \cdot \underline{v} = \underline{\nabla} \cdot \underline{v}_\perp$

$$\frac{\partial n}{\partial t} + \underline{v}_\perp \cdot \underline{\nabla} n + n \underline{\nabla} \cdot \underline{v} = 0 + \underline{\nabla}_\parallel v_\parallel$$

→ continuity

[Gale's standard H-M derivation]

$$m_i n \left(\frac{\partial v_\parallel}{\partial t} + \underline{v}_\perp \cdot \underline{\nabla} v_\parallel \right) = -\underline{\nabla}_\parallel \tilde{P}_i - n_i e |\underline{\nabla}_\parallel \tilde{\phi}|$$

acoustic scattering
ion pressure
electron pressure

→ parallel flow

$$\frac{\partial T_i}{\partial t} + \underline{v}_\perp \cdot \underline{\nabla} T_i = -\tilde{v}_\parallel E_\parallel \frac{\partial T_i}{\partial r} = \frac{2}{3} T_i \frac{\underline{\nabla}_\parallel \tilde{v}_\parallel}{\tilde{v}_\parallel}$$

temperature mixing
free energy source
compression factor

→ temperature Eqn.

free energy source.

→ compression factor
(Eqn. of state)

$$\frac{N_{\text{ow}}}{n_0} \approx \frac{|\underline{\nabla}_\parallel \tilde{\phi}|}{T_e}$$

→ Boltzmann electrons

non-dissipative

Non-dissipative character of ITG is fundamental

they $\tilde{V} \cdot \nabla_{\perp} = \langle U_E \rangle \frac{\partial}{\partial y} + \underbrace{\tilde{U}_E \cdot \nabla_{\perp}}_{E \times B \text{ NL.}}$

\downarrow shear
 (zonal flow)
 \downarrow driven by Reynolds stresses

$\tilde{V} \cdot \nabla \tilde{N} \Rightarrow 0$

Ignoring shear flow here: (Linear Eqn.)

$$\partial_t \frac{\tilde{\rho}}{\bar{\rho}} + \tilde{V}_E \cdot \nabla n \frac{n_0}{n_0} + \nabla_{\perp} \cdot \tilde{V} \rho + \underbrace{\nabla_{\parallel} \tilde{V}_{\parallel}}_{\text{new, rel. H-M. (acoustics)}} = 0$$

$$\partial_t \tilde{V}_{\parallel} + \tilde{V}_E \cdot \nabla \langle U_{\parallel} \rangle = - \frac{(\text{let } T_0)}{\bar{m}_i} \nabla_{\parallel} \frac{\tilde{\rho}}{\bar{\rho}} - \frac{\bar{T}_i \nabla_{\parallel} (\tilde{T}_0 / T)}{\bar{m}_i}$$

\downarrow PSFI/PVG (related process)
 \downarrow acoustic response
 \downarrow \tilde{T}_0 / T (phase)

$$\partial_t \frac{\tilde{T}_0}{T} = - \frac{\tilde{V}_E \cdot \nabla \langle U_{\parallel} \rangle}{\bar{T}_i} \Rightarrow \frac{2}{3} \bar{T}_i \nabla_{\parallel} \tilde{V}_{\parallel}$$

\downarrow free energy source
 \downarrow coupling to acoustics

For \tilde{V}_H :

$$\frac{\tilde{T}_i}{T} = \underbrace{-\frac{\tilde{V}_{Er}}{L_{Ti}(-i\omega)} + \frac{2}{3} \frac{k_{H1} \tilde{V}_H}{\omega}}_{\rightarrow \text{drive}}$$

$$\frac{\tilde{T}_i}{T} = -\frac{\tilde{V}_{Er}}{L_{Ti}(-i\omega)} + \frac{2}{3} \cancel{\frac{k_{H1} \tilde{V}_H}{\omega}}$$

then plug into \tilde{V}_H eqn:

$$-i\omega (\tilde{V}_H) = +V_{Ti}^2 \cancel{k_{H1}} \left(\frac{-V_{Er}}{L_{Ti}(-i\omega)} + \frac{2}{3} \frac{k_{H1} \tilde{V}_H}{\omega} \right) + \text{acoustic}$$

$$\tilde{V}_H \left(1 - \frac{2}{3} \frac{k_{H1}^2 V_{Ti}^2}{\omega^2} \right) = -V_{Ti}^2 \left(\frac{k_{H1} \tilde{V}_{Er}}{L_{Ti}(-i\omega) \omega} \right)$$

$$\tilde{V}_H = \frac{-V_{Ti}^2 k_{H1} \tilde{V}_{Er}}{L_{Ti}(-i\omega) \left(1 - \frac{2}{3} \frac{k_{H1}^2 V_{Ti}^2}{\omega^2} \right) \omega}$$

acoustic response perturbed by \tilde{V}_{Er} and V_{Ti}

Then plugging into continuity:

$k_{H1}^2 \ll \omega^2 \rightarrow$ drop polarization.

$$\tilde{V}_H = -i \frac{V_{Ti}^2 k_{H1} \tilde{V}_{Er}}{L_{Ti}(\omega^2) \left(1 - \frac{2}{3} \frac{k_{H1}^2 V_{Ti}^2}{\omega^2} \right)}$$

Thus:

① ② ③ ~ ③

$$(-\omega + i\omega\tau_n) \frac{1}{\tau} \approx 0$$

(retain polarization in ①)

$$+ \cancel{\kappa_{H1}} \left(\frac{+V_{Ti}^2 \kappa_{H1} V_{E1}}{\cancel{\tau} \omega^2 L_{Ti} \left(1 - \frac{2}{3} \frac{\kappa_{H1}^2 V_{He}^2}{\omega^2} \right)} \right) \approx 0$$

$\omega_{*n} > \omega \Rightarrow$ drop 1
paramagnetic with L_{Ti}

$$\omega_{*n} + \frac{\kappa_{H1}^2 V_{He}^2}{\omega^2} \omega_{Ti} \approx 0$$

$$\left[1 - \frac{2}{3} \frac{\kappa_{H1}^2 V_{Ti}^2}{\omega^2} \right]$$

$$M_i = \frac{L_n}{L_{Ti}}$$

$$1 - \frac{2}{3} \frac{\kappa_{H1}^2 V_{Ti}^2}{\omega^2} = - \frac{\kappa_{H1}^2 V_{Ti}^2}{\omega^2} M_i$$

$$M_i = \frac{L_n}{L_{Ti}} = \frac{d \ln T_i}{d \ln} \rightarrow \text{"hence eta-c mode"}$$

and thus:

$$\pm = \frac{k_{\perp}^2 v_{thi}^2}{\omega^2} \left(\frac{2}{3} - n_i \right)$$

$$\omega^2 = k_{\perp}^2 v_{thi}^2 \left(\frac{2}{3} - n_i \right)$$

→ dispersion relation and threshold

$$\omega^3 \rightarrow -\gamma^2 \text{ for } n_i > \frac{2}{3}$$

ITG has critical value of n_i here set by n_i

→ defines "critical value" of n_i

→ onset instability

Kadomtsev & Pogutse '70
Tang '76 reviews

Comments:

① → n_i / ITG mode is fundamentally different from Electron Drift Wave / ITM family.

Recall: contrast

wave $k \rightarrow \infty$

$$EDW \rightarrow \frac{\tilde{n}}{n} = \frac{1}{T} |\phi|^2 + \tilde{h} \rightarrow \text{dissipative}$$

and: $\omega - \omega_* < 0$
 + dissipation. \Rightarrow $\left. \begin{matrix} \text{inverse} \\ \text{negative} \\ \text{dissipation} \end{matrix} \right\} \text{instability}$

ITG/ M_i \rightarrow Boltzmann electrons suffice

Instability is reactive
 Caution: Non-adiabatic electrons can enter ITG - couple branches

\rightarrow What's the physics!

Recall drift wave: now add electrons
Drift + Acoustic

$$1 + k_{\perp}^2 \rho_s^2 = \frac{\omega_{pe}}{\omega} + k_{\perp}^2 \frac{c_s^2}{\omega^2}$$

$\omega = \frac{v_f}{1 + k_{\perp}^2 \rho_s^2}$ acoustic wave show this

\rightarrow drift-acoustic wave. $\omega_* > k_{\perp} v_G$

c.e. $\Delta N \rightarrow 0$: $\omega^2 = k_{\perp}^2 c_s^2 / [1 + k_{\perp}^2 \rho_s^2]$

usually heavily damped \rightarrow L.O.
 parallel sound. enhanced current

(destabilized by current $\frac{1}{2} P$) \rightarrow like COIT work out $\frac{1}{2}$.

analogous: $\omega^2 = k_{\perp}^2 c_s^2 / [1 + k_{\perp}^2 \frac{1}{2} \rho_s^2]$

Acoustic wave:

positive compressibility

$$\omega^2 = k_{\perp}^2 \left(\frac{dP}{d\rho} \right)$$

d.e.

pressure ↑
with density

⇓
compressibility

d.e.
δ ↑ ⇒ \tilde{P} ⇒ div. flow
⇒ reduces \tilde{P} , δ

$$C_s^2 > 0$$

ITG/MI:

Negative compressibility

⇓
instability

$$\omega^2 = k_{\perp}^2 v_{Ti}^2 \left(\frac{2}{3} - \mu_i \right)$$

$\tilde{\rho} \Rightarrow \tilde{P}_b \Rightarrow$ conv. flow
⇒ curved \tilde{P}

$$v_{Ti}^2 = v_{Ti}^2 \left(\frac{2}{3} - \mu_i \right) \frac{d^2 P}{dz^2}$$

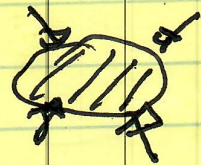
⇓ $\rho < 0$ for $\mu_i > \mu_{crit} = 2/3$.

Familiar

Example of Negative Compressibility??

self-gravitating

Jens Instability!



matter

$$\partial_t \rho + \nabla \cdot (\rho \underline{v}) = 0$$

$$\rho \frac{d\underline{v}}{dt} = -\nabla P + \rho \nabla \phi$$

↓
Gravitational force.

$$\nabla^2 \phi = 4\pi G \rho$$

Poisson's Eqn for Gravity ($1/r^2$ force)

\Rightarrow

$$\partial_t^2 \tilde{\rho} + \rho_0 \partial_t \underline{\underline{v}} = 0$$

$$\partial_t \underline{\underline{v}} = - \frac{\partial^2 \rho_0}{\rho_0} = \nabla^2 \phi$$

$$\partial_t^2 \underline{\underline{v}} - \nabla^2 c_s^2 \left(\frac{\rho_0}{\rho_0} \right) - G \frac{\partial^2 (4\pi \rho_0)}{\rho_0} = 0$$

$$\omega^2 = k^2 c_s^2 - 4\pi G \rho_0$$

classic Jeans dispersion

$$\omega^2 = k^2 c_s^2 \left(1 - \frac{4\pi G \rho_0}{c_s^2 k^2} \right)$$

["Compor"]

$$= \frac{1 - 4\pi G \rho_0}{c_s^2 k^2}$$

Can have negative compression

< 0 for $k < k_J$
 > 0 , $k > k_J$

$$\ell_{\text{Jeans}} \rightarrow \frac{\text{Jeans Length}}{\text{Length}} = \left(\frac{c_s^2}{4\pi G \rho_0} \right)^{1/2}$$

c.e. $\left\{ \begin{array}{l} \text{negative compression for} \\ l \gg \lambda \Rightarrow \text{gravity} \\ \text{overcomes pressure} \Rightarrow \text{collapse} \end{array} \right.$

Why negative compression? \Rightarrow Key Physics Question
acoustics

$$\frac{\partial \tilde{v}_u}{\partial t} = - \frac{c_s^2}{m_c} \nabla_{||} \frac{\rho}{T}$$

$$- v_{thc}^2 \nabla_{||} \left(\frac{\tilde{T}}{T} \right)$$

$\rho p_c = n_0 \tilde{T}_0 + T_0 \tilde{n}$
 $\tilde{n} \sim \frac{\rho}{T}$

Point: \tilde{T}/T not in phase with $\frac{\rho}{T}$
 $\frac{\tilde{T}}{T} \neq \frac{\rho}{T}$

What induces neg compression? $\Rightarrow \frac{\partial \langle T \rangle}{\partial t} \rightarrow$ via coupling to acoustic wave.
 c.e. crudely:

$$\frac{\tilde{T}}{T_0} \approx \frac{-v_p}{-\omega T} \frac{\partial \langle T \rangle}{\partial n} = - \frac{c \omega_p \tau_c}{\gamma} \frac{\rho}{T}$$

\hookrightarrow phase γ phase:

$\frac{1}{\rho_0} \frac{d\rho_0}{dr}$



$$\langle \tilde{v}_r \tilde{T} \rangle \rightarrow -\chi_c \frac{DKT_c}{18}$$

$$\chi_c \sim \langle \tilde{v}_r^2 \rangle \rho_0 \sim \langle \tilde{v}_r^2 \rangle \rho^{-1}$$

→ What is the Full dispersion relation
 check from n, T, v_{th} eqns. + Boltzmann
 DW acoustic DT coupling

$$1 - \frac{\omega_{pi}^2}{\omega^2} - \frac{k_{||}^2 c_s^2}{\omega^2} \left(1 - \frac{\omega_{pi}^2}{\omega} \right) - \frac{5}{3} \frac{k_{||}^2 v_{th}^2}{m_i \omega^2} \left(1 - \frac{\omega_{pi}^2}{\omega} \right) = 0$$

$$1 - \frac{\omega_{pi}^2}{\omega} - \frac{k_{||}^2 c_s^2}{\omega^2} \left(1 - \frac{\omega_{pi}^2}{\omega} \right) - \frac{5}{3} \frac{k_{||}^2 v_{th}^2}{\omega^2} \left(1 - \frac{\omega_{pi}^2}{\omega} \right) = 0$$

→ Is there a "quackie" }

$$\nabla \cdot (\rho \underline{v}) = 0 \quad \left[\text{incompressible mass flow} \right]$$

$$\tilde{v}_r \frac{d\langle n \rangle}{dr} + \cancel{\rho_0 \nabla_{||} v_{p0}} + \rho_0 \nabla_{||} \tilde{v}_r = 0$$

+ $\frac{v_{th}}{T} > \text{eqns.}$
 follows

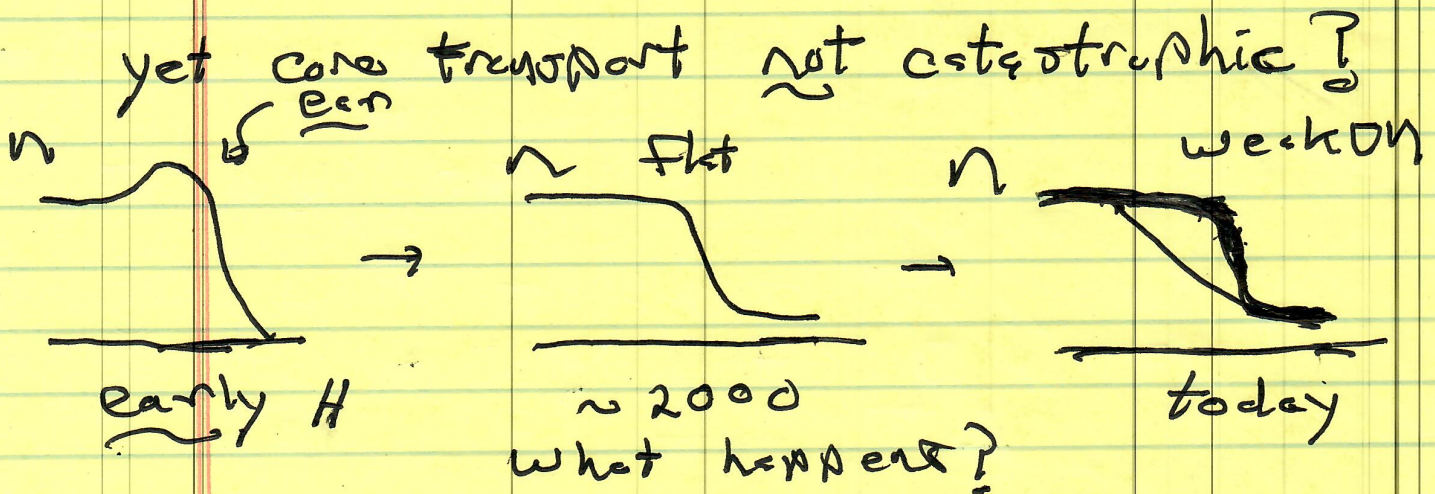
→ What of "Flat Density" Regime?
 ~> n_i large?

→ Gist of n_i mode:

- Peaked density profiles are good!

Alcator-C Pellet, et seq. ⇒ steepen
 DN, reduce n_i s.t. $n_i < n_{icrit}$

- but H-mode density profiles
 @ flat ⇒ $n_i \rightarrow \infty$!



Recall:

$$1 - \frac{\omega_p^2}{\omega} = \frac{k_{\perp}^2 c_s^2}{\omega^2} \left(1 - \frac{\omega_p^2}{\omega} \right) = k_{\perp}^2 \frac{5}{3} \frac{v_{th}^2}{\omega^2} \left(1 - \frac{\omega_p^2}{\omega} \right)$$

= 0

take $\omega_{*n} \rightarrow 0 \iff \nu_n \rightarrow 0$

$$1 - \frac{k_{||}^2 c_s^2}{\omega^2} \left(1 - \frac{\omega_{*Ti}}{\omega}\right) - \frac{5}{3} \frac{k_{||}^2 v_{Ti}^2}{\omega^2} = 0$$

$\omega_{*Ti} > \omega \implies \left\{ \begin{array}{l} \nu_{Ti} \text{ strong, for} \\ \text{simplcity} \end{array} \right.$

$$1 + \frac{k_{||}^2 c_s^2}{\omega^3} \omega_{*Ti} = 0$$

$$\omega = (-1)^{1/3} \left(k_{||}^2 c_s^2 \omega_{*Ti} \right)^{1/3}$$

instability!
(Threshold not addressed)

- flat density " ITG (not n_i)
- $\omega_{rj} \gamma$ set by ν_{Ti}
- no odd behavior, $\nu_n \rightarrow 0$.
- balances $\nabla_{||} \tilde{v}_{||}$ with $\frac{\partial n_i}{\partial t}$
- will be a cross-over value of ν_n .

⇒ 'Flat density' ITG ^{is}

one reason why ~~ITG~~ becomes

"ITG": { Can also have 'flat density' drift/TEM → DTG ⇒ wave
DTG ⇒ drives

→ Accuracy }

→ Fluid theory, not accurate for threshold, useful for physical understanding

- $\omega^2 = k_{\perp}^2 V_{ti}^2 \left(\frac{2}{3} - M_i \right)$

$\omega^2 < 0 \Rightarrow \omega - k_{\perp} V_{th}$ easily resonant

⇒ Kinetics

• ion Landau damping enters

→ PV }

shear flow can modify significantly → limits shift }

- $\nabla_{\perp} \tilde{V}_{\perp}$ breaks PV conservation of H-M.

⇒ can formulate PV budget, Potential enstrophy budget. Useful.

→ Related? - { PSFI, PVG, ... } { Parallel shear flow instability }

$\nabla \langle V_{||} \rangle$ driver instability! (S)

So what? - shear flow! ... (R)

Negative compression, not KH! Inf. \tilde{R}_L (S)
↓
acoustic coupling!

⇒ 'relative' of ITG/ M_i ⇒ PSFI

⇒ couples linearly to ITG/ M_i .

⇒ rather delicate, but active.

To clarify, put $\begin{cases} \nabla T \rightarrow 0 \\ \nabla n \rightarrow 0 \end{cases}$, $\underline{T}_i \rightarrow 0$

$$\partial_t \frac{1}{T} \phi + \nabla_{||} \tilde{V}_{||} = 0$$

$$\partial_t \tilde{V}_{||} = -V_{Ez} \partial_n \langle V_{||} \rangle - c_s^2 \nabla_{||} \frac{1}{T} \phi$$

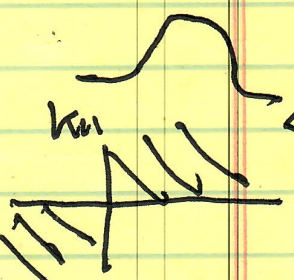
$$\frac{d^2}{dt^2} \frac{1}{T} \vec{\phi} + \nabla_{\mathbf{u}} \left(-V_{\text{en}} \partial_n \langle V_{\mathbf{u}} \rangle - C_s^2 \nabla_{\mathbf{u}} \frac{1}{T} \vec{\phi} \right) = 0$$

$$-\omega^2 = k_{\parallel} k_{\perp} \rho_s C_s \partial_n \langle V_{\mathbf{u}} \rangle + k_{\perp}^2 C_s^2 = 0$$

$$\begin{aligned} \omega^2 &= -k_{\parallel} k_{\perp} \rho_s C_s \partial_n \langle V_{\mathbf{u}} \rangle + k_{\perp}^2 C_s^2 \\ &= -k_{\perp} C_s (k_{\parallel} \rho_s \partial_n \langle V_{\mathbf{u}} \rangle - k_{\perp} C_s) \end{aligned}$$

Need $-k_{\parallel} \rho_s \partial_n \langle V_{\mathbf{u}} \rangle > k_{\perp} C_s$ } for stability
 \Rightarrow criterion on $\partial_n \langle V_{\mathbf{u}} \rangle$

$-k_{\parallel} k_{\perp} \rho_s \partial_n \langle V_{\mathbf{u}} \rangle > 0$ for $\partial_n \langle V_{\mathbf{u}} \rangle < 0$

 \Rightarrow spectral asymmetry } required device

\Rightarrow clearly negative compression \downarrow
 $\Rightarrow \partial \langle V_{\mathbf{u}} \rangle$ induced needed phase.

\Rightarrow DN stabilizing, (as M_i)

- coupled to ITG. cf. N Matter, PD.
and ultimately $\chi_p \sim \chi_i$

PSFI most important in strong
rotation, flat n regimes \Rightarrow
cone H-mode, with NBI, strong.

\rightarrow Also: Toroidal ITG

\rightarrow [curvature driven

\rightarrow [commonality with
FLR stabilized interchange
 $[\omega_0 \omega_{*p_i} \text{ vs } \omega_{*n}^2$

$\rightarrow R/L_{Ti}$, L_n/L_{Ti} are
critical parameters.

\rightarrow Fluid, but Mechanism
different than negative
compression.

→ (Zonal) Flows and Saturation

→ clearly $\nabla \cdot \underline{V}_{pol} \rightarrow \frac{d}{dt} \nabla_{\perp}^2 \phi$
 $\rightarrow \partial_r \langle \tilde{v}_r \nabla_{\perp}^2 \tilde{\phi} \rangle$

⇒ ITG generates zonal flows ↓

⇒ additional coupling from diamagnetic contribution

⇒ shear feedback, as usual

also Zonal eqns:

→ $\underbrace{\partial_r \langle \tilde{v}_r \tilde{T} \rangle + \frac{d}{dt} \langle T \rangle + \dots}_{\text{Zonal}} = 0$

⇒ Ion temperature profile corrugations formed. $\left\{ \begin{array}{l} \phi_z \\ \delta T_z \end{array} \right.$

also

→ $\underbrace{\partial_t \langle v_{||} \rangle + \partial_r \langle \tilde{v}_r \tilde{v}_{||} \rangle + \dots}_{\text{Zonal}} = 0$

⇒ (Zonal) acoustic flows generated.

Note:

$$\tilde{V}_{ii} = - \frac{i v_{Ti}^2 k_{ii} \tilde{V}_{Er}}{L_{Ti} \omega^2 (1 - \text{scw})}$$

\downarrow
 $\omega_r^2 + 2i\gamma\omega_r - \gamma^2$

so

$$\langle \omega_r \tilde{V}_{ii} \rangle = + \pi_r \frac{\partial \langle T_i \rangle}{\partial r}$$

\downarrow symmetry?

$$\pi_r = \rho \left\{ \sum_n |v_{rn}|^2 \epsilon_i \frac{v_{Ti}^2 k_{ii}}{T_i (\omega_r + 2i\gamma\omega_r - \gamma^2)} \right\}$$

c.e. they:

$$\partial_t \langle dV_{ii} \rangle = - \partial_r \left(\pi_r \frac{\partial \langle T_i \rangle}{\partial r} \right)$$

$\nabla \langle T_i \rangle$ drives parallel flow
 \Rightarrow welcome to intrinsic rotation!

→ Flows driven by:

$$Q_i \rightarrow \nabla T_i \rightarrow \langle \tilde{U}_r \tilde{U}_u \rangle \rightarrow \langle U_u \rangle$$

Plasma can rotate without torque.

→ symmetry breaking required.

What sets $\langle U_u \rangle$?

also \times effect in dynamics.

TBC.

also: Impurity Modes