Problem 1 (10 pts)


A body of mass 2.8 g floats on water (density of water $=1 \mathrm{~g} / \mathrm{cm}^{3}$ ) with $70 \%$ of its volume submerged. In another liquid, this body sinks to the bottom and has weight corresponding to an apparent mass of 2.0 g . Find:
(a) The volume of the body, in $\mathrm{cm}^{3}$.
(b) The density of the other liquid, in $\mathrm{g} / \mathrm{cm}^{3}$.

Problem 2 (10 pts)


There is water flowing through the pipe shown above, from left to right. The radius on the left side is $r_{1}$, on the right side $r_{2}$, with $r_{2}<r_{1}$. The pressure difference between both sides is $\Delta \mathrm{P}=6 \mathrm{kPa}$.
(a) Which side has higher pressure, right or left? Justify.
(b) Find an expression for the speed of water flow on the right side, $v_{2}$, in terms of the pressure difference $\Delta \mathrm{P}$, the water density $\rho$ and the radii of both sides $r_{1}, r_{2}$.
(c) With $r_{1}=5 \mathrm{~cm}, r_{2}=3 \mathrm{~cm}$ and the density of water $1000 \mathrm{~kg} / \mathrm{m}^{3}$, find the speed of water flow on both sides, in $\mathrm{m} / \mathrm{s}$, and the volume rate of flow, in $\mathrm{m}^{3} / \mathrm{s}$.

Problem 3 (10 pts +5 pts extra credit)


The container shown in the figure is filled with mercury $(\mathrm{Hg})$, of density $13.6 \mathrm{~g} / \mathrm{cm}^{3}=13,600 \mathrm{~kg} / \mathrm{m}^{3}$, and there is a weightless piston resting on its surface that can move freely, that has on top of it two weights of mass 50 kg each. The container has cross-sectional area $100 \mathrm{~cm}^{2}$. The inverted glass tube has its open end inside the container, and is filled with Hg up to height h above the surface of Hg in the container. On the top part of the glass tube there is vacuum. The cross section of the glass tube is $1 \mathrm{~cm}^{2}$. Atmospheric pressure is $\mathrm{P}_{0}=1 \mathrm{~atm}=1.013 \times 10^{5} \mathrm{~N} / \mathrm{m}^{2}$.
(a) What is the height h of the column of Hg in the glass tube, in cm ? Hint: it is not 76 cm .

Suppose now one of the 50 kg weights is removed, the other one remains:
(b) What is the new height of the Hg column, in cm ?
(c) By how much (in cm ) did the piston move up when the 50 kg weight was removed?
(d) What is the work (in Joules) that was done to move the piston up when the weight was removed?
(e) Explain where the energy to do the work calculated in (d) came from. Make a semiquantitative estimate of the energies involved to verify that your explanation makes sense.

