

Problem 1 (10 pts)

An ideal gas has 32,000 molecules moving with velocity in the x direction in the range -1m/s to 1m/s, and 16,000 molecules moving with velocity in the x direction in the range 199m/s to 201m/s .

- Approximately how many molecules are moving with velocity in the y direction between 198m/s and 202m/s?
- How many molecules are moving with velocity in the x direction between 399m/s and 401m/s?
- If this ideal gas is oxygen (molecular weight 32), what is its temperature, in K?
- If the temperature is increased by a factor of 2, does the number of molecules with velocity in the x direction in the range -1m/s to 1m/s increase, decrease or stay the same? Justify your answer.
- Same as (d) for the number of molecules with velocity in the x direction in the range 199m/s to 201m/s.

Use $k/u=8311\text{m}^2/(\text{s}^2\text{K})$ (u =unified atomic mass unit, k =Boltzmann constant)

Problem 2 (10 pts)

1.5 kg of ice at temperature $-20\text{ }^\circ\text{C}$ are put into 2kg of water at temperature T . What happens is either: (i) all the ice melts; (ii) part of the ice melts; (iii) part of the water freezes.

- Explain why "(iv) all the water freezes" can't happen.
- Find for which ranges of T (in $^\circ\text{C}$) the outcomes (i), (ii) and (iii) will occur.
- If the outcome is that exactly half of the ice melts, what was the initial water temperature T ? (in $^\circ\text{C}$)

Ignore any heat flow to the surroundings

Specific heat of ice $2.1\text{kJ/kg }^\circ\text{C}$, of water $4.186\text{kJ/kg }^\circ\text{C}$, heat of fusion of ice 333kJ/kg

Problem 3 (10 pts+3 extra credit)

n moles of a monoatomic ideal gas at temperature T_1 occupying volume V_1 expand quasistatically at constant pressure to volume $V_2=3V_1$, absorbing 50,000 J of heat in the process.

- What is the final temperature, T_2 , in terms of T_1 ?
- How much work (in J) did the gas do in this process? Did its internal energy increase or decrease? By how much (in J)?
- Subsequently, the gas is compressed adiabatically (and quasistatically) back to volume V_1 . Find the final temperature, T_3 , in terms of T_1 .
- Draw these processes in a PV diagram.
- (for extra credit) Find the work done in the adiabatic compression, in J.