

9 Big Ideas

Here we list 9 “big ideas” in fundamental plasma physics from a previous 218A course. These are the key points one should glean from the course.

- i) **Coulomb force as long range**
 - a) Screening, λ_D , $n\lambda_D^3 > 1$ for “plasma” state
 - b) Difference from hard sphere gas
 - c) Infrared divergence – Coulomb logarithm

- ii) **Waves and Instabilities**
 - a) Plasma, ion-acoustic, EM
 - b) Wave Energy Theorem, Adiabatic Theory for Waves
 - c) Negative Energy Waves, Instabilities → how dissipation can be destabilizing
 - d) Two Stream Instability - bunching

- iii) **Nonlinear Waves**
 - a) Steepening and breaking mechanisms
 - b) Collisional and collisionless shocks/solitons
 - c) Collisionless shock models

- iv) **Kinetics**
 - a) Vlasov Equation from BBGKY hierarchy
 - b) Landau Damping
 - c) Physics of Landau Damping — phase mixing
 - d) Landau Growth, B-O-T instability, CDIA

- v) **Near Thermal Equilibrium: How to Compute Fluctuation Spectrum**
 - a) Fluctuation-Dissipation Theorem
 - b) Test Particle Model
 - c) Equilibrium Fluctuation Spectrum

- vi) **Transport and Relaxation Near Equilibrium**
 - a) Diffusion, Central Limit Theorem, Fokker-Planck Eqn.
 - b) Boltzmann Eqn. + small momentum transfer → Landau Collision Operator
Lenard-Balescu Eqn., via TPM and Relation to Landau Collision Operator
 - c) Rosenbluth Potentials and Calculation
 - d) Dreicer Field for runaway electrons

- vii) **Mean Field Theory for Instability Evolution**
 - a) Quasi-Linear Equations
 - b) Relation to Chaos, Time Scales
 - c) τ_{ac} vs τ_b , validity of unperturbed orbits
 - d) Energy-Momentum Theorems for mean field theory
 - e) Bump-on-Tail Saturation
 - f) Anomalous Resistivity

viii) **Paradigms of Turbulence**

- a) Nonlinear evolution \rightarrow turbulence
- b) K41 paradigm \rightarrow singularity via *enstrophy production* \rightarrow *cascade*
- c) Langmuir Turbulence \rightarrow singularity via *collapse* \rightarrow Disparate Scale Interaction

ix) **Rayleigh-Taylor Instability – A Case Study in Macroscopics**

- a) Release of free energy
- b) Different cases, limits – b.c.'s, profiles, stabilization, dissipation
- c) Linear \rightarrow nonlinear transition
- d) Nonlinear structure (spike and bubble)