

PHYSICS 1B – Fall 2009



Electricity & Magnetism



Professor Brian Keating
SERF Building. Room 333

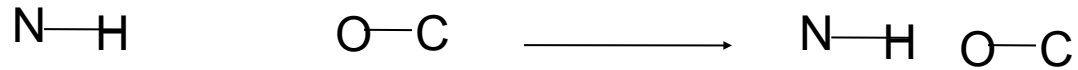
Wednesday October 14, 2009

16.1 PART 2 & 16.2 ELECTRIC POTENTIAL (CONTINUED)

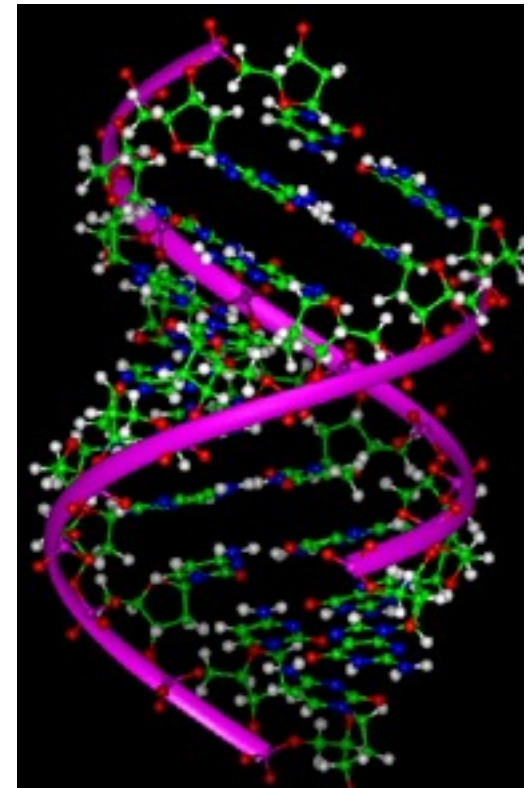
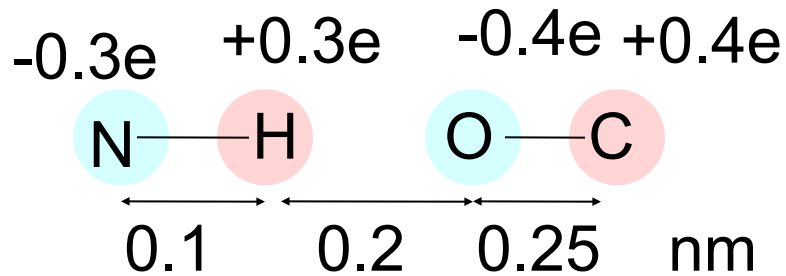
Quiz grades: on the web by last 5 digits of your PID
number

Average was an 7 with a standard deviation of 2.

Hydrogen Bond

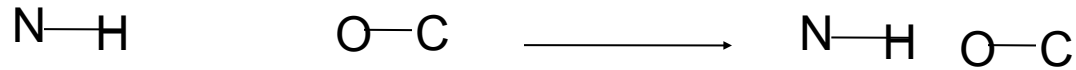


The hydrogen bond energy can be estimated by partial charges

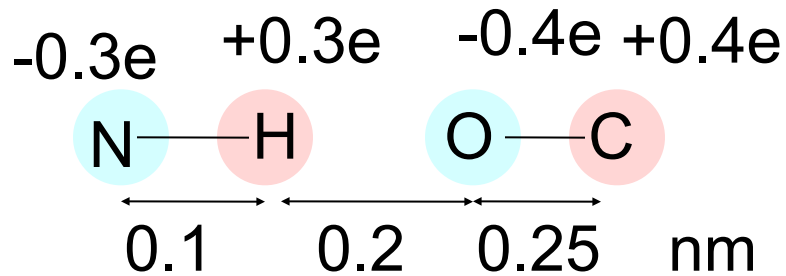


DNA

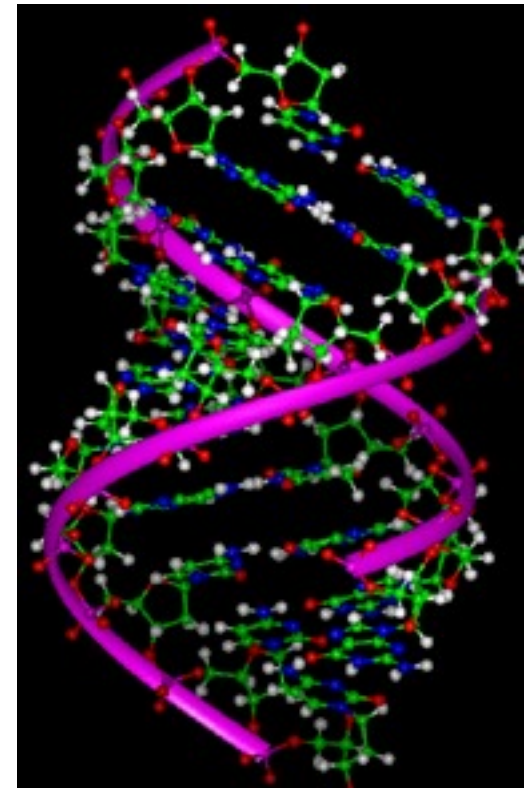
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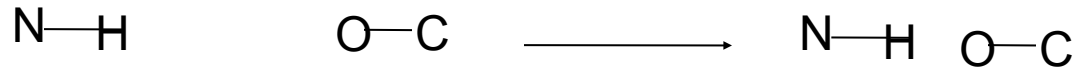


$$\text{bond energy} = \sum \frac{kq_i q_j}{r_{ij}} \quad (\text{scalar sum})$$

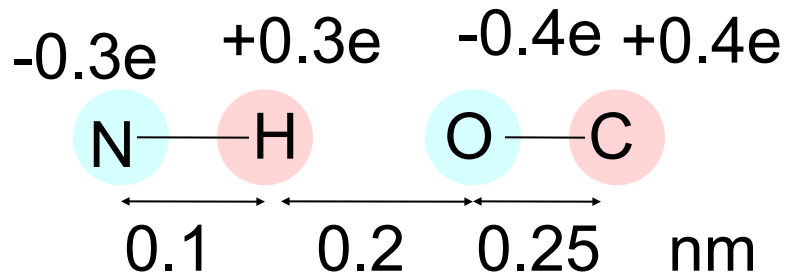


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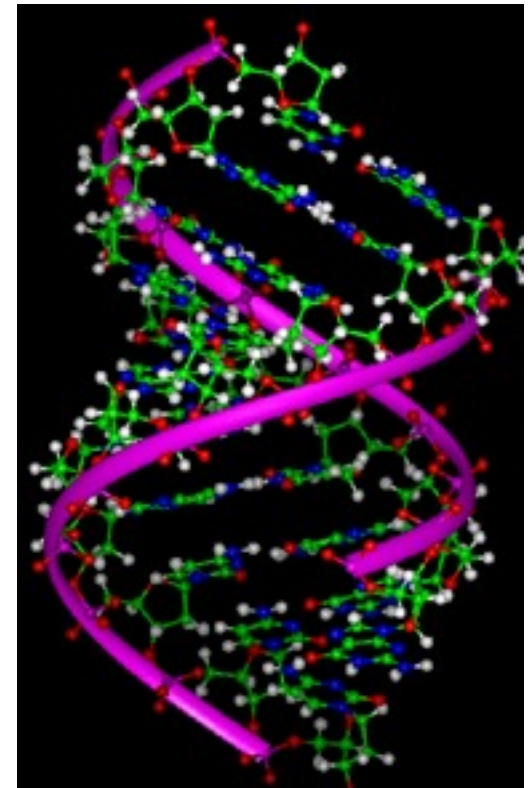


The hydrogen bond energy can be estimated by partial charges



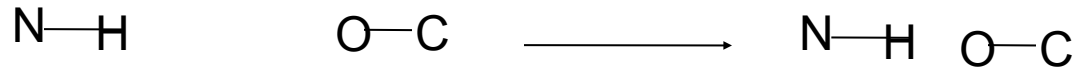
$$\text{bond energy} = \text{sum} \frac{kq_i q_j}{r_{ij}} \quad (\text{scalar sum})$$

$$\Delta \text{PE} = \frac{ke^2}{10^{-9}} \left(\frac{(-.3)(-.4)}{.1+.2} + \frac{-.3(.4)}{.1+.2+.25} + \frac{+.3(-.4)}{.2} + \frac{.3(.4)}{.2+.25} \right)$$

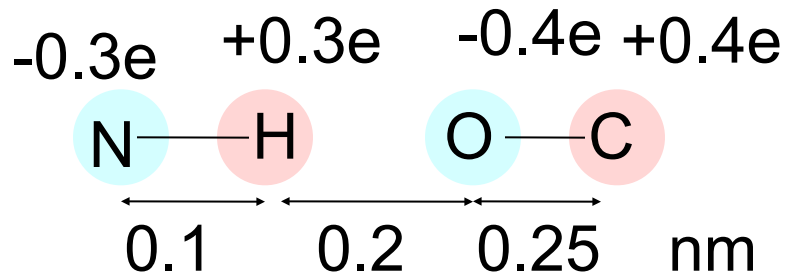


DNA

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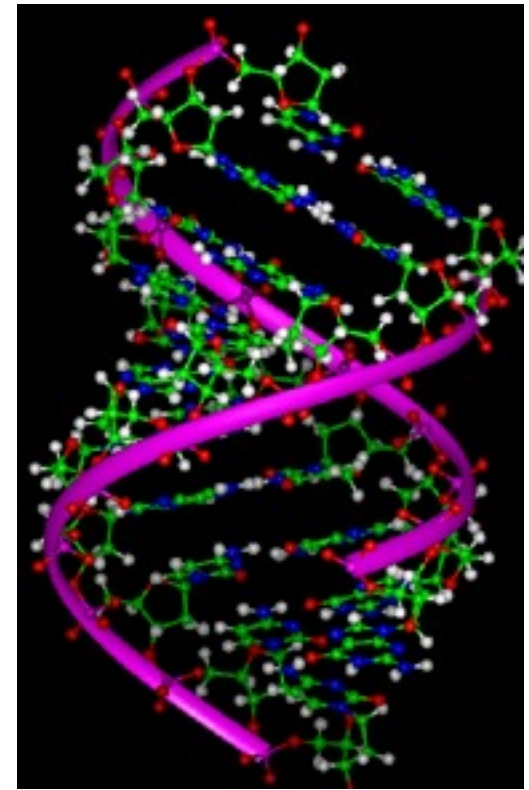


The hydrogen bond energy can be estimated by partial charges



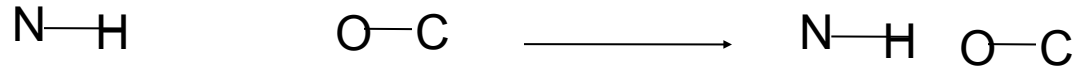
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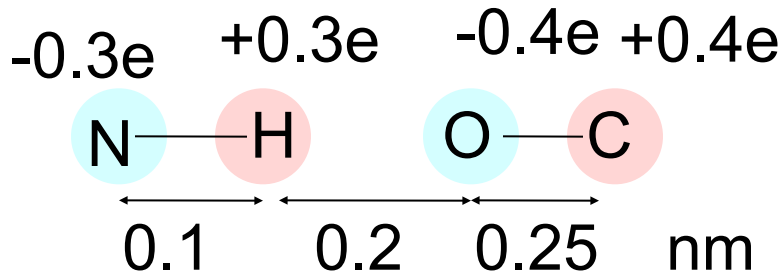


DNA

Hydrogen Bond



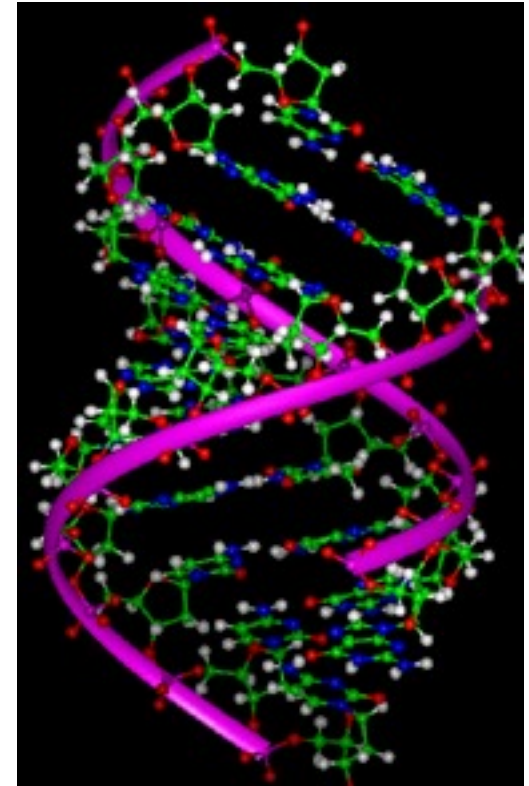
The hydrogen bond energy can be estimated by partial charges



bond energy = sum $\frac{kq_i q_j}{r_{ij}}$ (scalar sum)

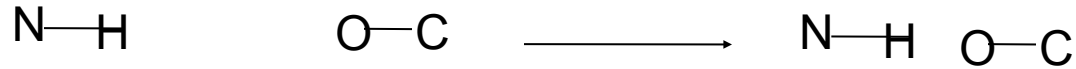
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$$\Delta PE = -0.22 \text{ eV}$$

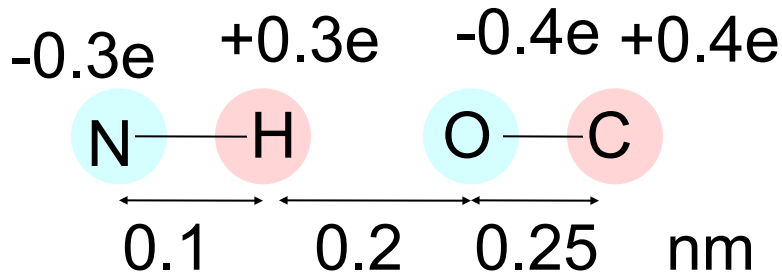


DNA

Hydrogen Bond



The hydrogen bond energy can be estimated by partial charges

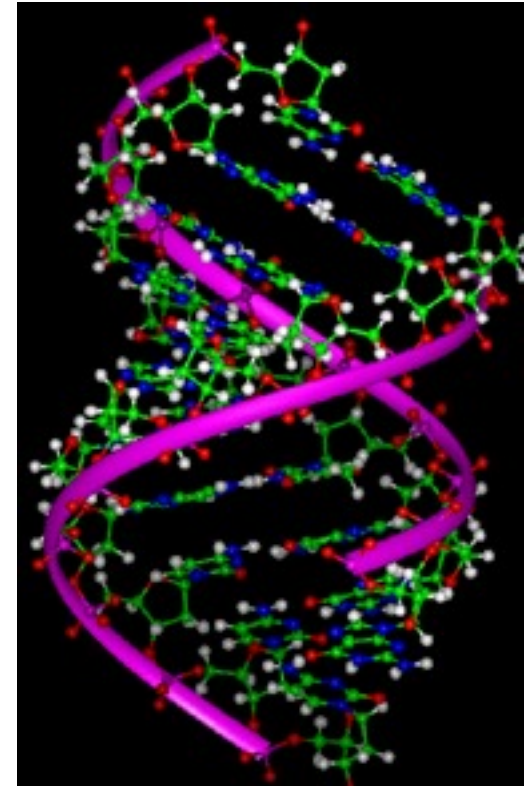


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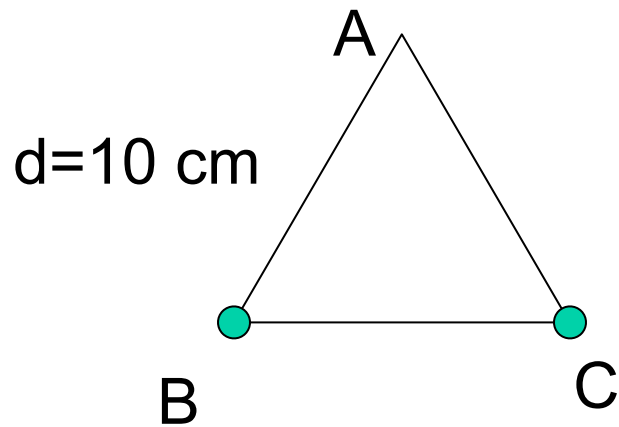
$$\Delta PE = -0.22 \text{ eV}$$

Weaker than a ionic bond but still significant.

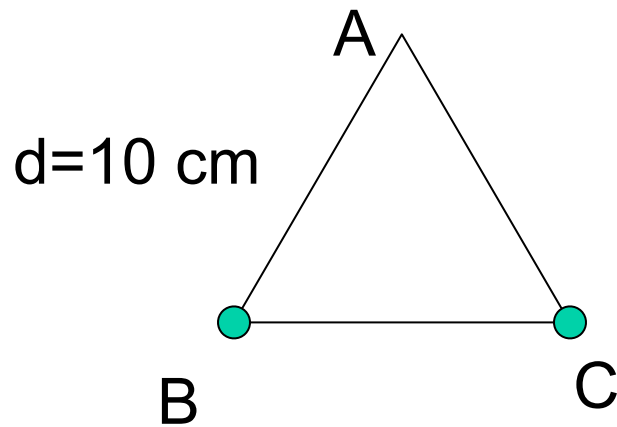


DNA

Two charges of $+q$ each are placed at corners of an equilateral triangle, with sides of 10 cm. If the Electric field due to each charge is 100 V/m at the A find the potential at A



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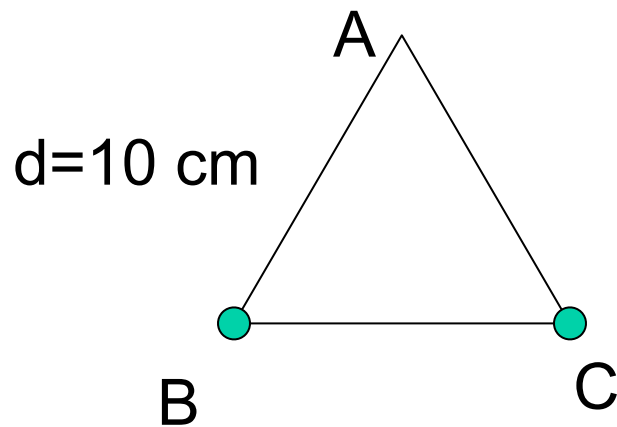


V at A due to each charge

$$E = \frac{k_e q}{r^2}$$

$$V = \frac{k_e q}{r}$$

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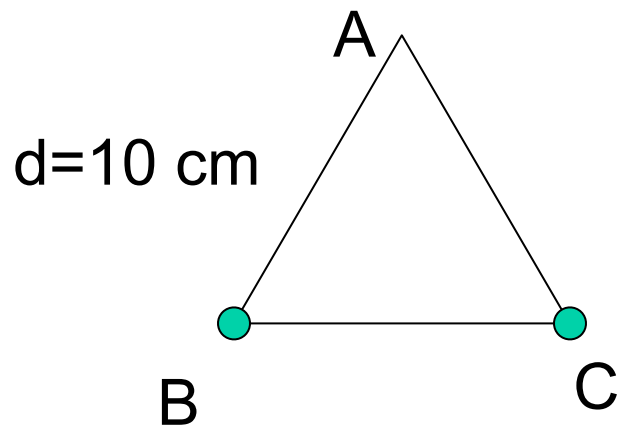
$$E = \frac{k_e q}{r^2}$$

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$$\frac{E}{V} = \frac{1}{r}$$

$$V = Er = 100(0.1) = 10V$$

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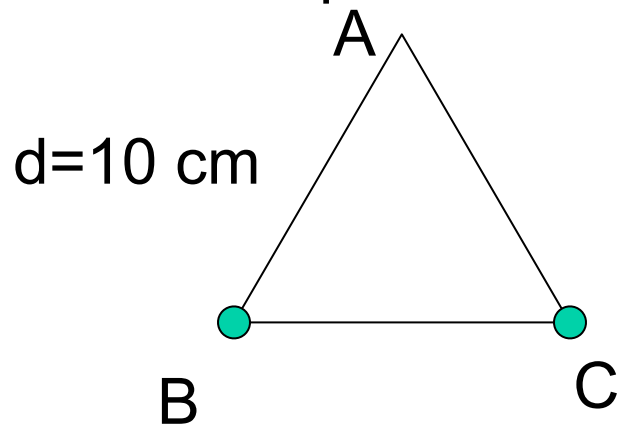
$$V = Er = 100(0.1) = 10V$$

$$V_{\text{total}} = V_{BA} + V_{CA} = 2V = 20 \text{ V}$$

Potential is a scalar

Two charges of $+q$ each are placed at corners of an equilateral triangle, with sides of 10 cm. The Electric field due to each charge is 100 V/m at A.

What is the potential at A?

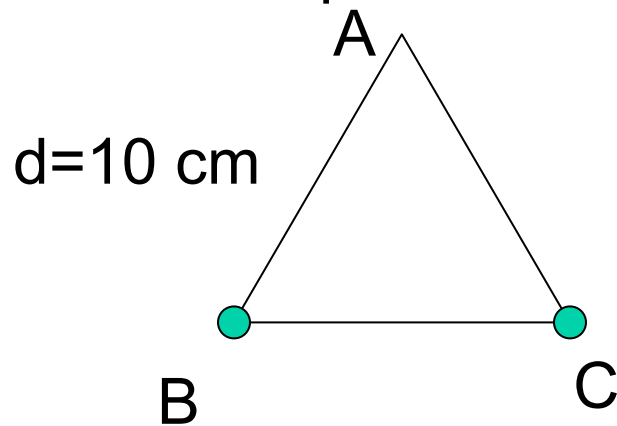


- A. 10V
- B. 100V
- C. 1000V



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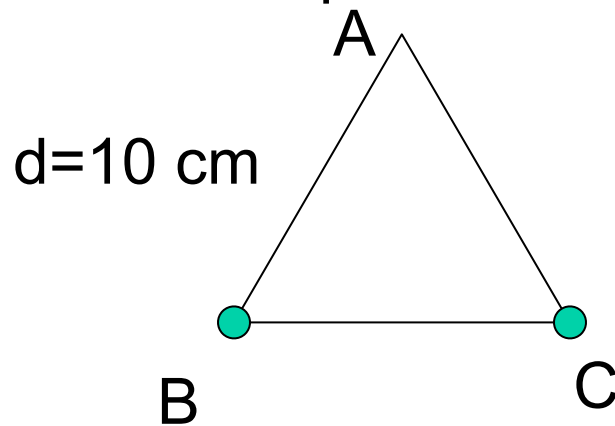
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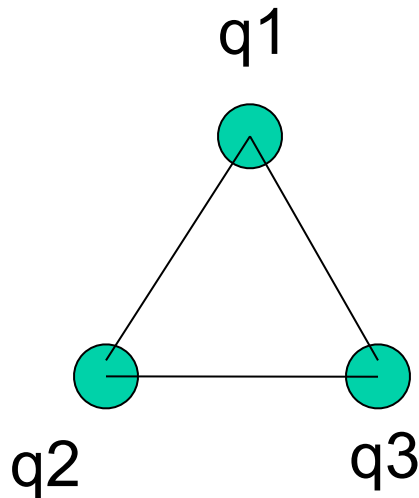
Potential is a scalar

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3 charges of 1×10^{-9} C are placed at the corners of an equilateral triangle. Each side of the triangle has a length of 1.0 cm. Find the work needed to bring the charges together from a long distance away.

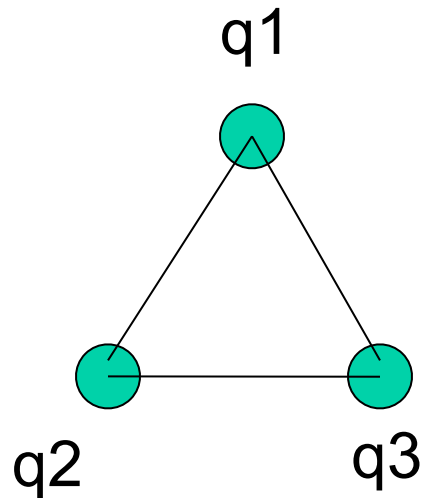


PE due to Coulomb interaction

How many interactions?

PE =

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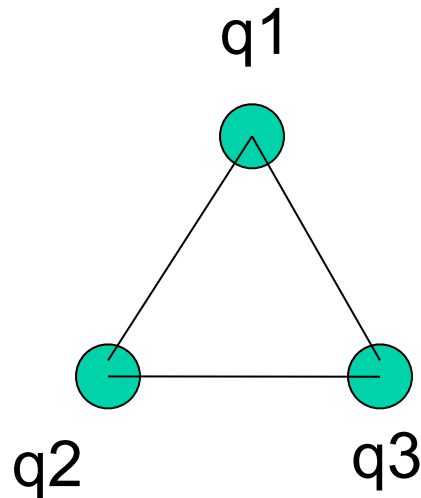


PE due to Coulomb interaction

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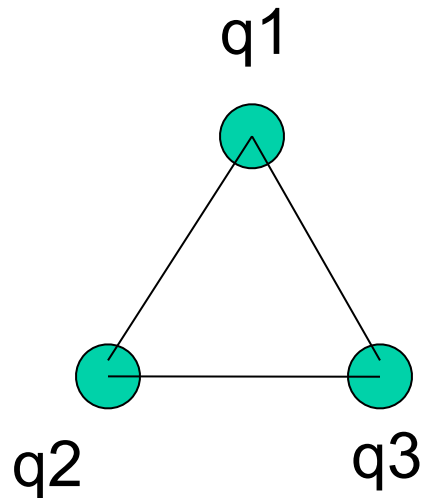


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$$PE = PE_{12} + PE_{13} + PE_{23}$$

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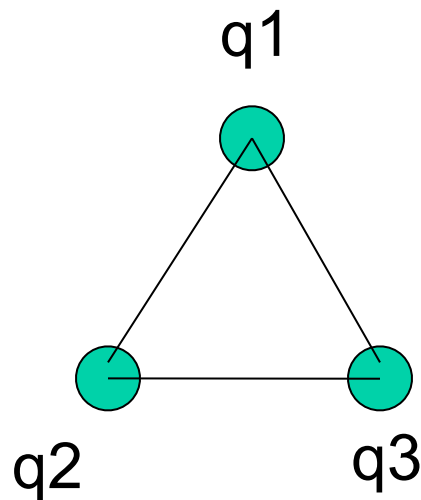
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$$PE = PE_{12} + PE_{13} + PE_{23}$$

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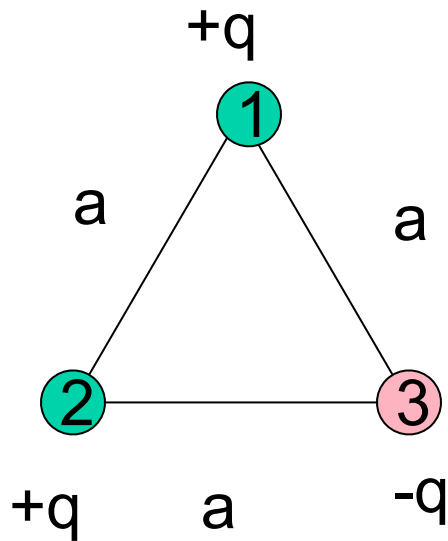
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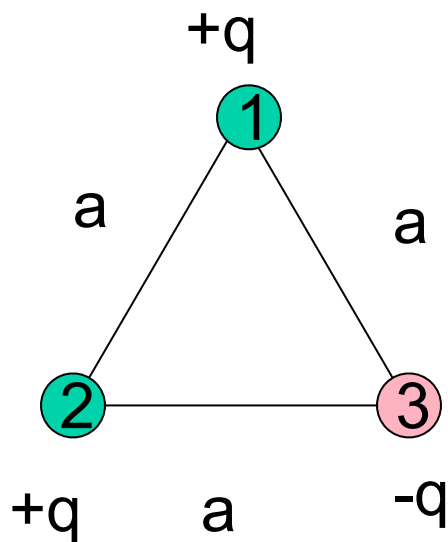
$$PE = 3 \frac{k_e q^2}{r}$$

$$PE = 3 \frac{9 \times 10^9 (1 \times 10^{-9})^2}{(0.01)^2} = 2.7 \times 10^{-4} \text{ J}$$

The following charges are brought together from a large distance away. What is the change in PE? Is the charge distribution stable? (i.e. does it have a negative PE)



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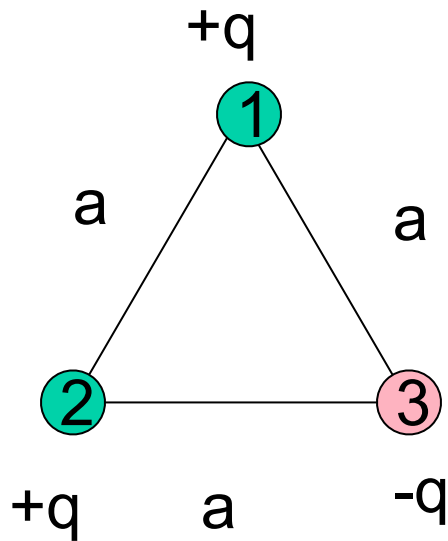
How many interactions?

How many positive?

How many negative?

What is the total change in PE?

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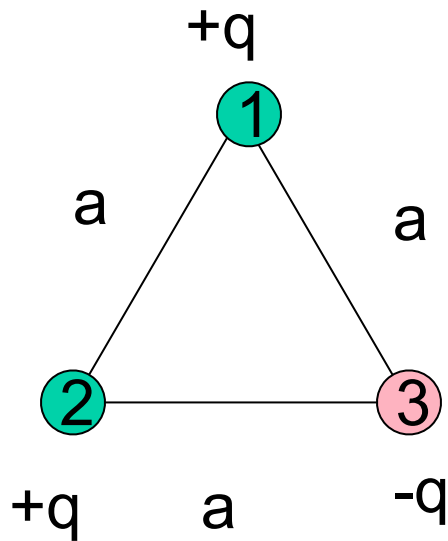
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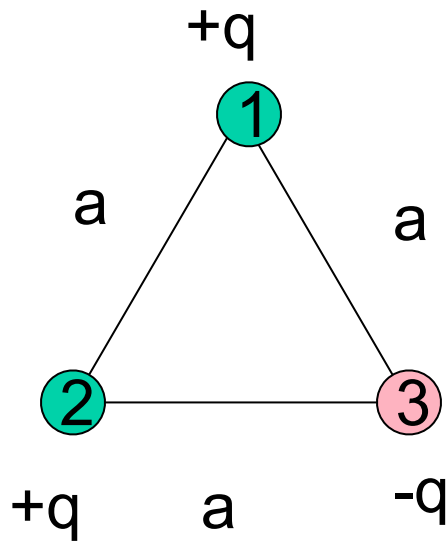
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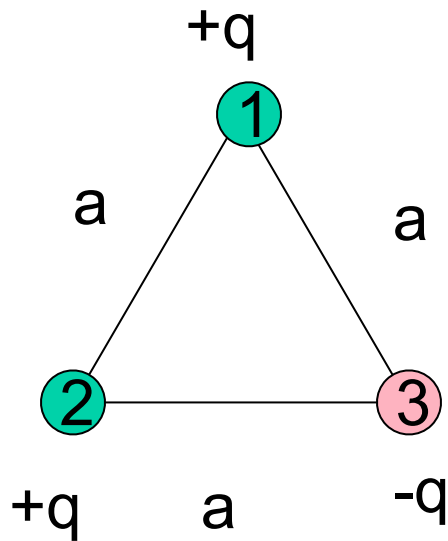
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How many negative? 2

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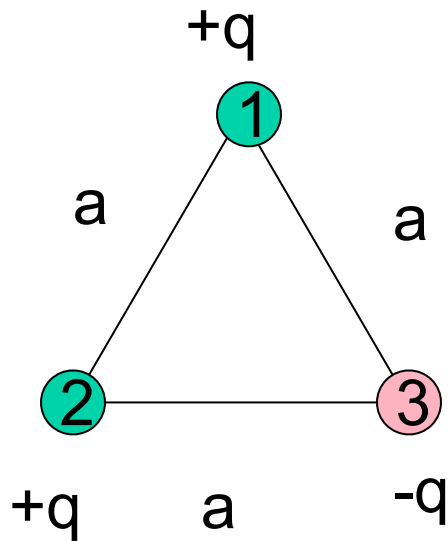
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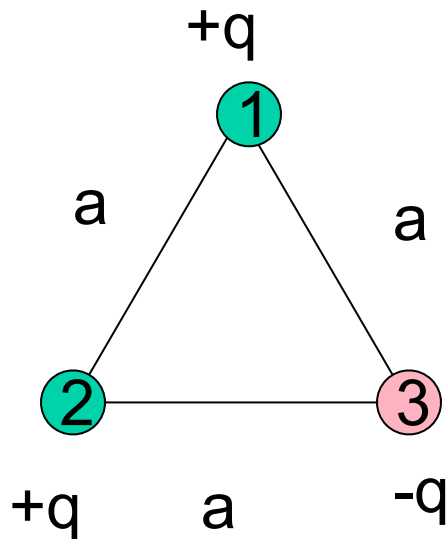
How many negative? 2

What is the total change in PE?

$$PE = PE_{12} + PE_{13} + PE_{23}$$

$$PE = PE_0 - 2PE_0 = -PE_0 = -\frac{k_e q^2}{a}$$

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How many interactions? 3

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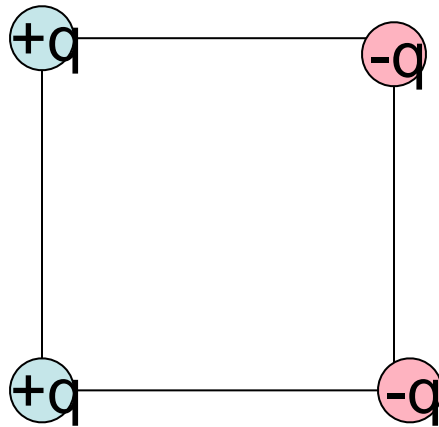
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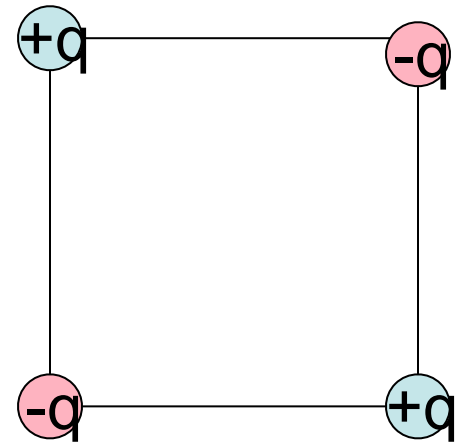
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STABLE

Which of the charge distributions is the most stable?
(has the lowest PE)



A. This one

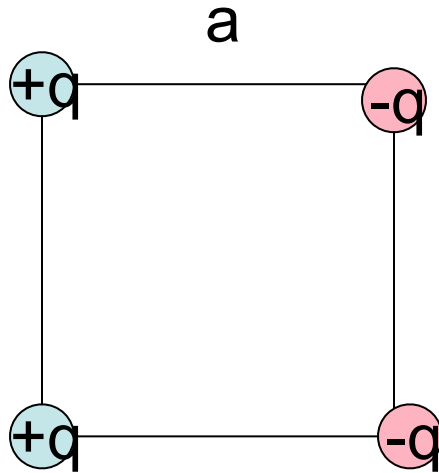


B. This one

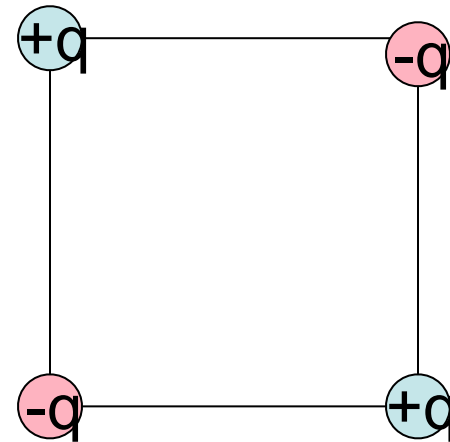


Which of the charge distributions is the most stable?
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$$PE_0 = \frac{k_e q^2}{a}$$



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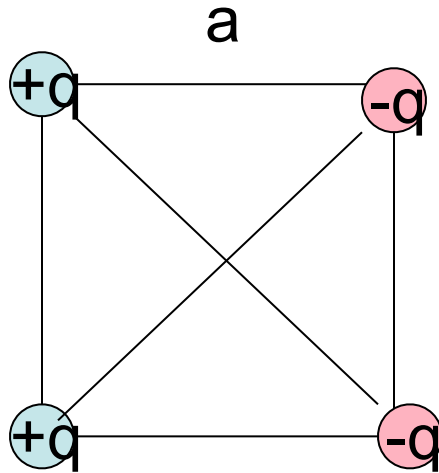


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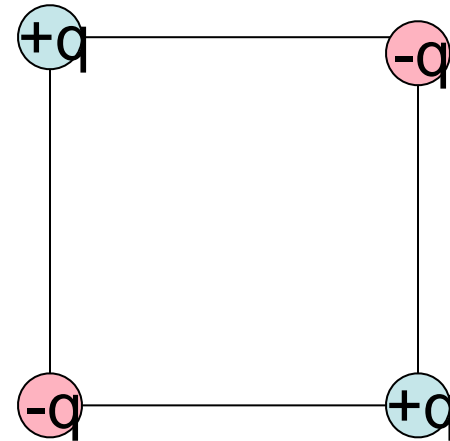


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A. This one



B. This one

PE_0

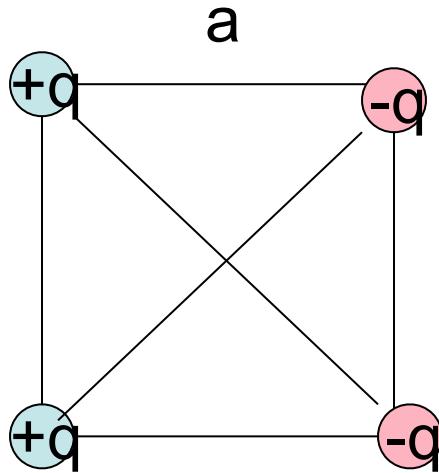
$PE_0/\sqrt{2}$

Total PE

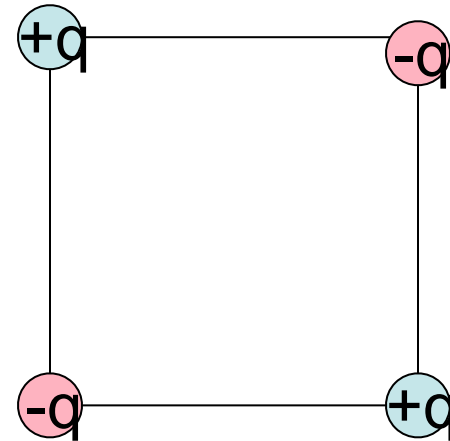


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B. This one

PE₀ +2 -2

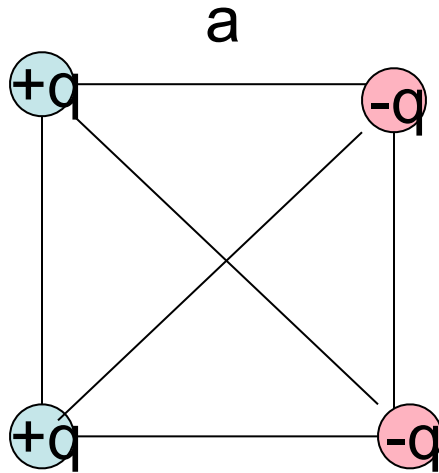
PE₀/√2

Total PE

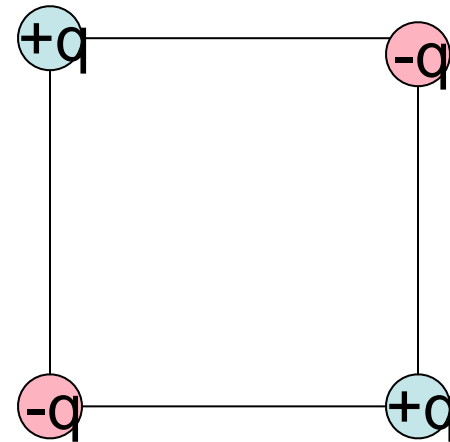


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B. This one

PE_0	+2	-2
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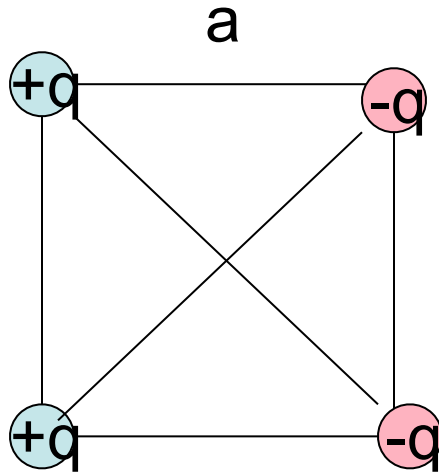
$PE_0/\sqrt{2}$		-2
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Total PE

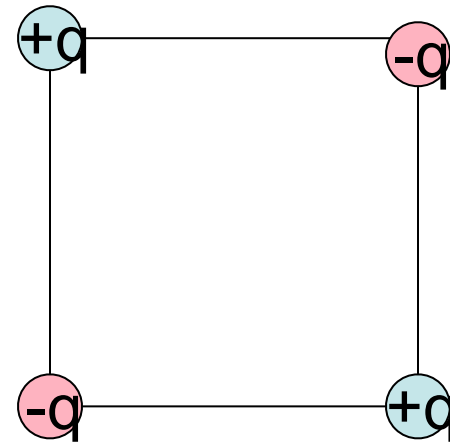


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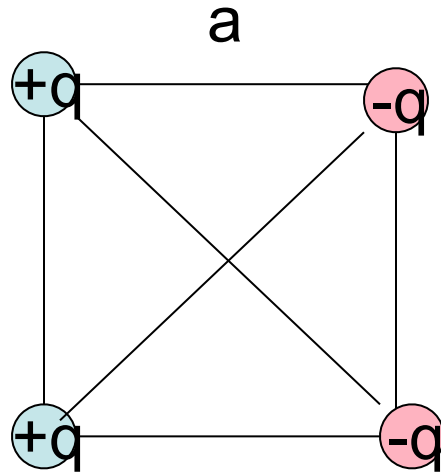
Total PE

$$-\frac{2}{\sqrt{2}} PE_0 = -1.4 PE_0$$

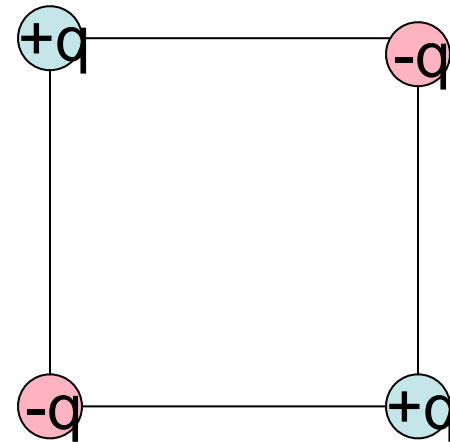


Which of the charge distributions is the most stable?
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A. This one



B. This one

PE_0	+2	-2
--------	----	----

$PE_0/\sqrt{2}$		-2
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Total PE

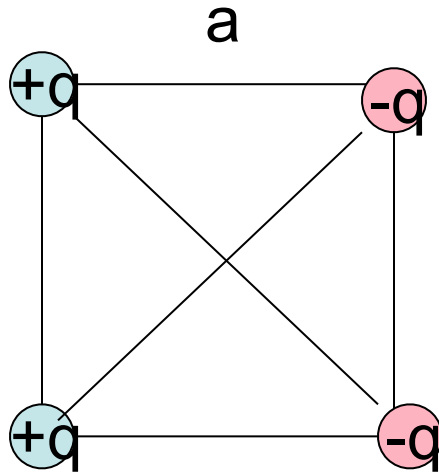
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-4

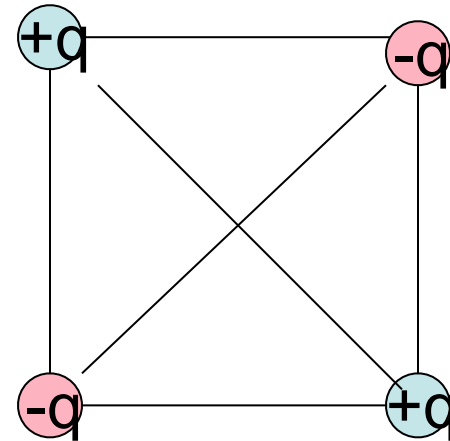


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$$PE_0 = \frac{k_e q^2}{a}$$



A. This one



B. This one

PE_0

+2

-2

$PE_0/\sqrt{2}$

-2

+2

-4

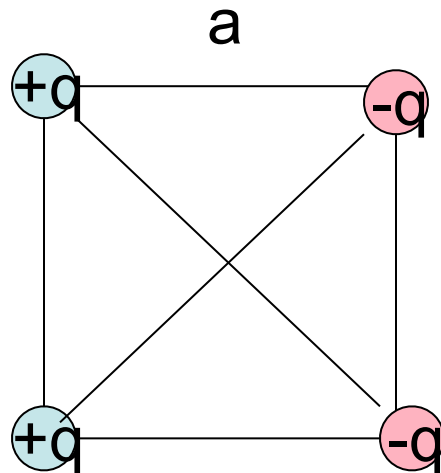
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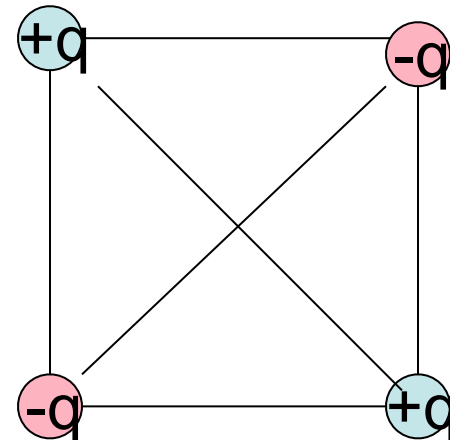


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$PE_0/\sqrt{2}$		-2
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Total PE	$-\frac{2}{\sqrt{2}} PE_0 = -1.4 PE_0$
----------	--

-4

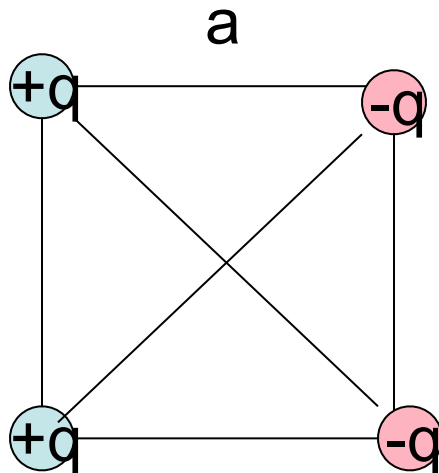
+2

$(-4 + \frac{2}{\sqrt{2}}) PE_0 = -2.6 PE_0$
--

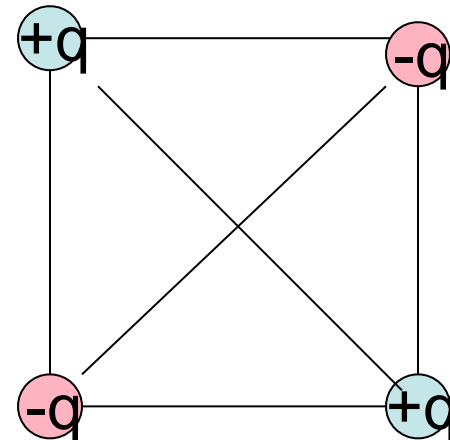


Which of the charge distributions is the most stable?
(has the lowest PE)

$$PE_0 = \frac{k_e q^2}{a}$$



A. This one



B. This one

STABLE

PE_0	+2	-2
--------	----	----

$PE_0/\sqrt{2}$		-2
-----------------	--	----

Total PE	$-\frac{2}{\sqrt{2}}PE_0 = -1.4PE_0$
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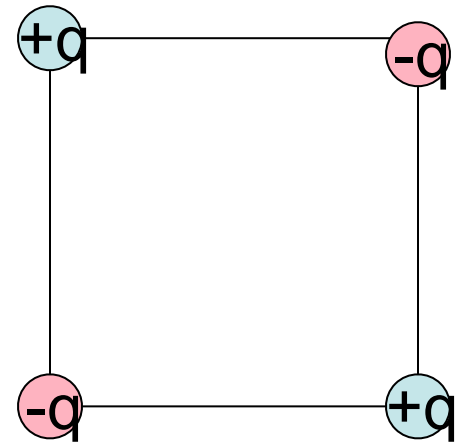
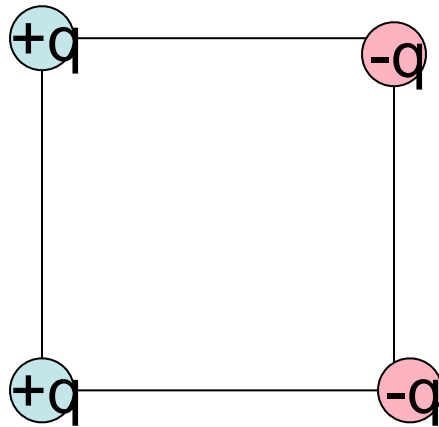
	-4
--	----

+2

$(-4 + \frac{2}{\sqrt{2}})PE_0 = -2.6PE_0$
--

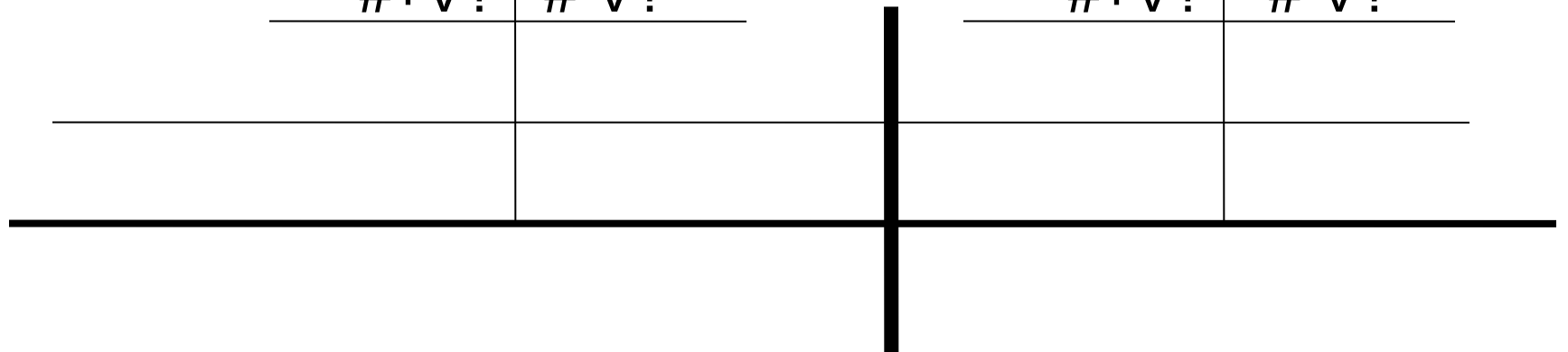


Which of the charge distributions is the most stable?
(has the lowest PE)



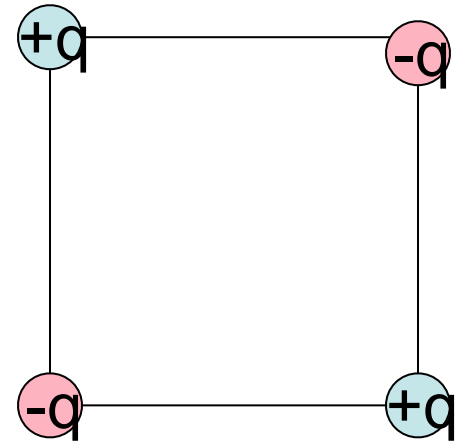
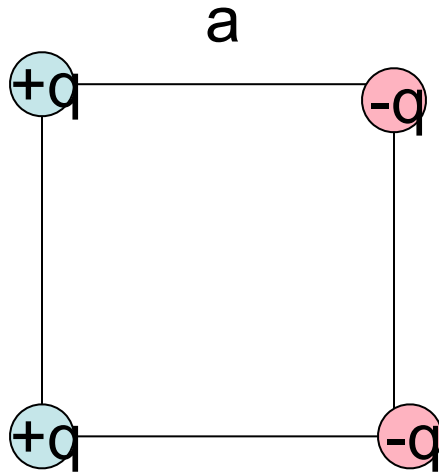
$\# +V?$	$\# -V?$

$\# +V?$	$\# -V?$



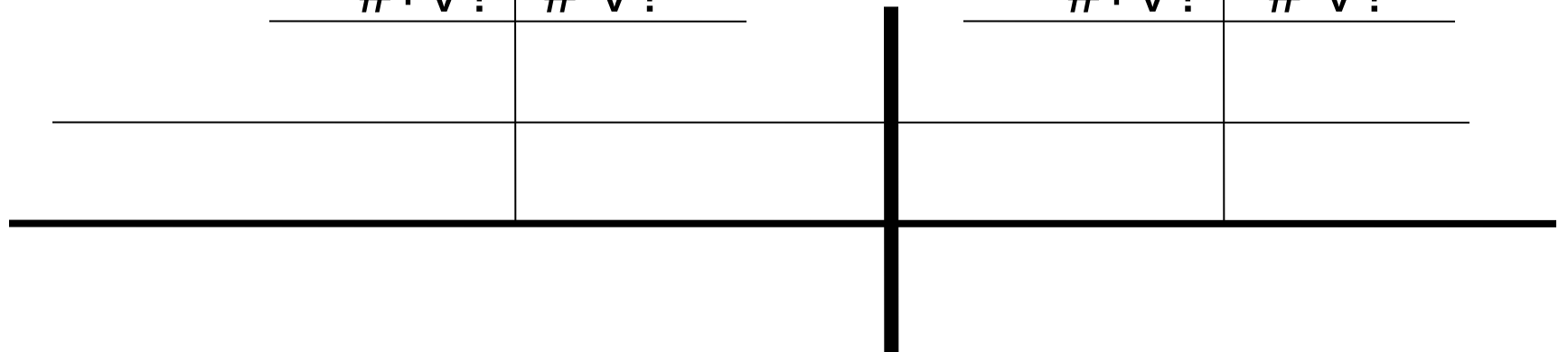
Which of the charge distributions is the most stable?
(has the lowest PE)

$$PE_0 = \frac{k_e q^2}{a}$$



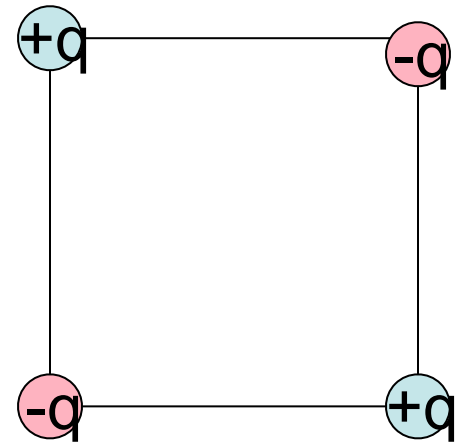
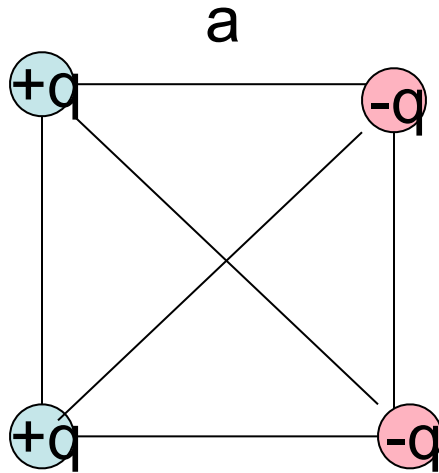
#+V?	#-V?

#+V?	#-V?



Which of the charge distributions is the most stable?
(has the lowest PE)

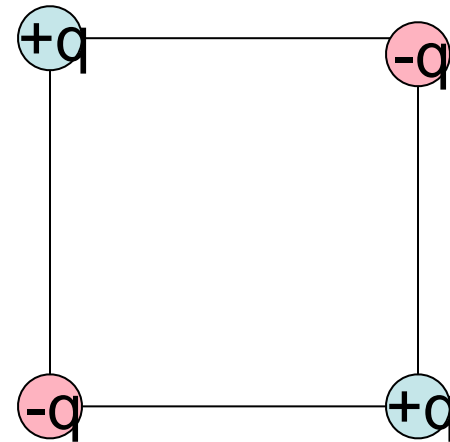
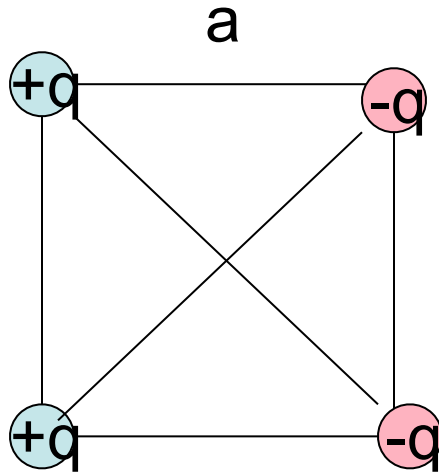
$$PE_0 = \frac{k_e q^2}{a}$$



	#+V?	#-V?		#+V?	#-V?
PE ₀					
PE ₀ /√2					
Total PE					

Which of the charge distributions is the most stable?
(has the lowest PE)

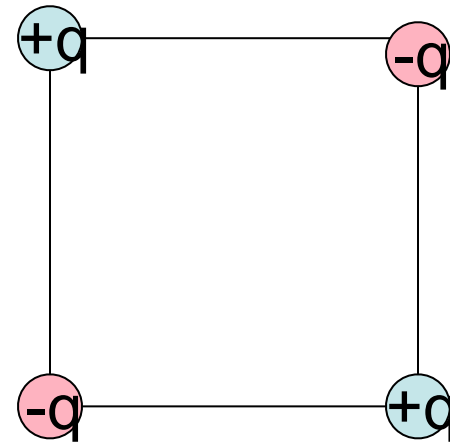
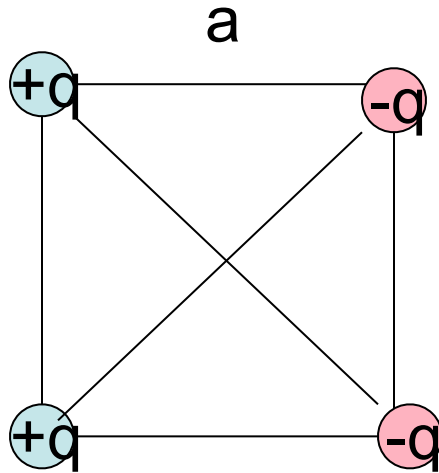
$$PE_0 = \frac{k_e q^2}{a}$$



	#+V?	#-V?		#+V?	#-V?
PE_0	+2	-2			
$PE_0/\sqrt{2}$					
Total PE					

Which of the charge distributions is the most stable?
(has the lowest PE)

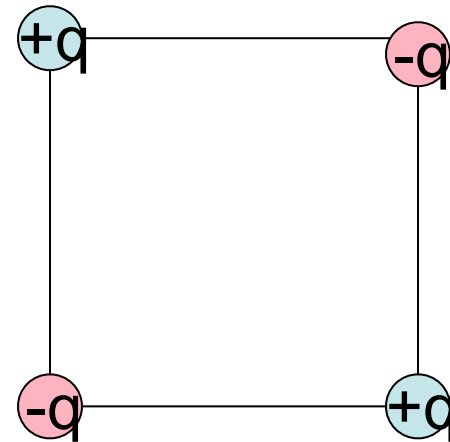
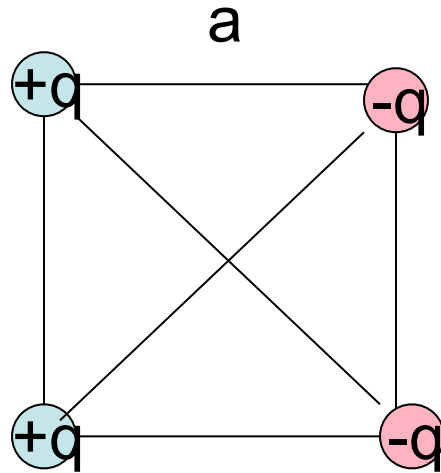
$$PE_0 = \frac{k_e q^2}{a}$$



	#+V?	#-V?		#+V?	#-V?
PE_0	+2	-2			
$PE_0/\sqrt{2}$		-2			
Total PE					

Which of the charge distributions is the most stable?
(has the lowest PE)

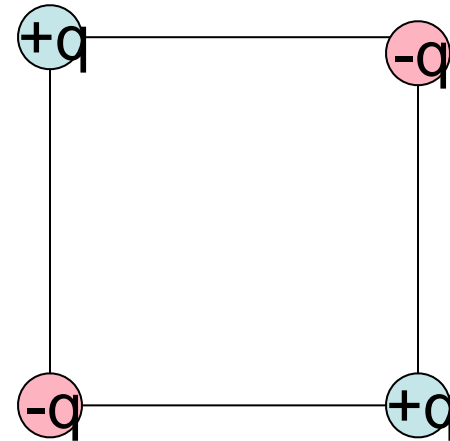
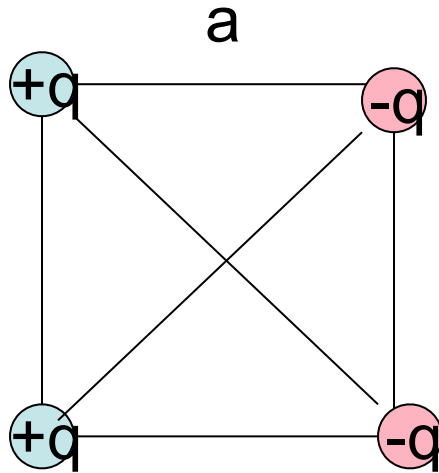
$$PE_0 = \frac{k_e q^2}{a}$$



	#+V?	#-V?		#+V?	#-V?
PE_0	+2	-2			
$PE_0/\sqrt{2}$		-2			
Total PE	$-\frac{2}{\sqrt{2}}PE_0 = -1.4PE_0$				

Which of the charge distributions is the most stable?
(has the lowest PE)

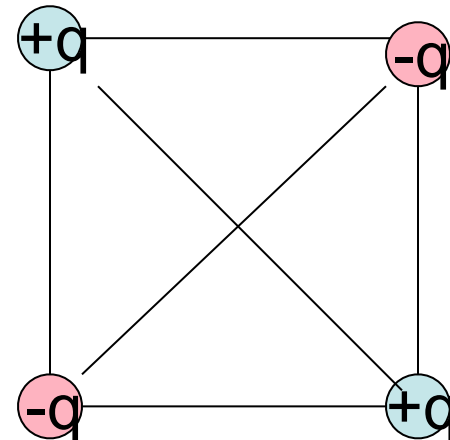
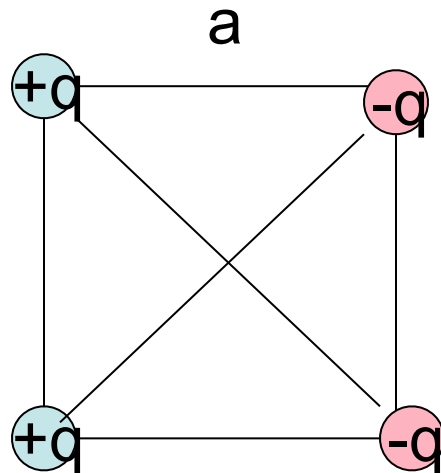
$$PE_0 = \frac{k_e q^2}{a}$$



	#+V?	#-V?	#+V?	#-V?
PE_0	+2	-2		-4
$PE_0/\sqrt{2}$		-2		
Total PE	$-\frac{2}{\sqrt{2}} PE_0 = -1.4 PE_0$			

Which of the charge distributions is the most stable?
(has the lowest PE)

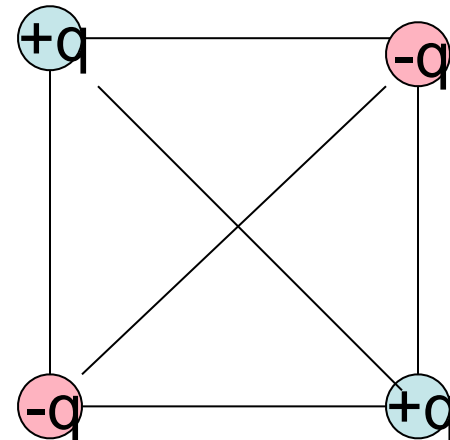
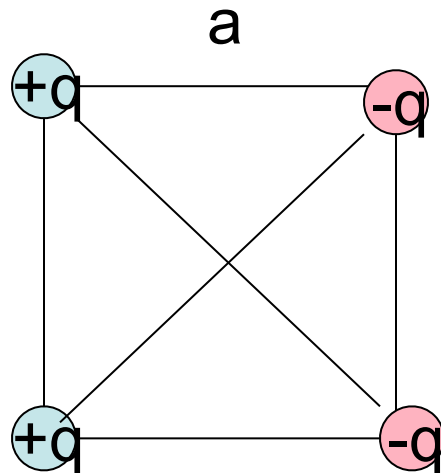
$$PE_0 = \frac{k_e q^2}{a}$$



	#+V?	#-V?		#+V?	#-V?
PE_0	+2	-2			-4
$PE_0/\sqrt{2}$		-2		+2	
Total PE	$-\frac{2}{\sqrt{2}}PE_0 = -1.4PE_0$				

Which of the charge distributions is the most stable?
(has the lowest PE)

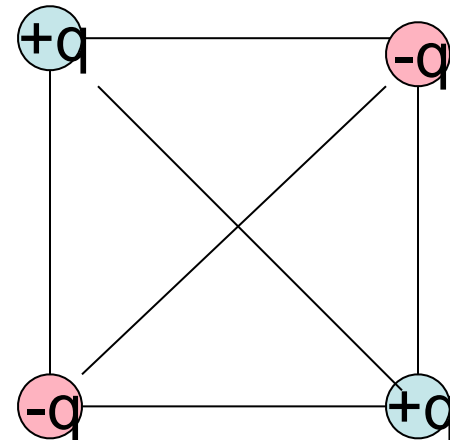
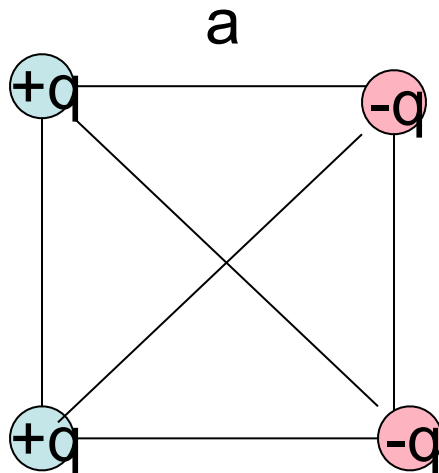
$$PE_0 = \frac{k_e q^2}{a}$$



	#+V?	#-V?	#+V?	#-V?
PE_0	+2	-2		-4
$PE_0/\sqrt{2}$		-2	+2	
Total PE	$-\frac{2}{\sqrt{2}}PE_0 = -1.4PE_0$		$(-4 + \frac{2}{\sqrt{2}})PE_0 = -2.6PE_0$	

Which of the charge distributions is the most stable?
(has the lowest PE)

$$PE_0 = \frac{k_e q^2}{a}$$



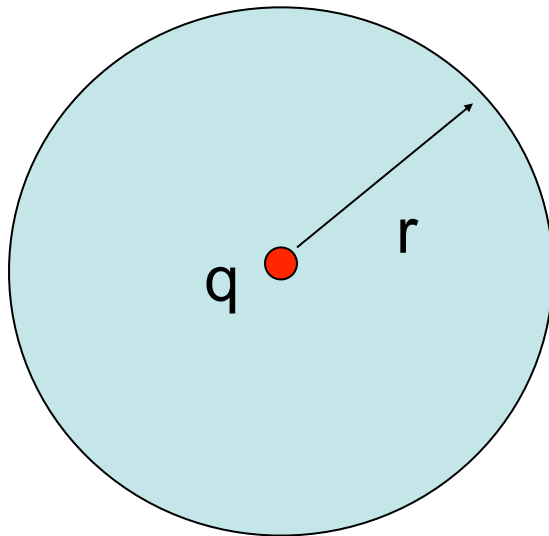
	#+V?	#-V?	#+V?	#-V?
PE_0	+2	-2		-4
$PE_0/\sqrt{2}$		-2	+2	
Total PE	$-\frac{2}{\sqrt{2}}PE_0 = -1.4PE_0$		$(-4 + \frac{2}{\sqrt{2}})PE_0 = -2.6PE_0$ more stable	

16.2 Equipotentials

Equipotential surfaces

Equipotential Surface - positions in space at which the electrical potentials are equal

Example 1- A sphere centered around a point charge



Every point on the surface of the sphere of radius r has the same potential

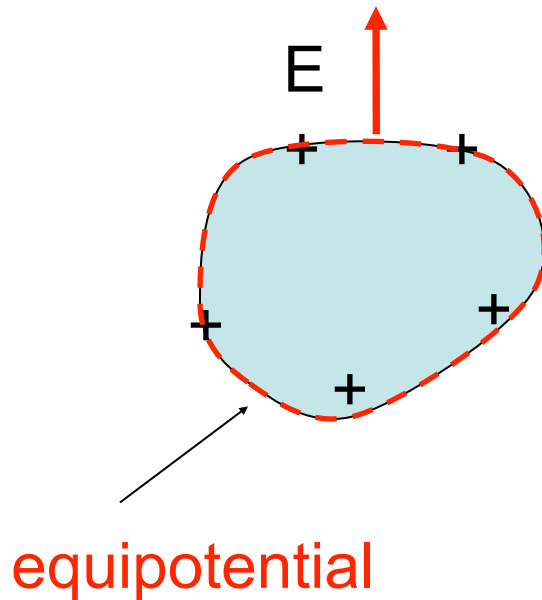
$$V = \frac{k_e q}{r}$$

The surface of the sphere is an **equipotential surface**

Equipotential surface-

Example 2: a charged conductor

The surface of a conductor is an **equipotential surface**.



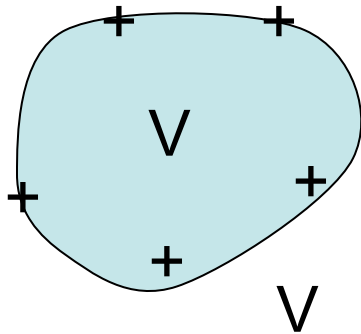
E field is perpendicular to the surface.

Component of $E = 0$ parallel to the surface

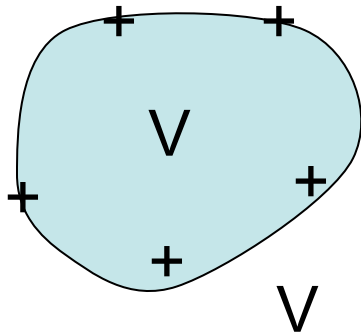
$$\Delta V = Ed = 0$$

Thus, No change in potential along the surface

The interior of the conductor is an **equipotential** and at the same potential as the surface.



The interior of the conductor is an **equipotential** and at the same potential as the surface.



$E=0$ in the conductor

Thus, the potential doesn't change from the surface potential

PHYSICS 1B – Fall 2009



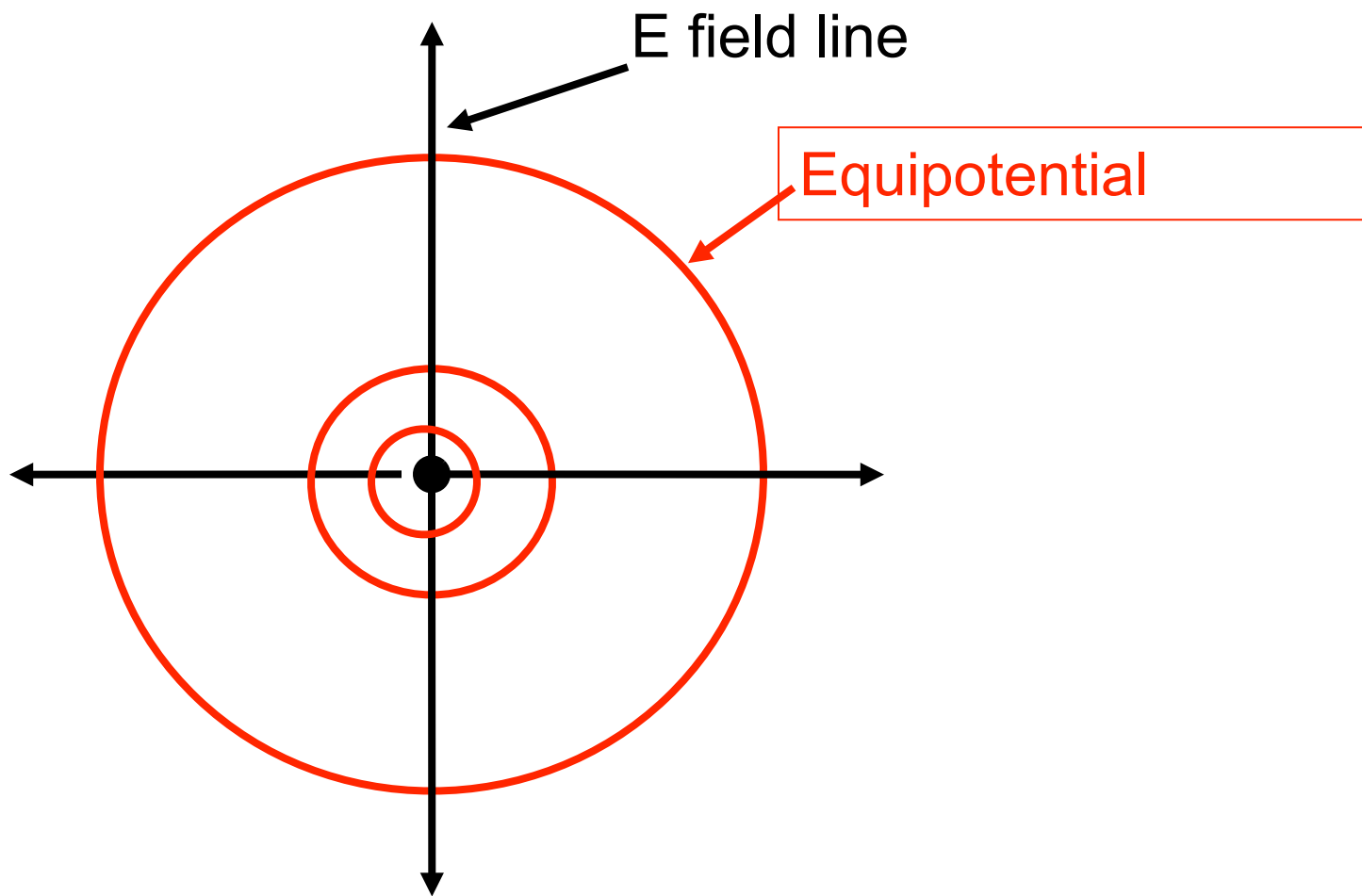
Electricity & Magnetism



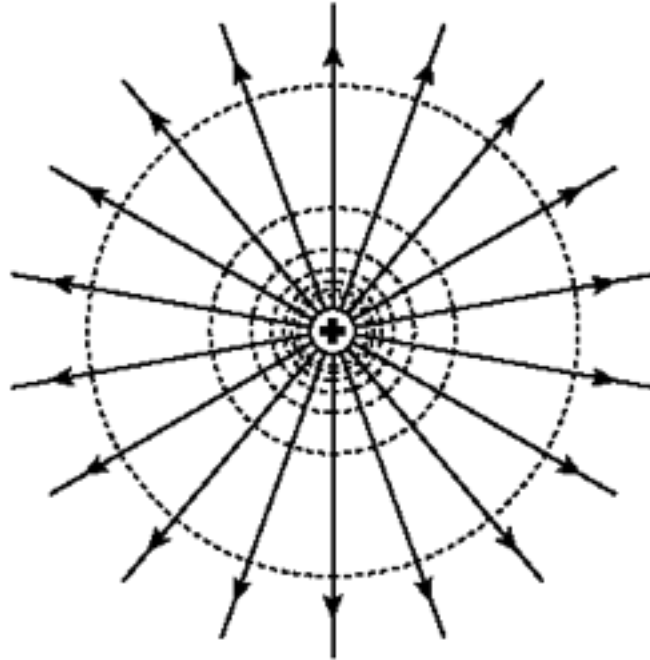
Professor Brian Keating
SERF Building. Room 333

Friday October 16, 2009

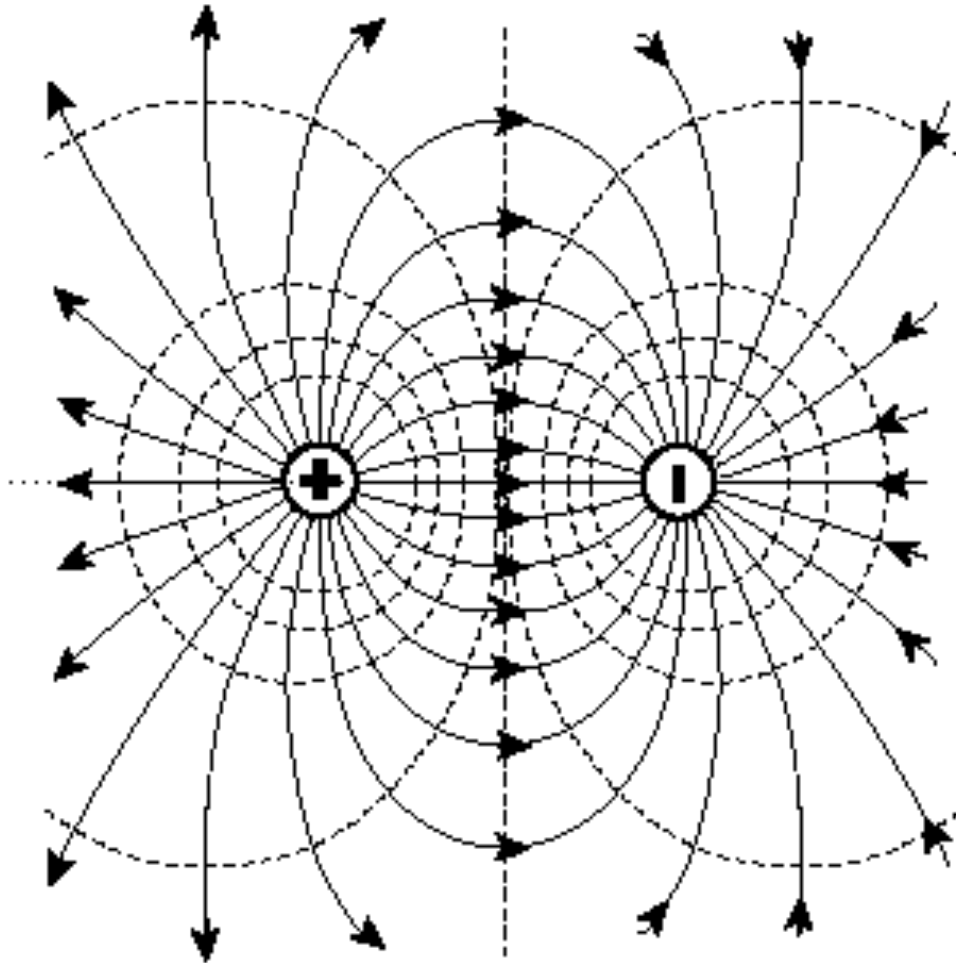
The **equipotential surfaces** are perpendicular to E field lines.



Equipotential lines: point charge



Equipotential lines: dipole



Which line type/style represents the electric field?

A. solid

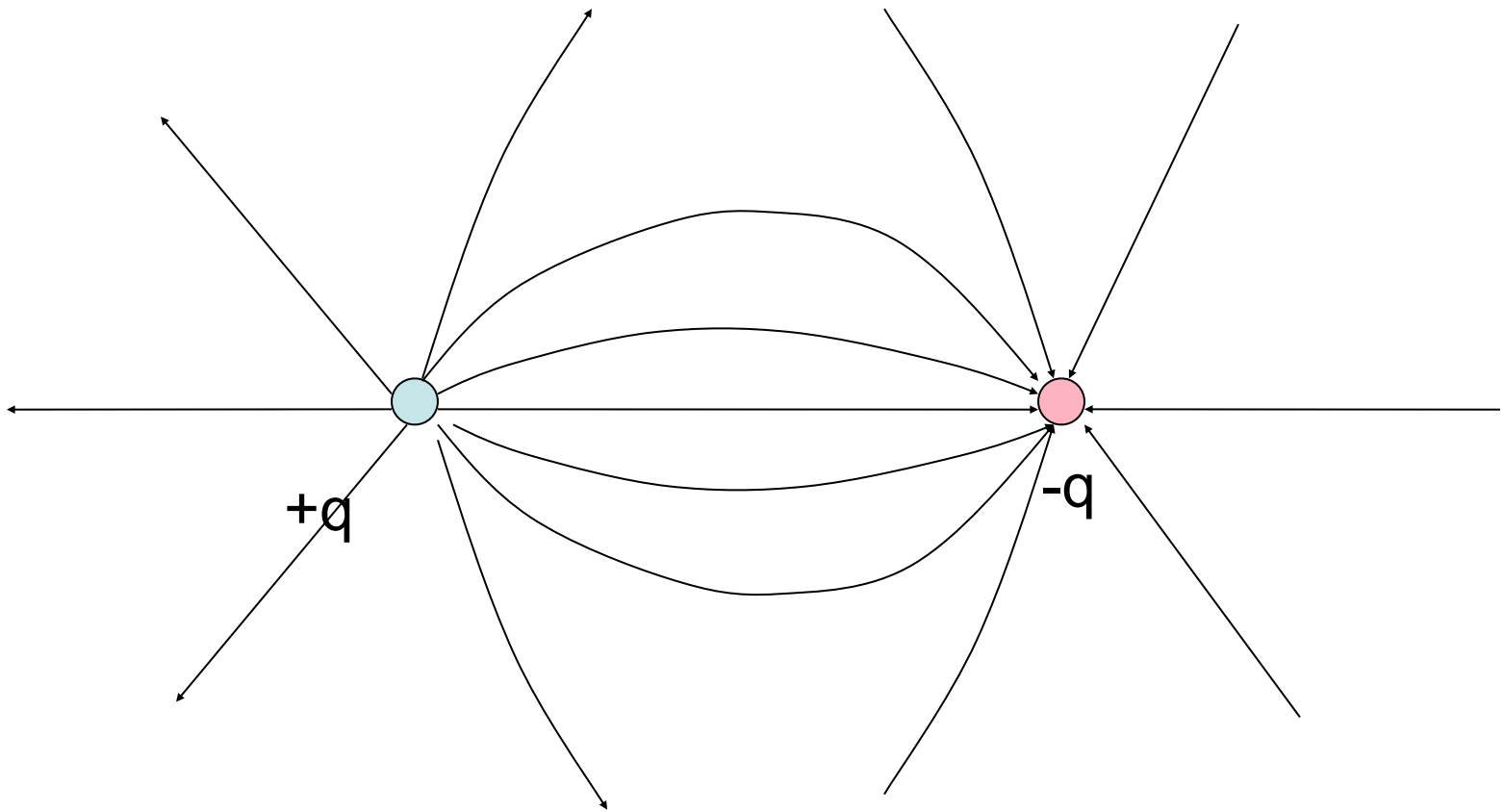
B. dashed



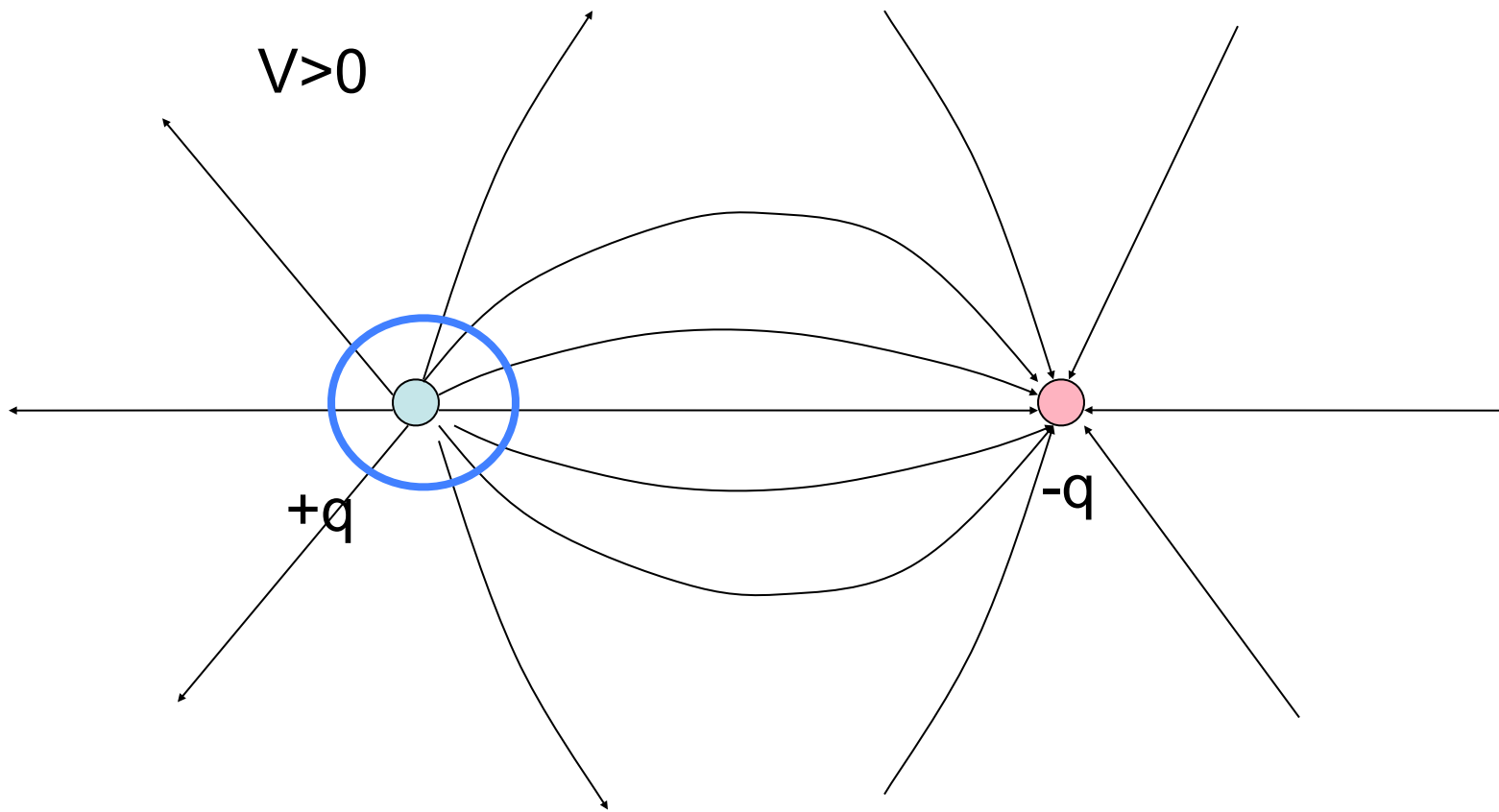
Draw a sketch of the equipotential surfaces for a electric dipole ($+q$, $-q$) in a plane through both charges



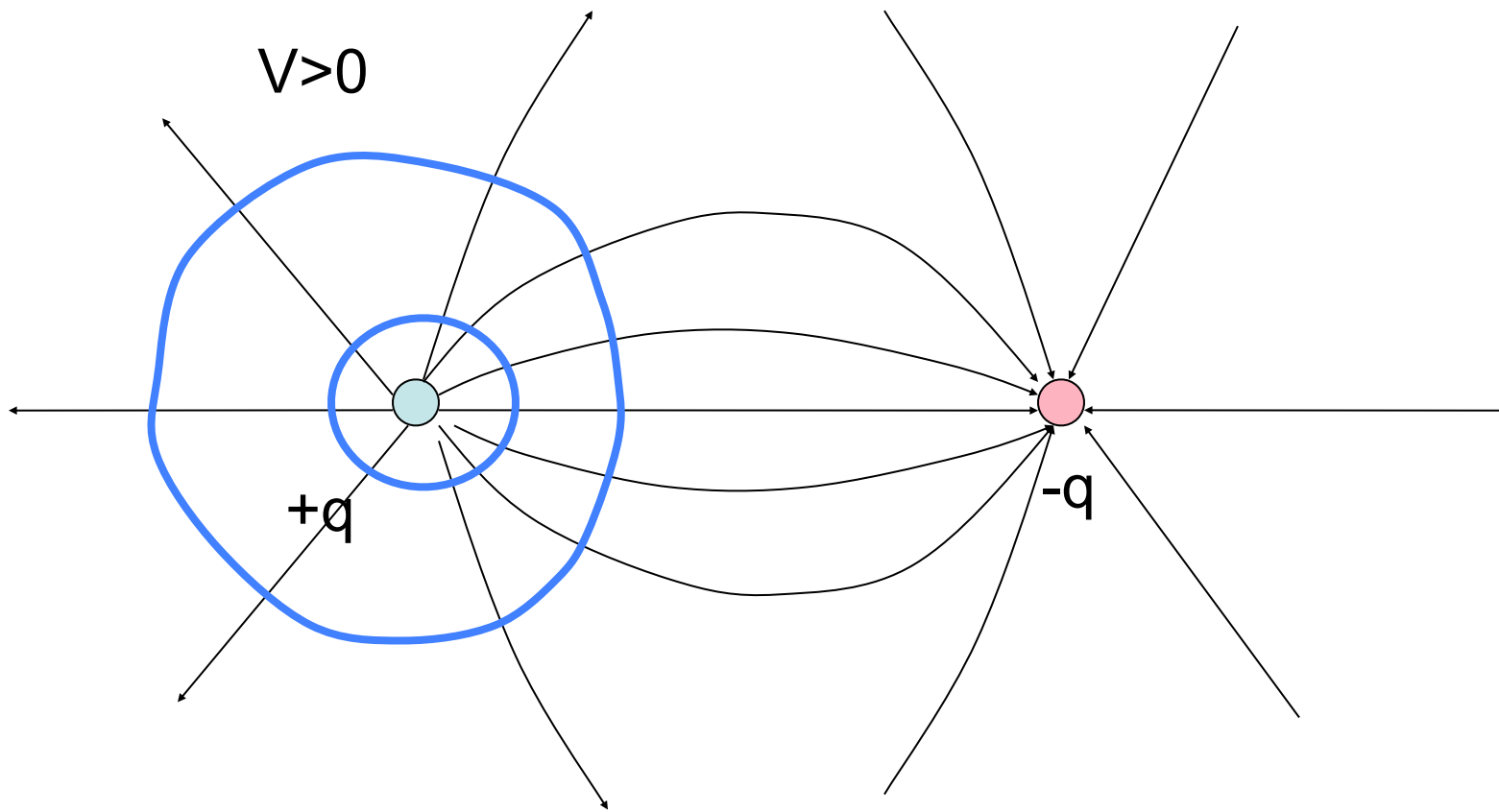
Draw a sketch of the equipotential surfaces for a electric dipole ($+q$, $-q$) in a plane through both charges



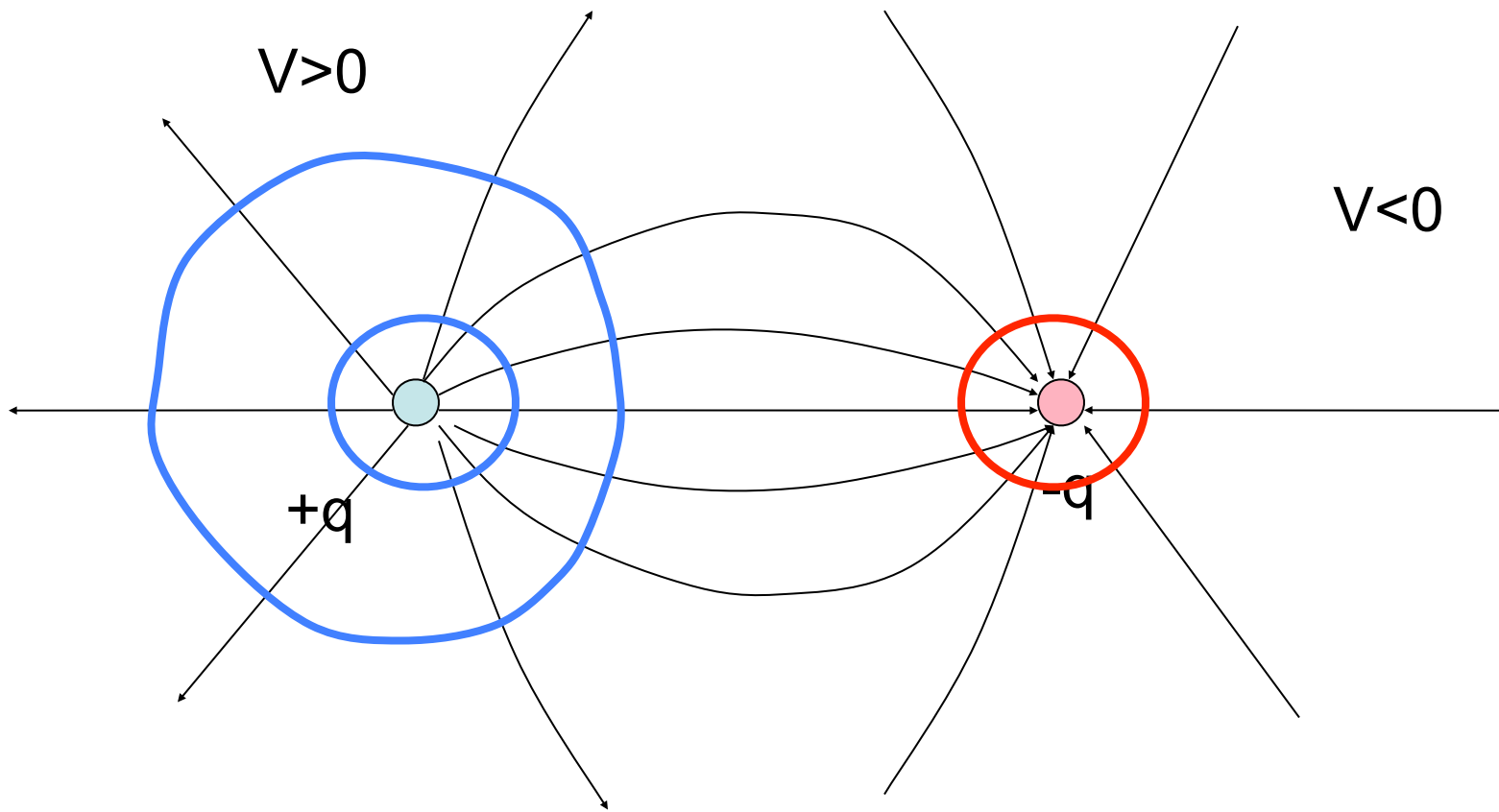
Draw a sketch of the equipotential surfaces for a electric dipole ($+q$, $-q$) in a plane through both charges



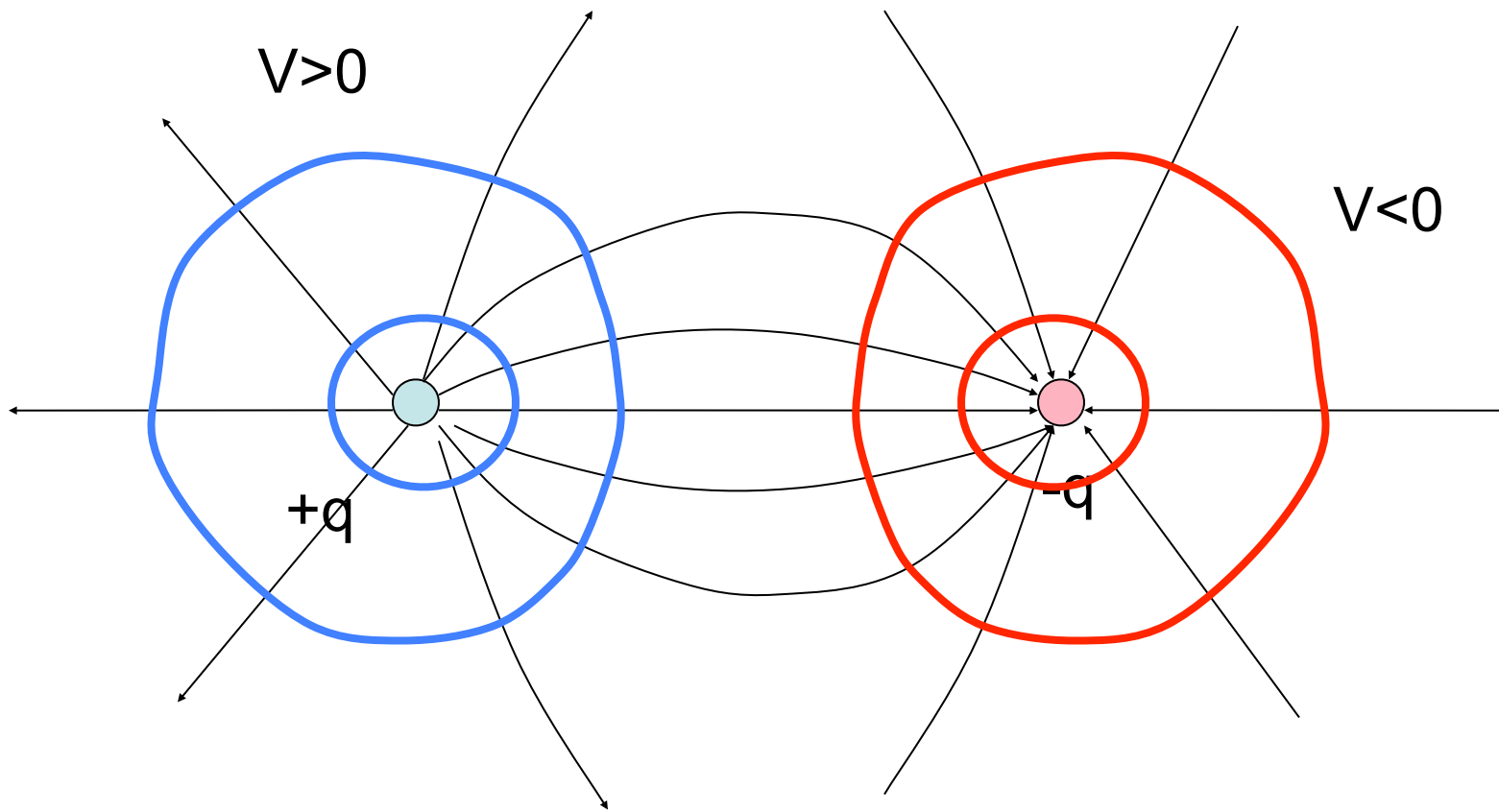
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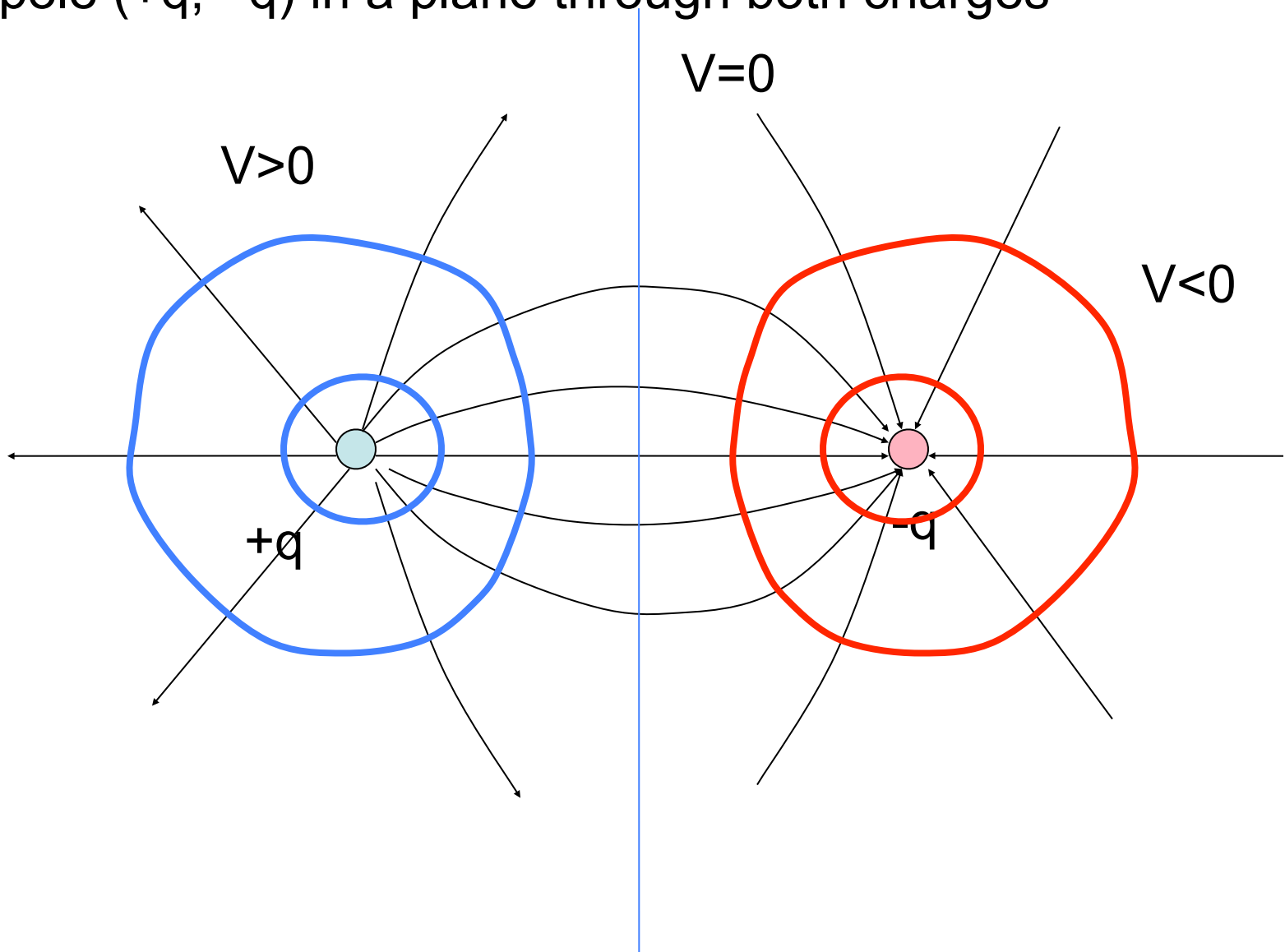
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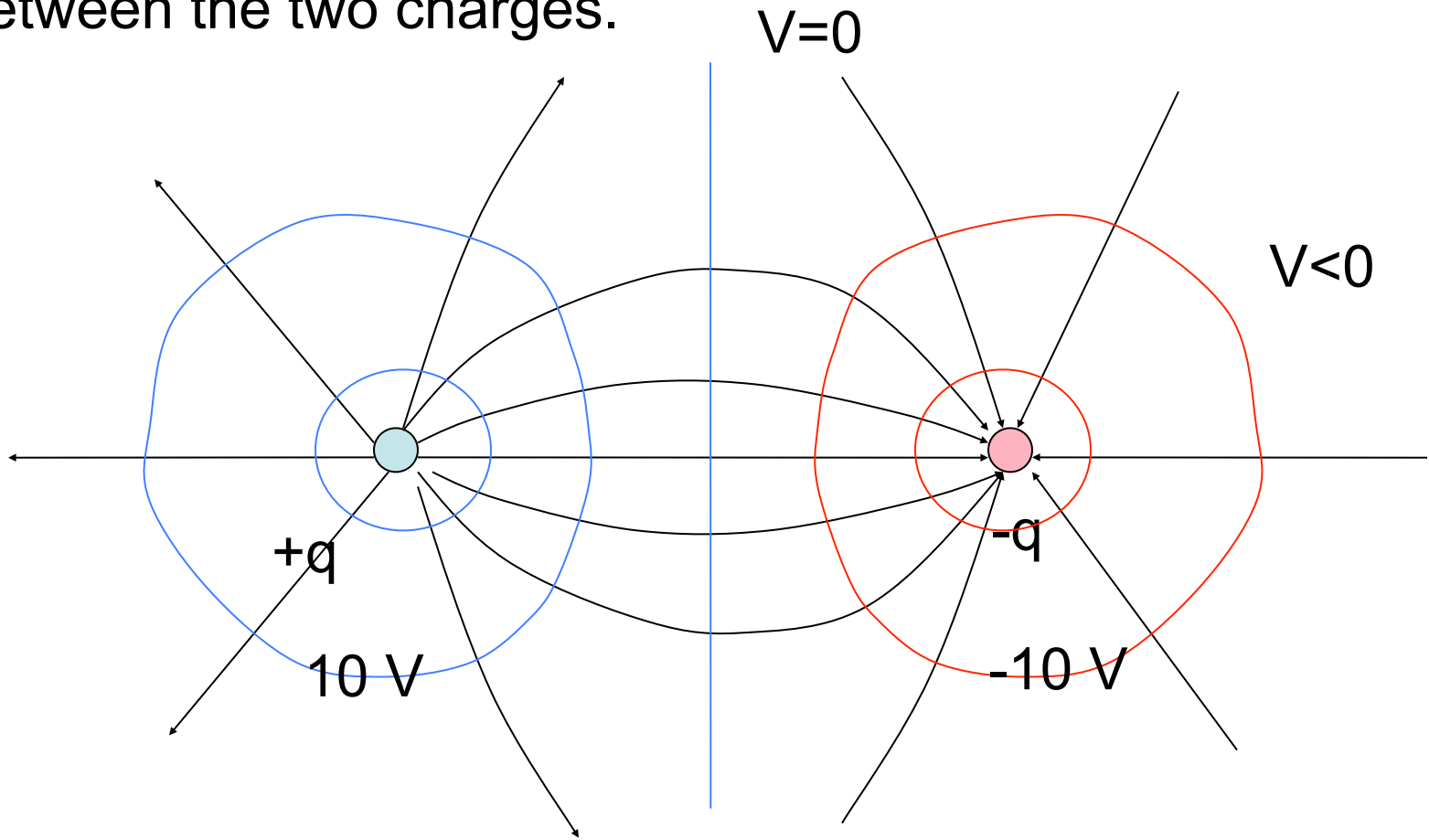
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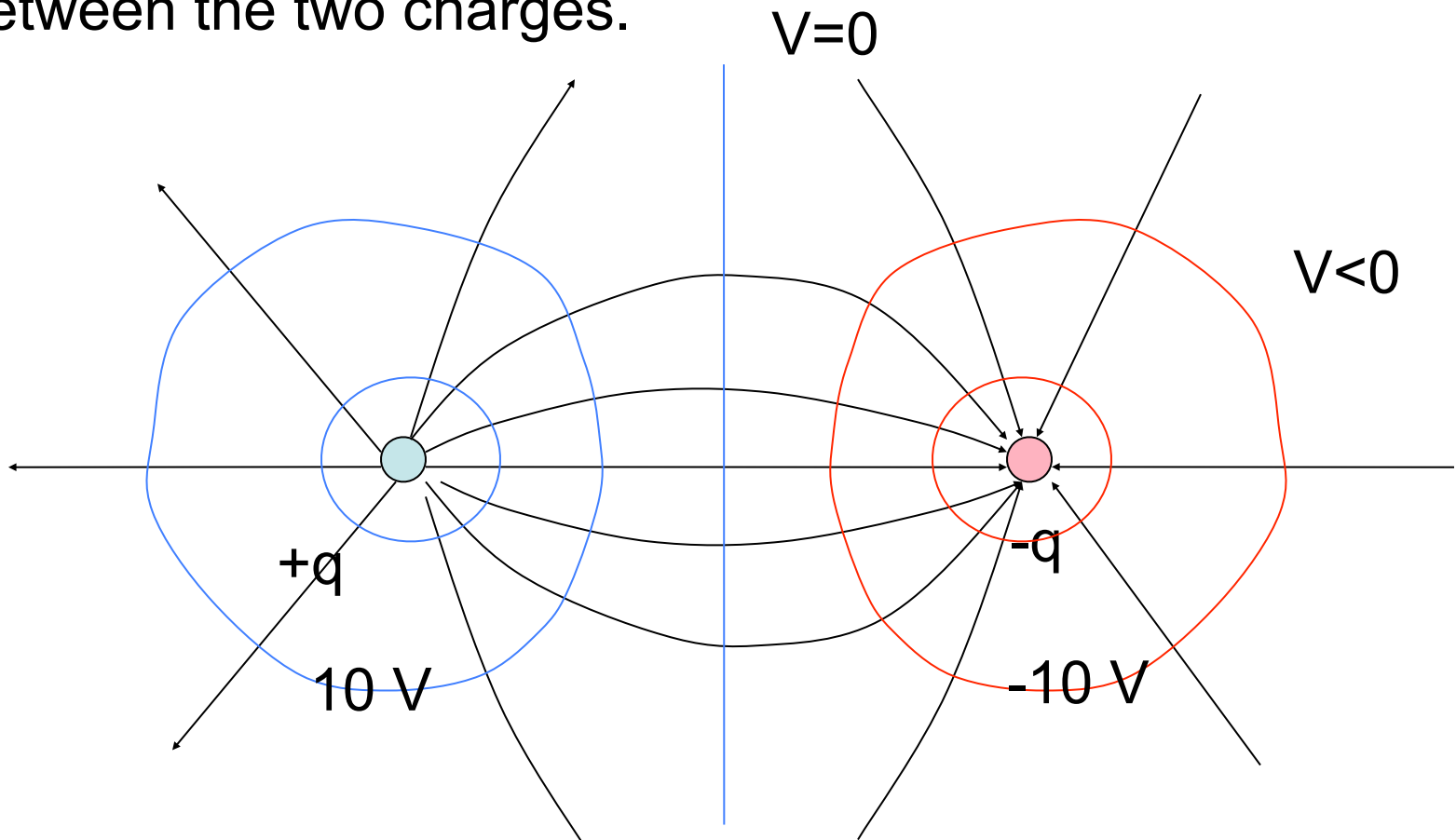
Draw a sketch of the equipotential surfaces for a electric dipole ($+q$, $-q$) in a plane through both charges



Suppose the two charges are 10 cm apart and the equipotential surfaces are as labeled estimate the E field between the two charges.



Suppose the two charges are 10 cm apart and the equipotential surfaces are as labeled estimate the E field between the two charges.



$$E = \frac{\Delta V}{d} \approx \frac{20}{0.05} \approx 400\text{ V/m}$$

Rutherford Scattering experiment

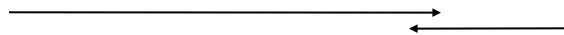
Determination of the size of the nucleus

α particle He nucleus

$$q = +2e$$

$$m = 6.64 \times 10^{-27} \text{ kg}$$

$$v = 2.0 \times 10^7 \text{ m/s}$$



recoil



gold
foil

gold nuclei
 $Q = +79e$

Rutherford Scattering experiment

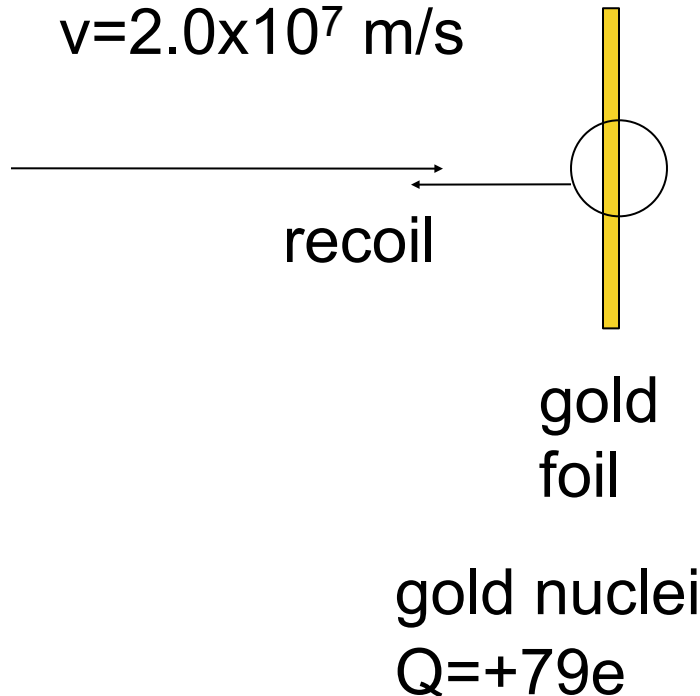
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Rutherford Scattering experiment

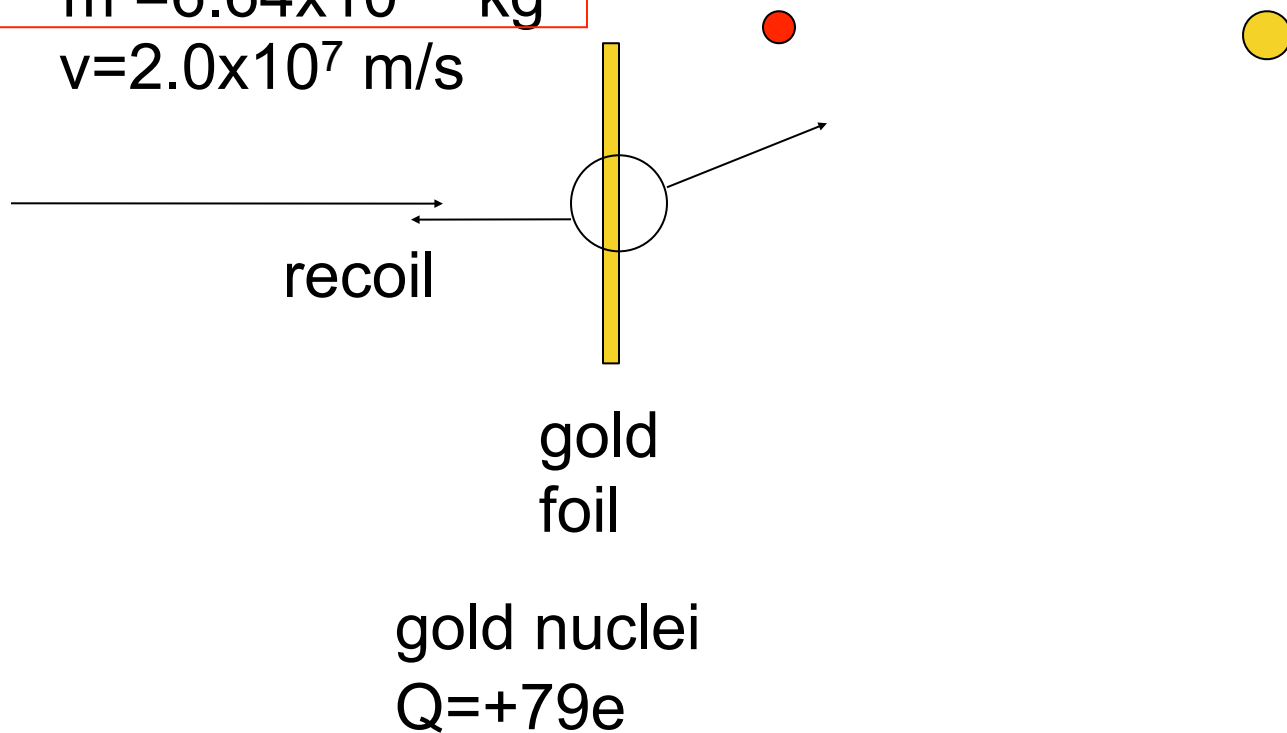
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Rutherford Scattering experiment

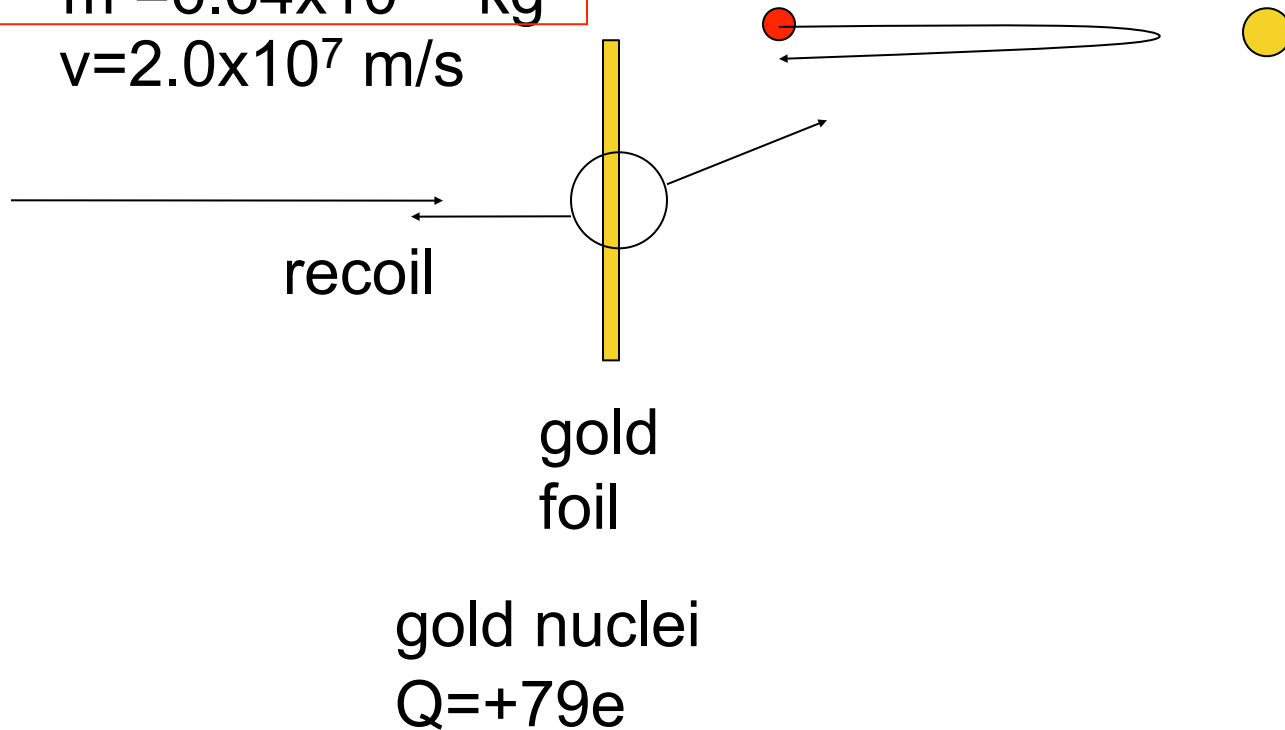
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Rutherford Scattering experiment

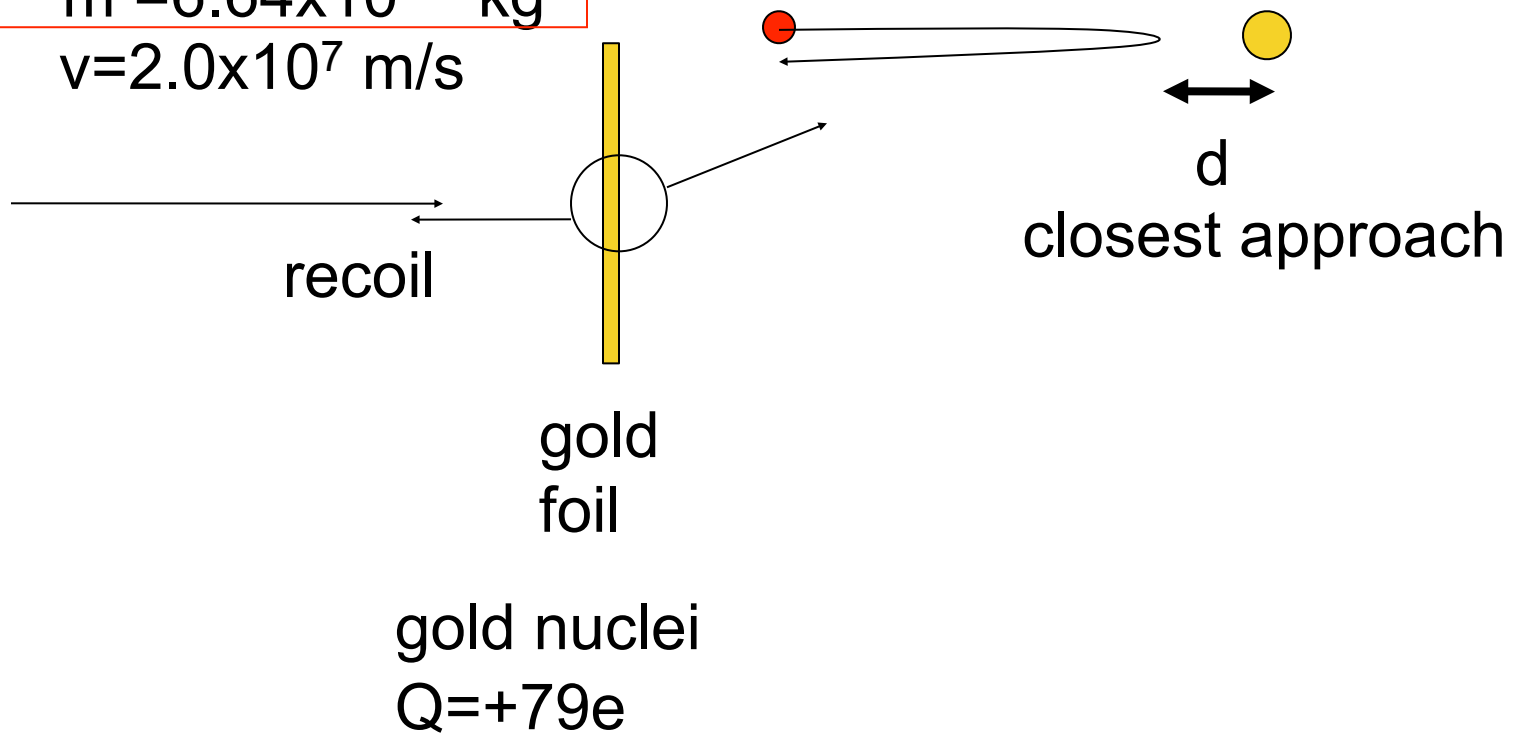
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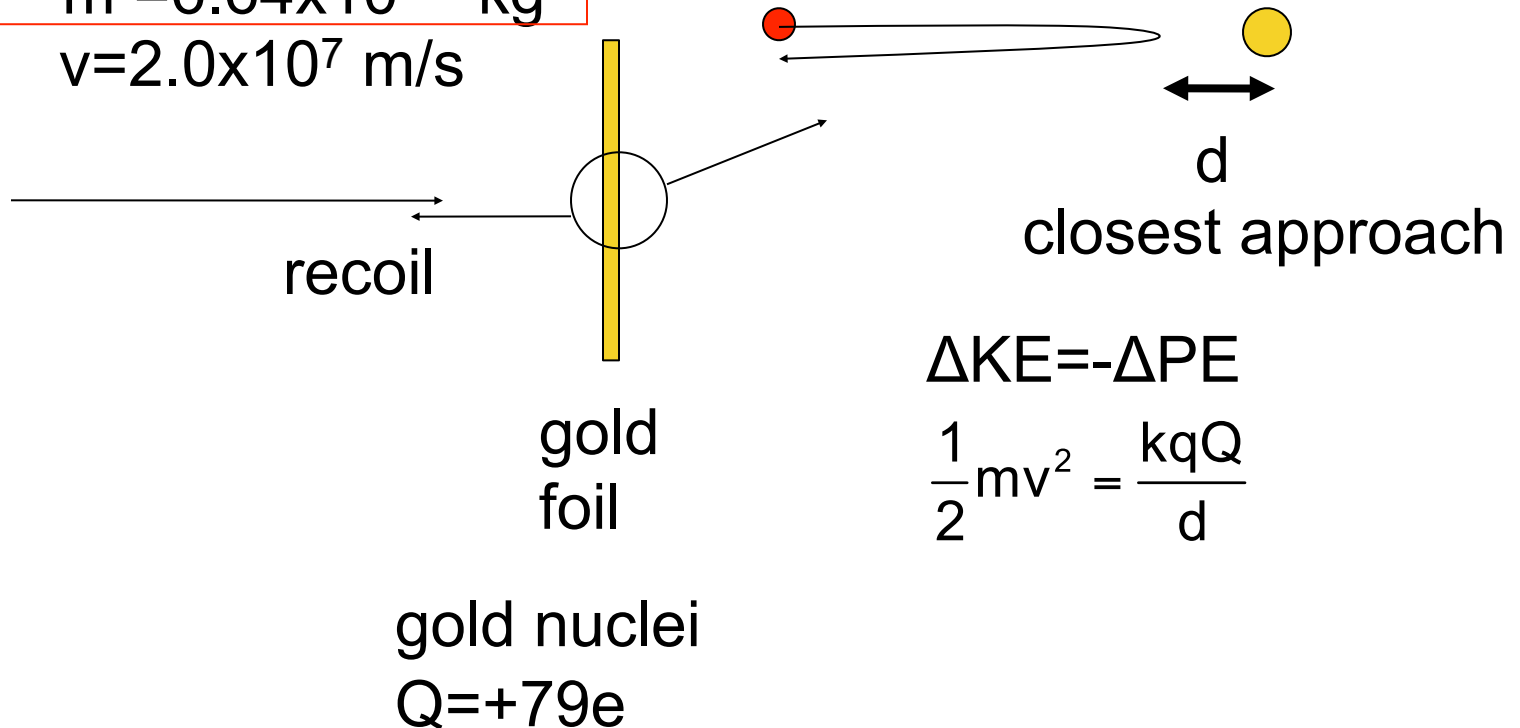


Rutherford Scattering experiment

Determination of the size of the nucleus

α particle He nucleus

$$q = +2e$$
$$m = 6.64 \times 10^{-27} \text{ kg}$$
$$v = 2.0 \times 10^7 \text{ m/s}$$



$$\Delta KE = -\Delta PE$$

$$\frac{1}{2}mv^2 = \frac{kqQ}{d}$$

gold nuclei
 $Q = +79e$

Rutherford Scattering experiment

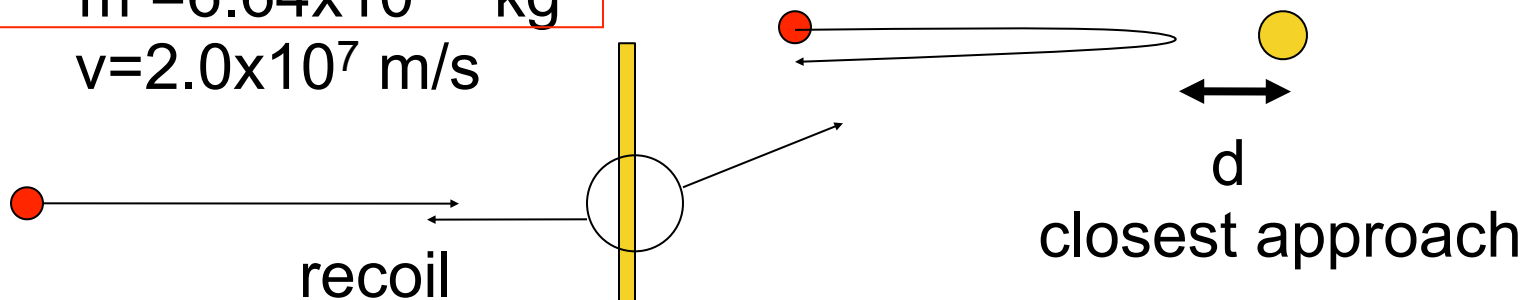
Determination of the size of the nucleus

α particle He nucleus

$$q = +2e$$

$$m = 6.64 \times 10^{-27} \text{ kg}$$

$$v = 2.0 \times 10^7 \text{ m/s}$$



gold foil

gold nuclei
 $Q = +79e$

$$\Delta KE = -\Delta PE$$

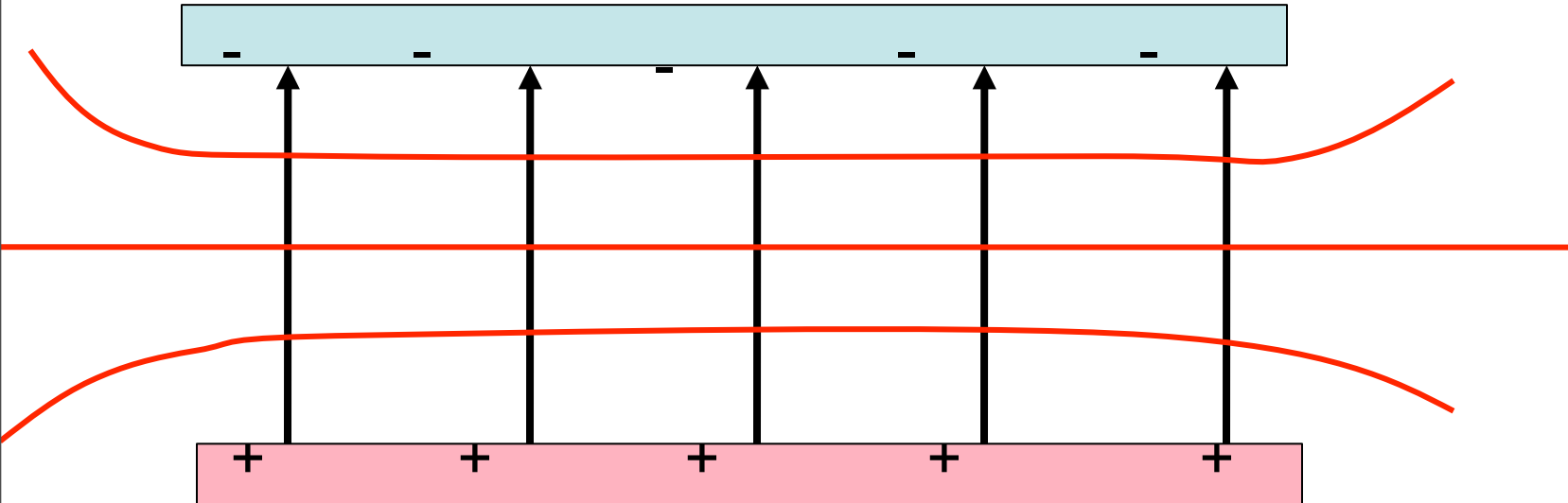
$$\frac{1}{2}mv^2 = \frac{kqQ}{d}$$

$$d = \frac{2k_e qQ}{mv^2} = \frac{2(9 \times 10^9)(2)(79)(1.6 \times 10^{-19})^2}{6.64 \times 10^{-27} (2 \times 10^7)^2}$$

$$d = 2.7 \times 10^{-14} \text{ m}$$

nuclear size $< d$, much smaller than size of an atom $\sim 0.3 \times 10^{-9} \text{ m}$

Parallel plate capacitor

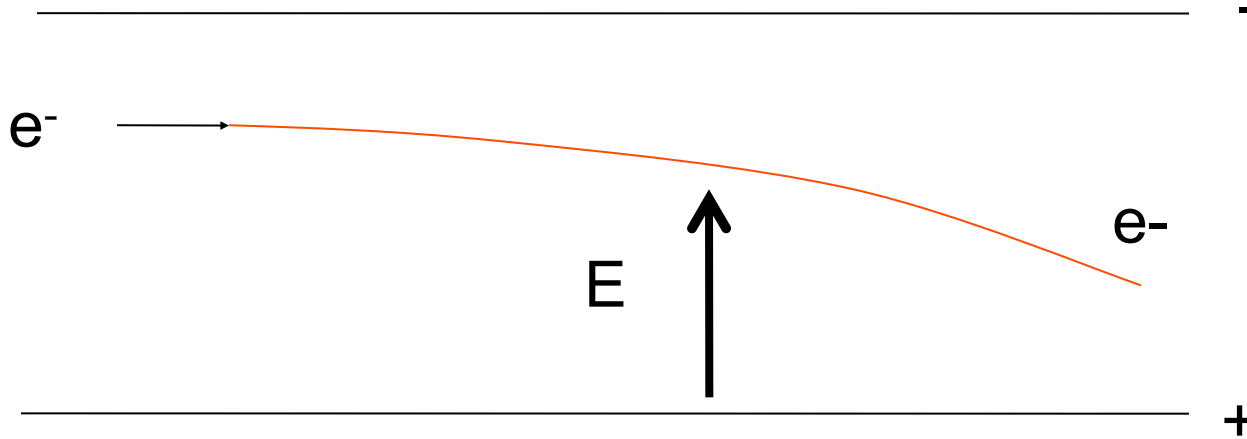


FIELD LINES IN BLACK (VECTORS)

POTENTIAL CONTOURS IN RED

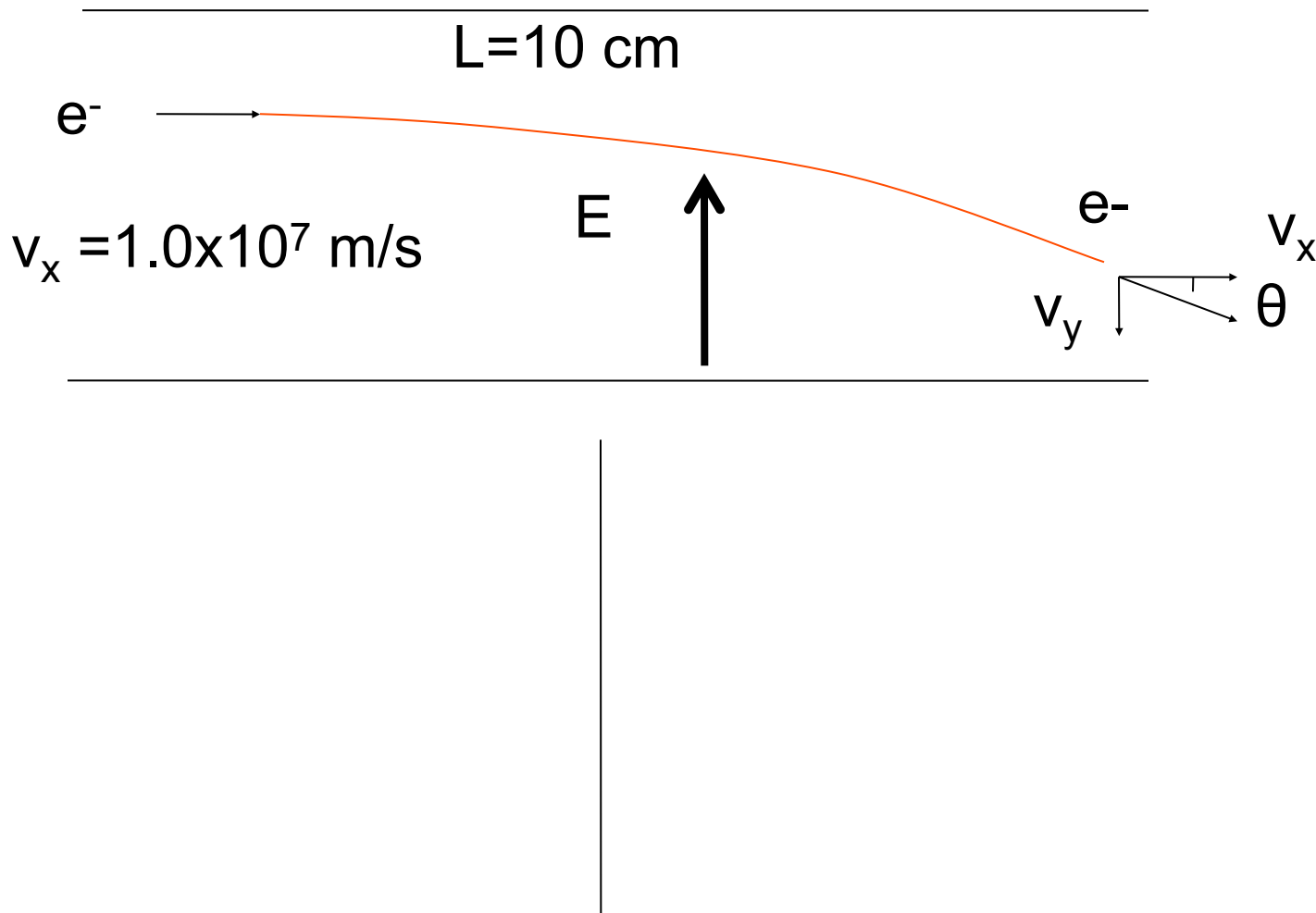
(NO ARROWS, BECAUSE NOT A VECTOR)

Deflection of an electron beam in an electric field

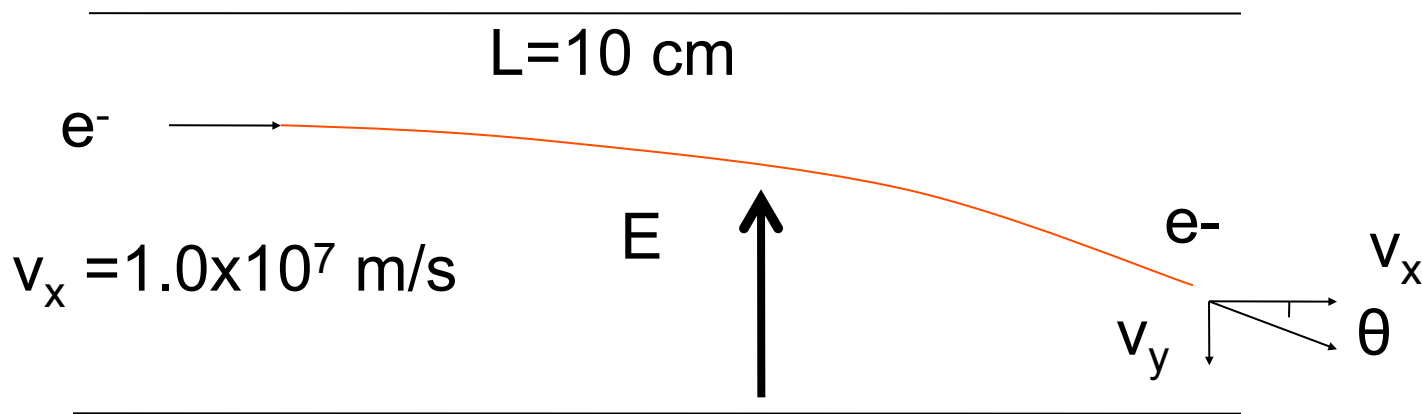


Calculation – velocity, acceleration – Next Slide:
calculate the angle the electron exits at...

An electron beam passes through two parallel plates of a length 10 cm having an electric field of E . The initial velocity of the electron is 1.0×10^7 m/s. Find the angle through which the beam is deflected.

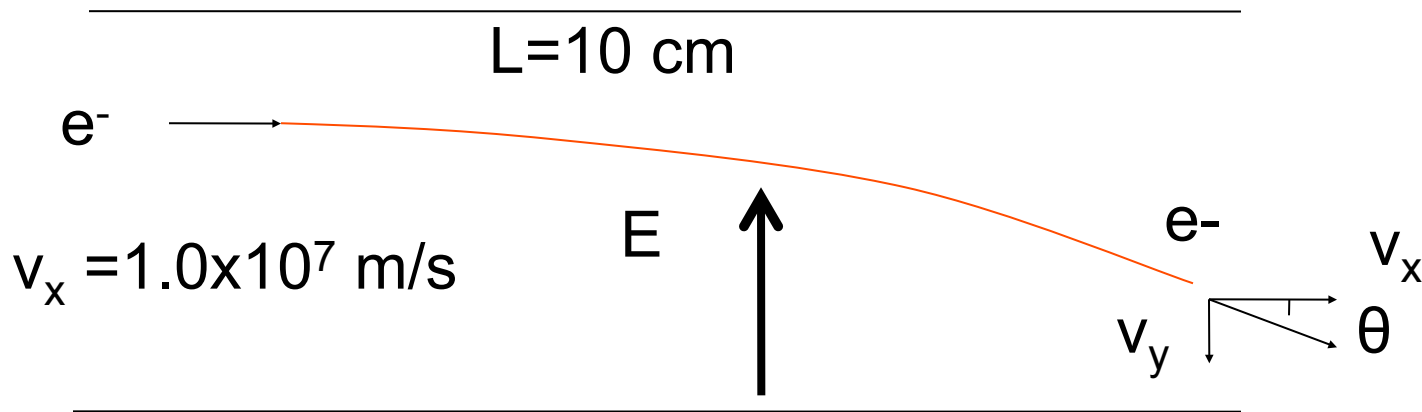


An electron beam passes through two parallel plates of a length 10 cm having an electric field of E . The initial velocity of the electron is 1.0×10^7 m/s. Find the angle through which the beam is deflected.



$$F = qE = ma$$

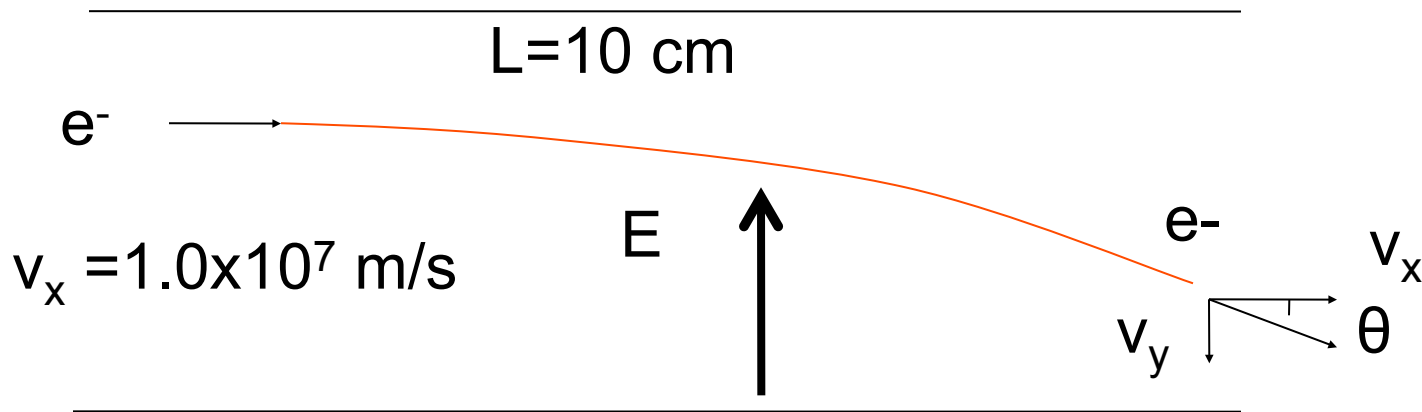
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$$F = qE = ma$$

$$v_y = at = \frac{F}{m}t = \frac{qE}{m}t$$

An electron beam passes through two parallel plates of a length 10 cm having an electric field of E . The initial velocity of the electron is 1.0×10^7 m/s. Find the angle through which the beam is deflected.



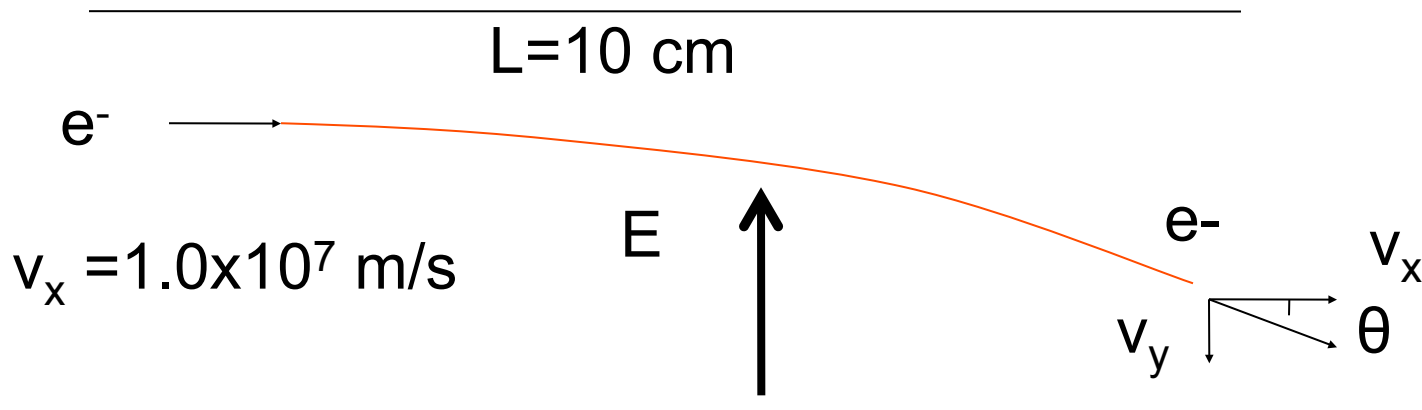
$$F = qE = ma$$

$$v_y = at = \frac{F}{m}t = \frac{qE}{m}t$$

$$t = \frac{L}{v_x}$$

$$v_y = \frac{qE}{m} \left(\frac{L}{v_x} \right)$$

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$$F = qE = ma$$

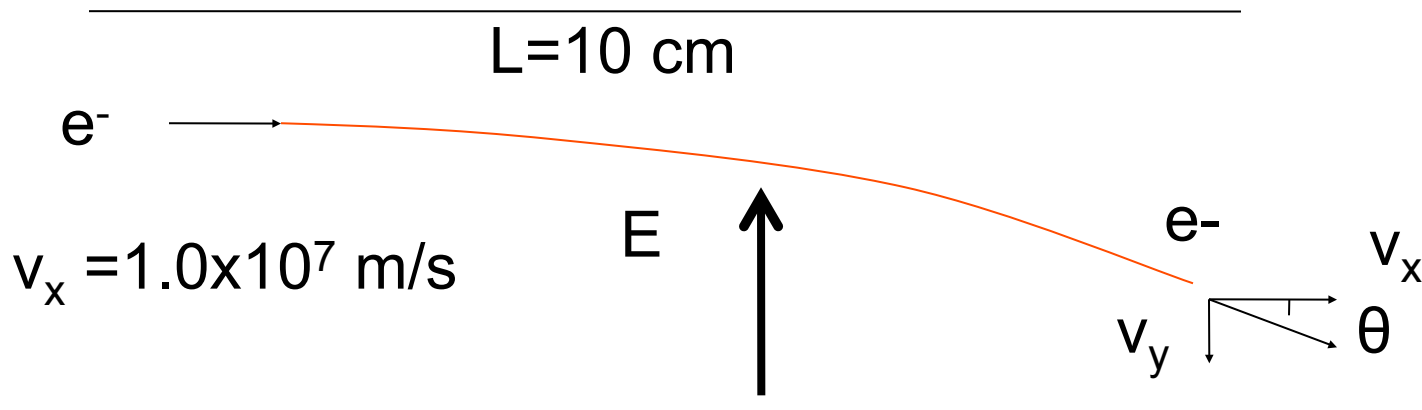
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$$t = \frac{L}{v_x}$$

$$v_y = \frac{qE}{m} \left(\frac{L}{v_x} \right)$$

$$\tan\theta = \frac{v_y}{v_x} = \frac{qEL}{v_x^2 m}$$

An electron beam passes through two parallel plates of a length 10 cm having an electric field of E . The initial velocity of the electron is 1.0×10^7 m/s. Find the angle through which the beam is deflected.



$$F = qE = ma$$

$$v_y = at = \frac{F}{m}t = \frac{qE}{m}t$$

$$t = \frac{L}{v_x}$$

$$v_y = \frac{qE}{m} \left(\frac{L}{v_x} \right)$$

$$\tan\theta = \frac{v_y}{v_x} = \frac{qEL}{v_x^2 m}$$

$$\theta = \tan^{-1} \left(\frac{qEL}{v_x^2 m} \right) = \tan^{-1} \left(\frac{1.6 \times 10^{-19} (1000) (0.1)}{(10^7)^2 (9 \times 10^{-31})} \right) = 10^\circ$$

Capacitance

Capacitor- a device for storing charge and energy, can be discharged rapidly to release energy.

Applications

- Camera flash
- automobile starting system
- capacitors in electronic devices
- computer memories (store information)
- Laser flash lamp

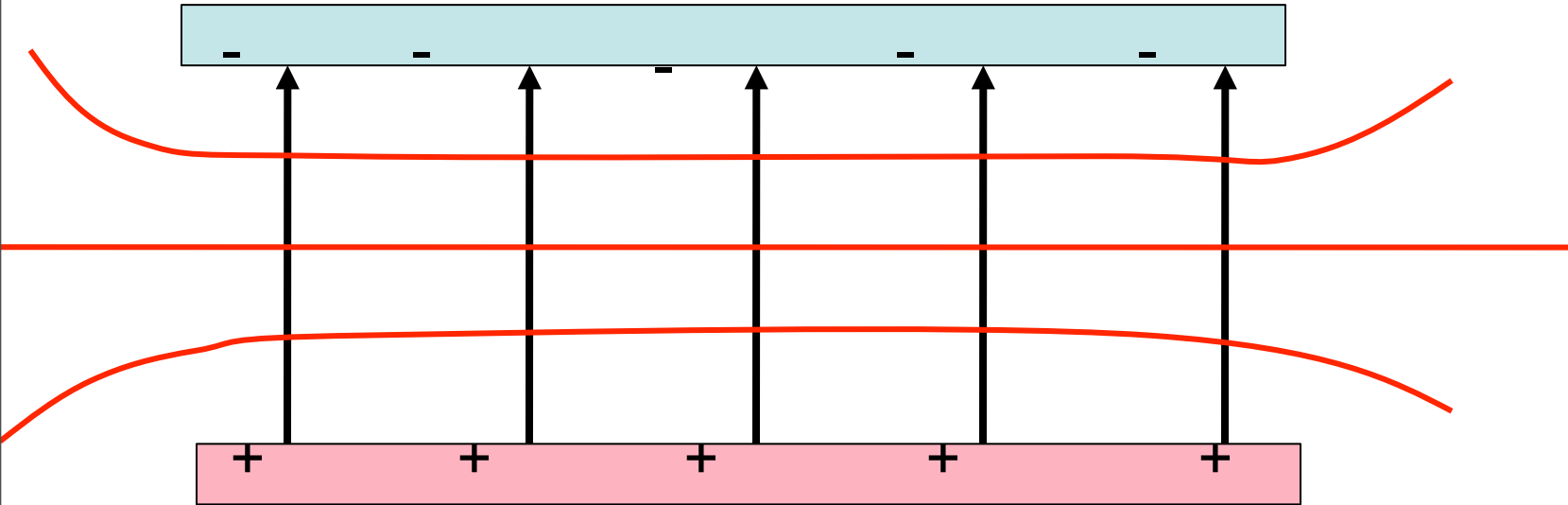


laser fusion

Energy stored in a capacitor 2×10^6 J released in $1-2 \times 10^{-6}$ s.

High Power $\sim 10^{12}$ W

Parallel plate capacitor



FIELD LINES IN BLACK (VECTORS)

POTENTIAL CONTOURS IN RED

(NO ARROWS, BECAUSE NOT A VECTOR)

PHYSICS 1B – Fall 2009

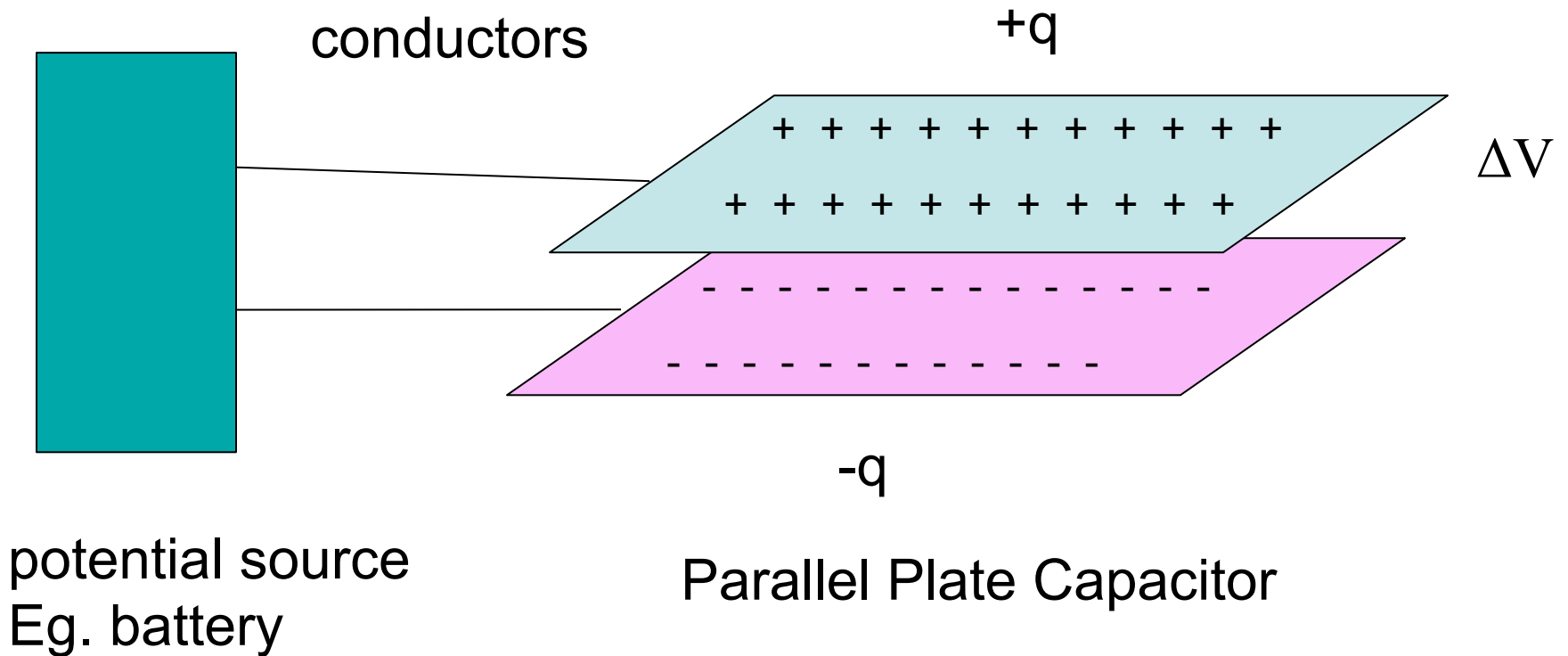


Electricity & Magnetism



Professor Brian Keating
SERF Building. Room 333

October 19, 2009

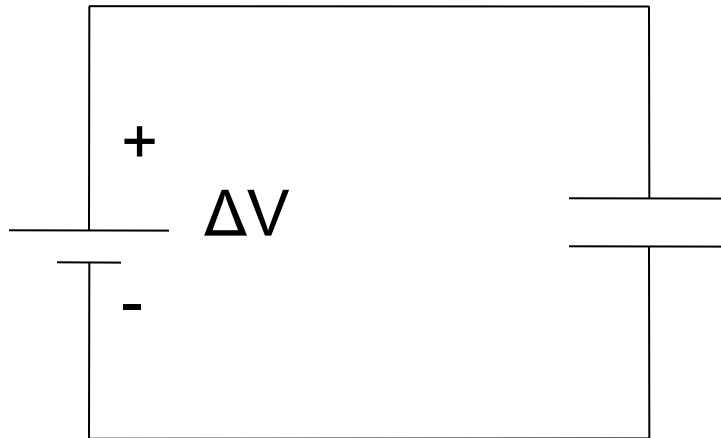


Work is done to separate charges
Capacitor Stores Electrical Energy

Circuit Diagram

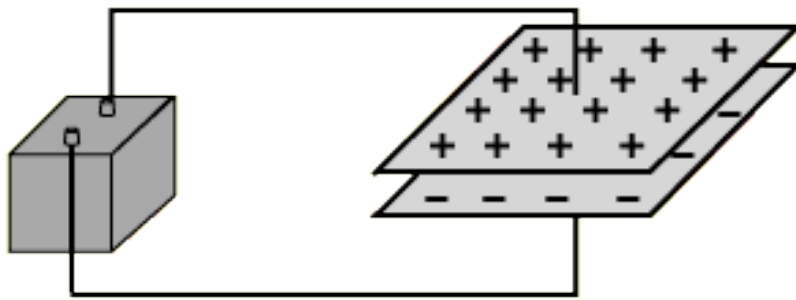
Wire = conductor

Voltage
source



+q capacitor
C
-q

conductor



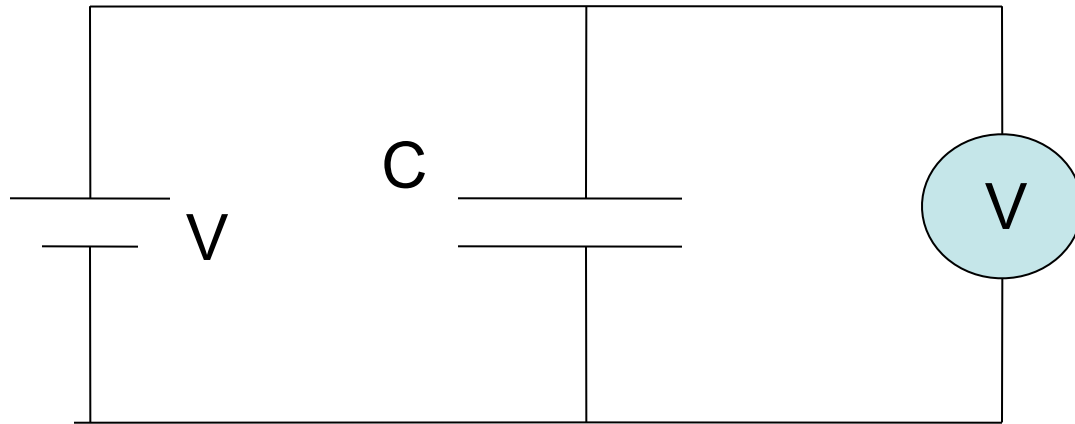
Capacitor

A battery will transport charge from one plate to the other until the voltage produced by the charge buildup is equal to the battery voltage.

$$C = \frac{Q}{V}$$

$$\text{Unit} = \frac{\text{coulomb}}{\text{volt}} = \text{Farad}$$

Measuring voltage



Voltmeter

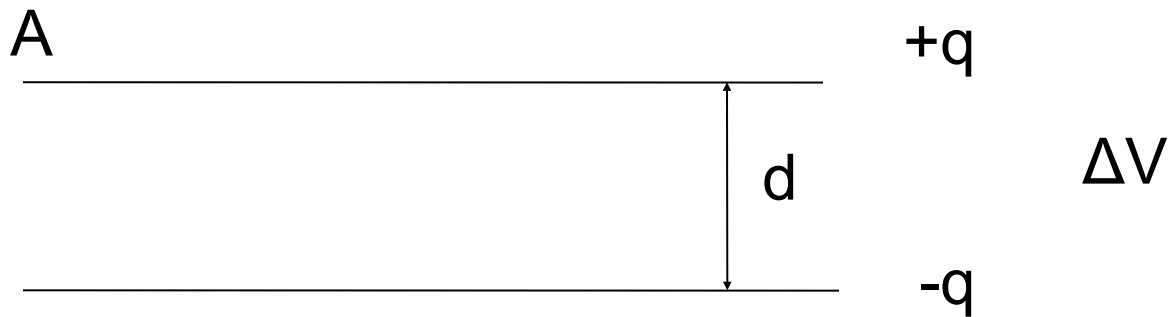
Ideal voltmeter

Draws no charge

Perfect insulator

Parallel Plate Capacitor

Metal plates with area A , separated by a gap, d containing an insulating material. (eg. Air)



Capacitance – describes the ability to store separated charge

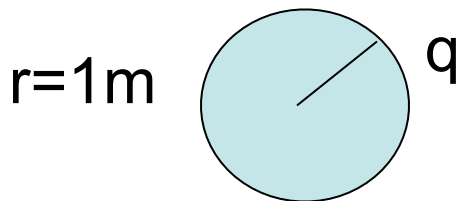
$$C = \frac{q}{\Delta V} \quad \text{Units C/V, farad (F)}$$

A 100 microfarad capacitor is charged to 100 V. How much charge does it store?

$$C = \frac{q}{\Delta V}$$

$$q = C(\Delta V) = 100 \times 10^{-6} (100) = 10^{-2} \text{ C}$$

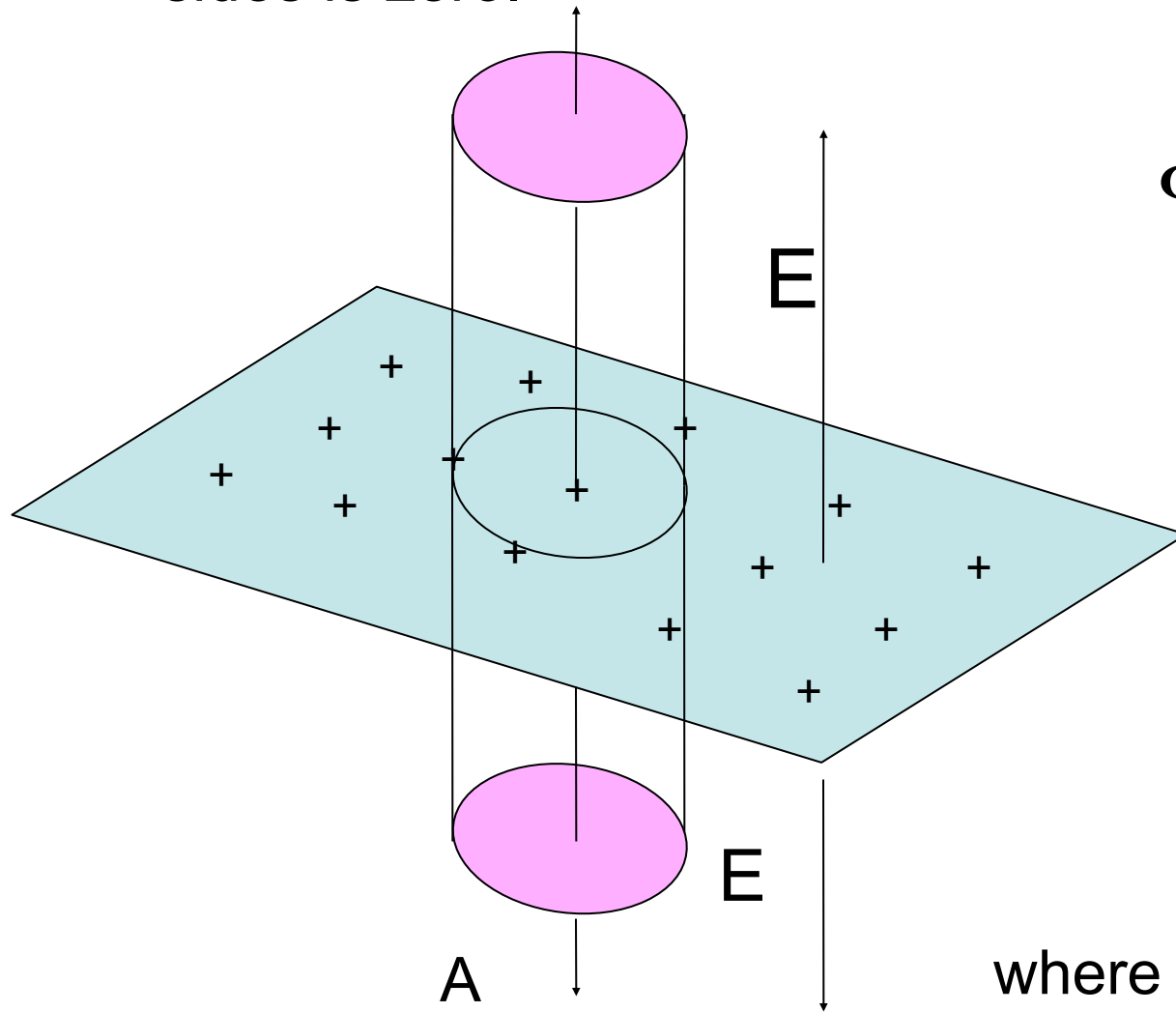
This is a lot of charge. Recall that 10^{-2} C on a sphere of 1m radius generates a potential of



$$V = \frac{k_e q}{r} = 9 \times 10^7 \text{ V}$$

How does the capacitor store this charge without high potentials? How do you get a large capacitance?

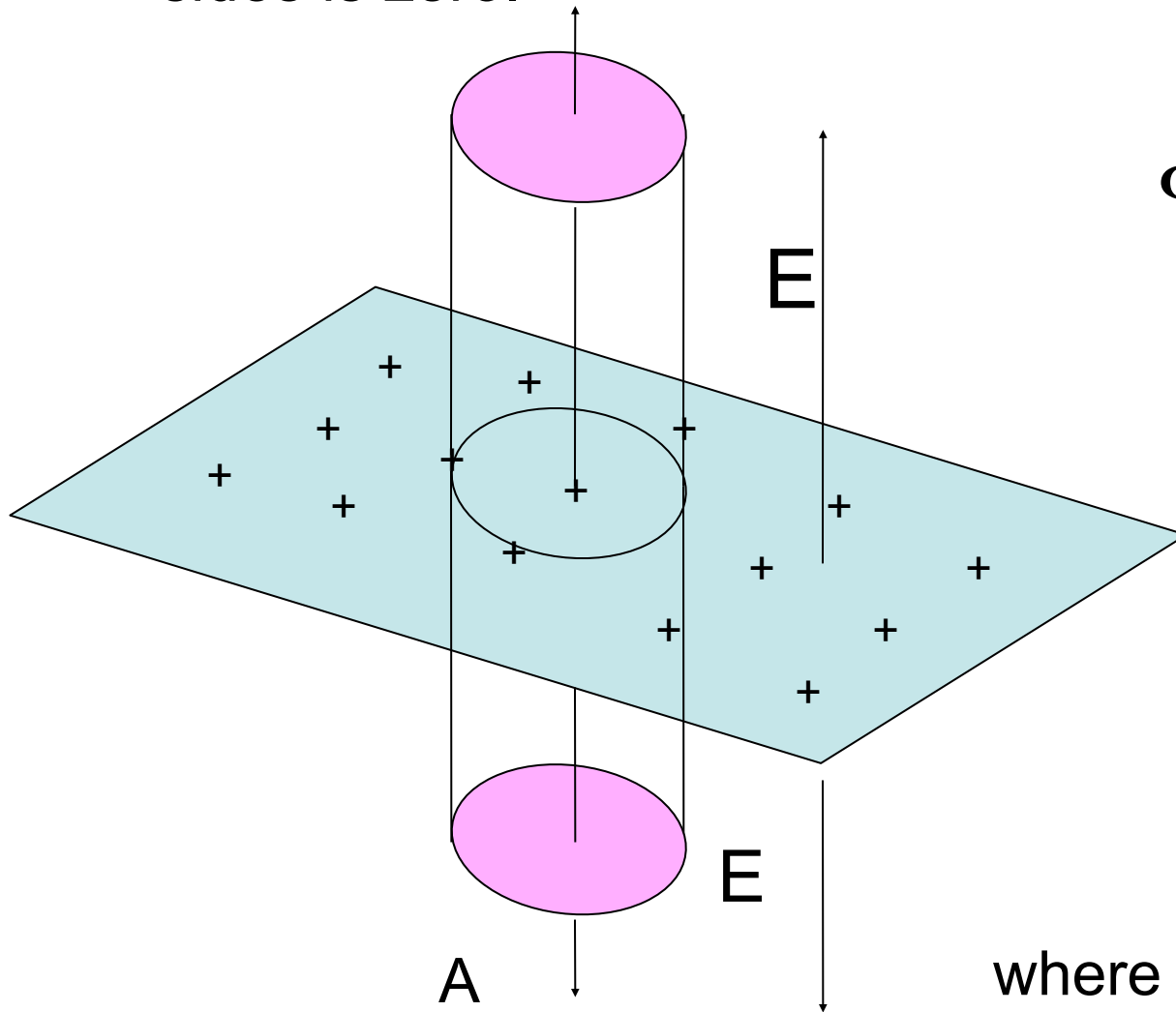
Gaussian surface- a cylinder with sides perpendicular to the plane. E is constant at ends. Flux through sides is zero.



$$\Phi_E = 2AE = \frac{q}{\epsilon_0}$$

where

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$$\Phi_E = 2AE = \frac{q}{\epsilon_0}$$

$$E = \frac{q}{2A\epsilon_0}$$

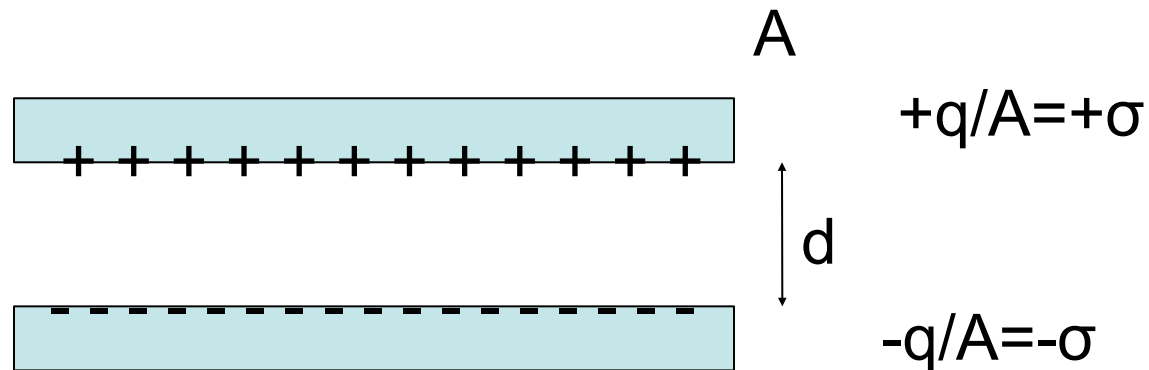
$$E = \frac{\sigma}{2\epsilon_0}$$

where

$$\sigma = \frac{q}{A}$$

Parallel plate capacitor

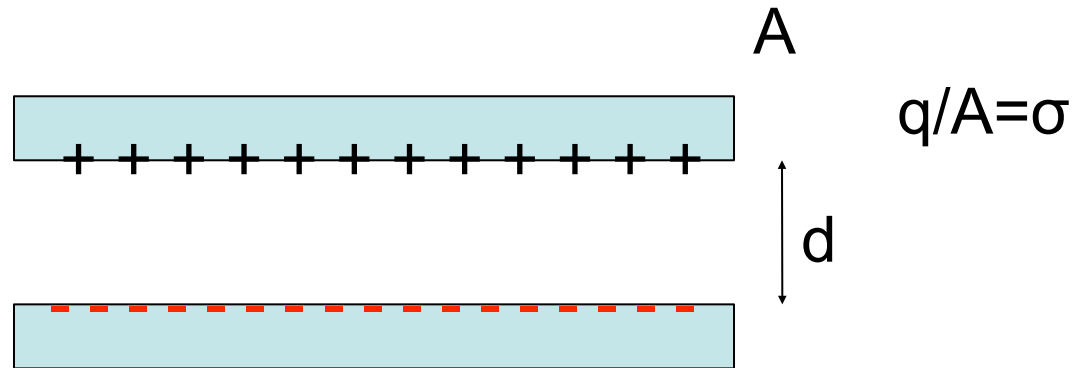
two “infinite” planes of charge area A separated by distance d where $d \ll A$, carry charge $+q$, $-q$



The charges are at the inner surface of the capacitor

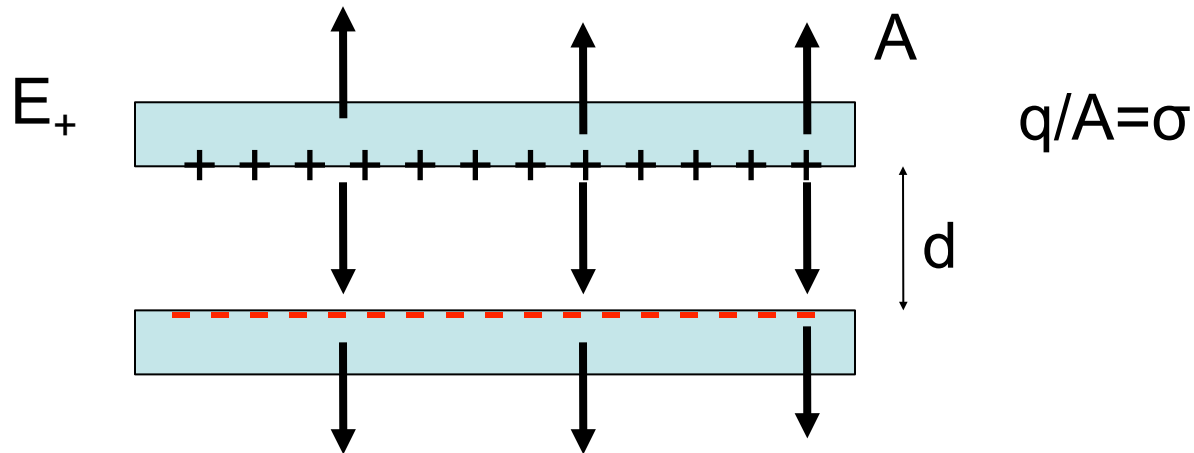
Field inside the capacitor plates

By superposition of charges due to sheet of charge



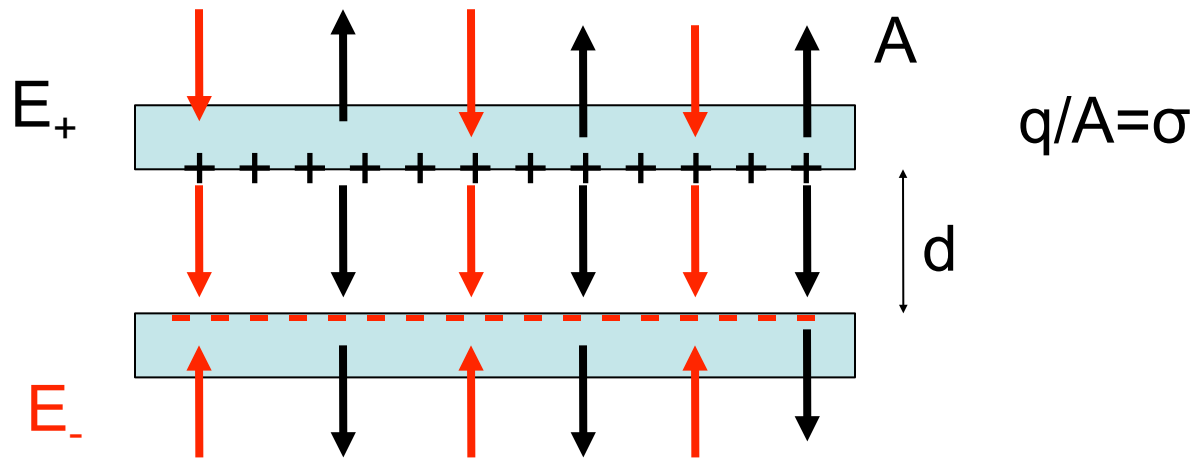
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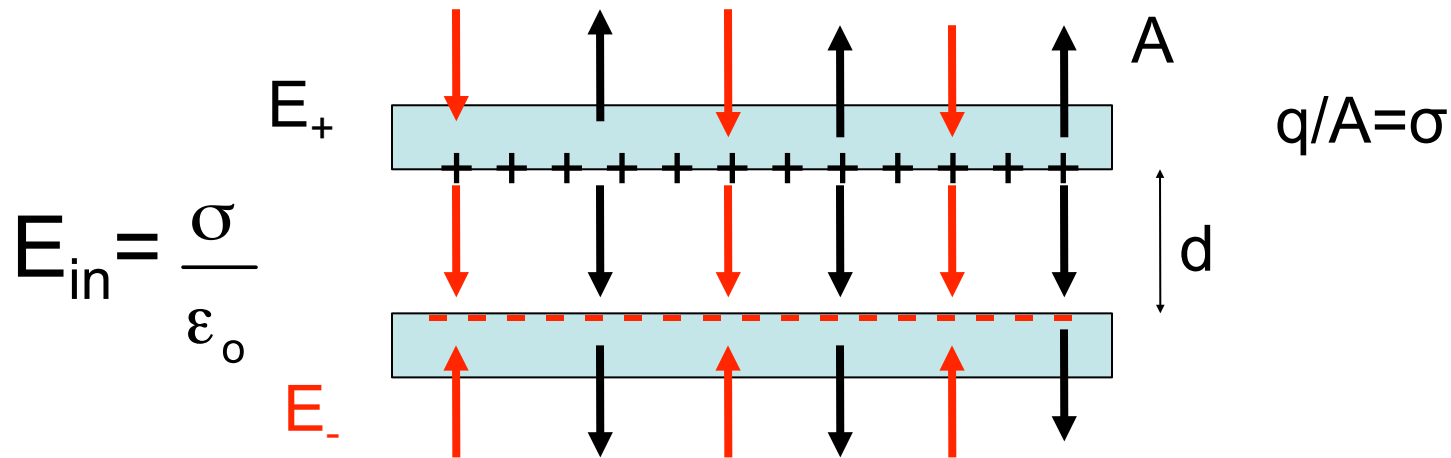
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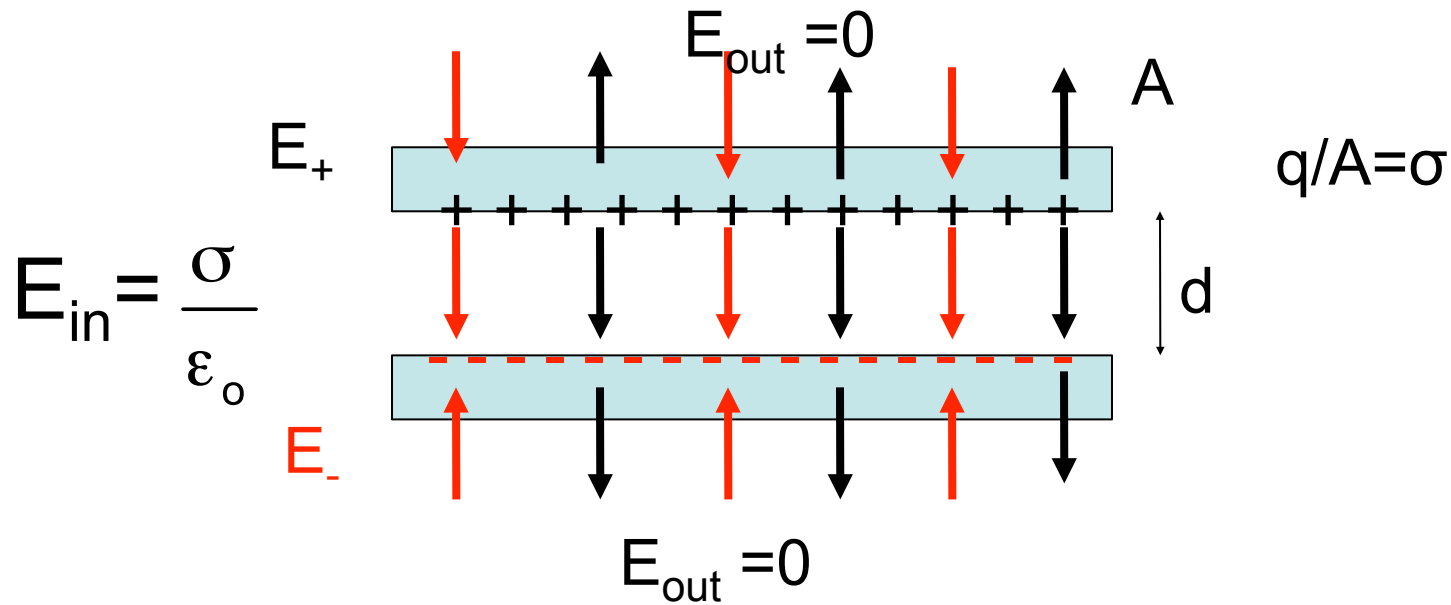


$$E_{in} = \frac{\sigma}{\epsilon_0}$$

$$E_{in} = E_+ + E_- = 2 \frac{\sigma}{2\epsilon_0} = \frac{\sigma}{\epsilon_0}$$

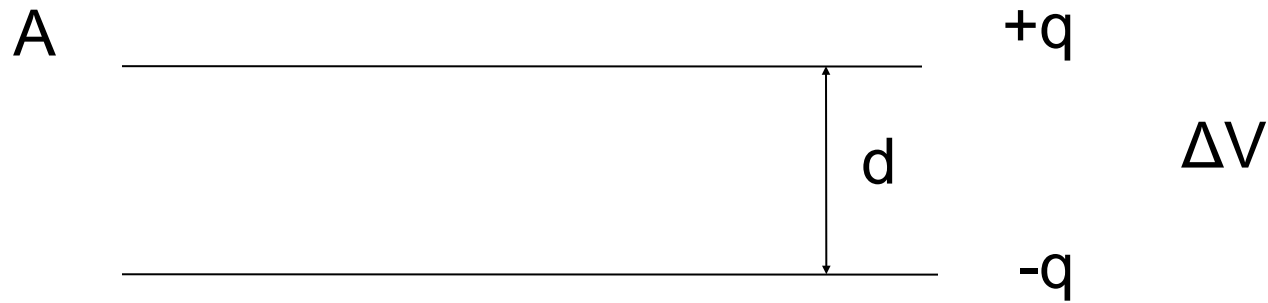
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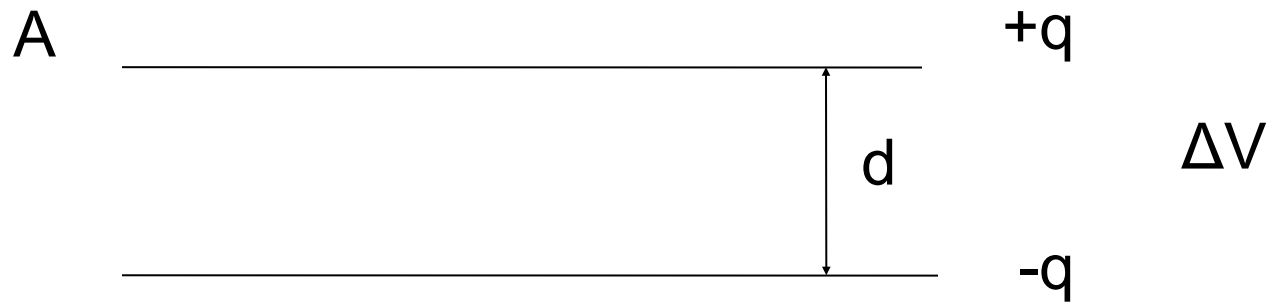


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What is the capacitance of a parallel plate capacitor with plates of area A separated by distance d ? (in air)



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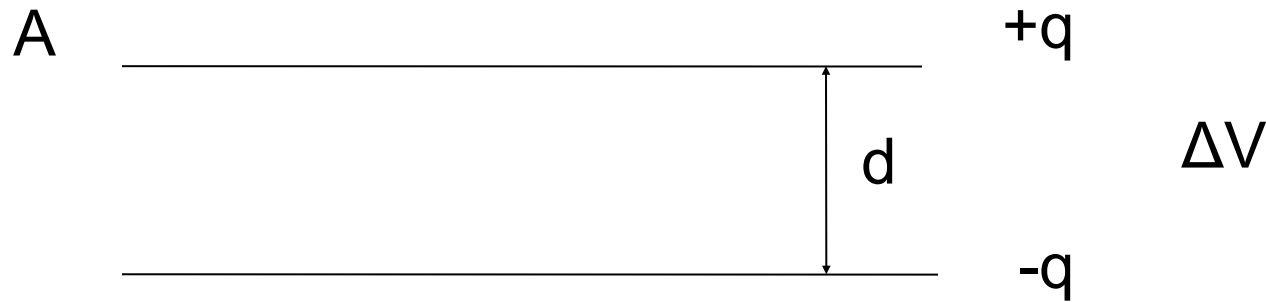


Recall from
Gauss' law

$$E = \frac{\sigma}{\epsilon_0} = \frac{q}{A\epsilon_0} = \frac{\Delta V}{d}$$

E field
increases with
charge density

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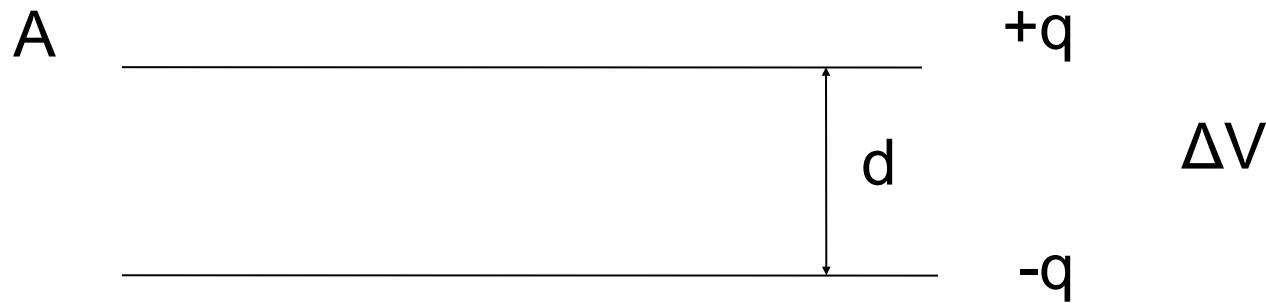
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rearrange

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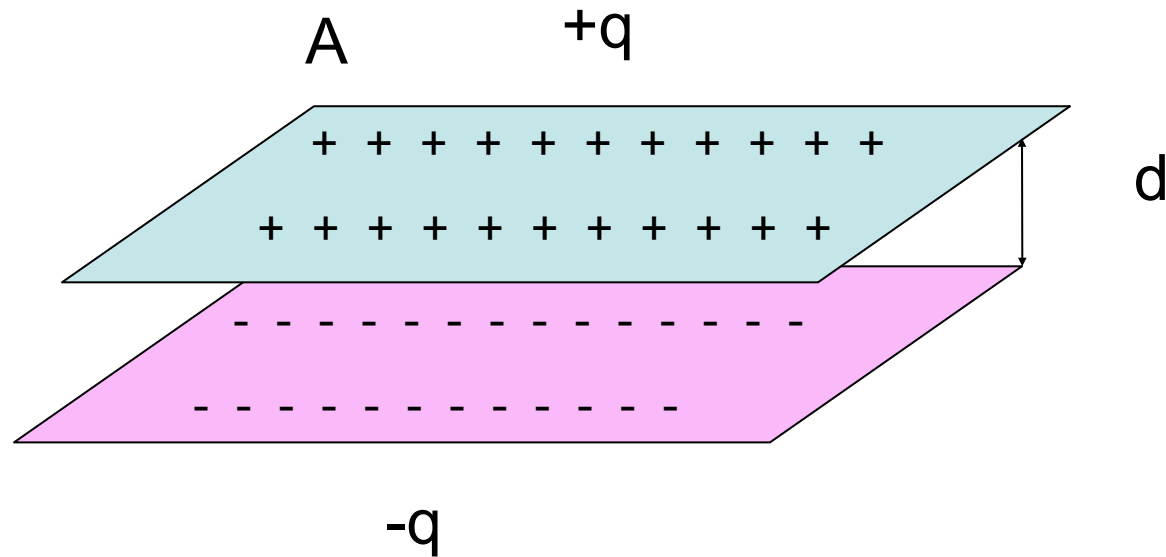
$$\frac{q}{\Delta V} = \frac{A\epsilon_0}{d}$$

thus

$$C = \frac{A\epsilon_0}{d}$$

to increase C
Increase A
Decrease d

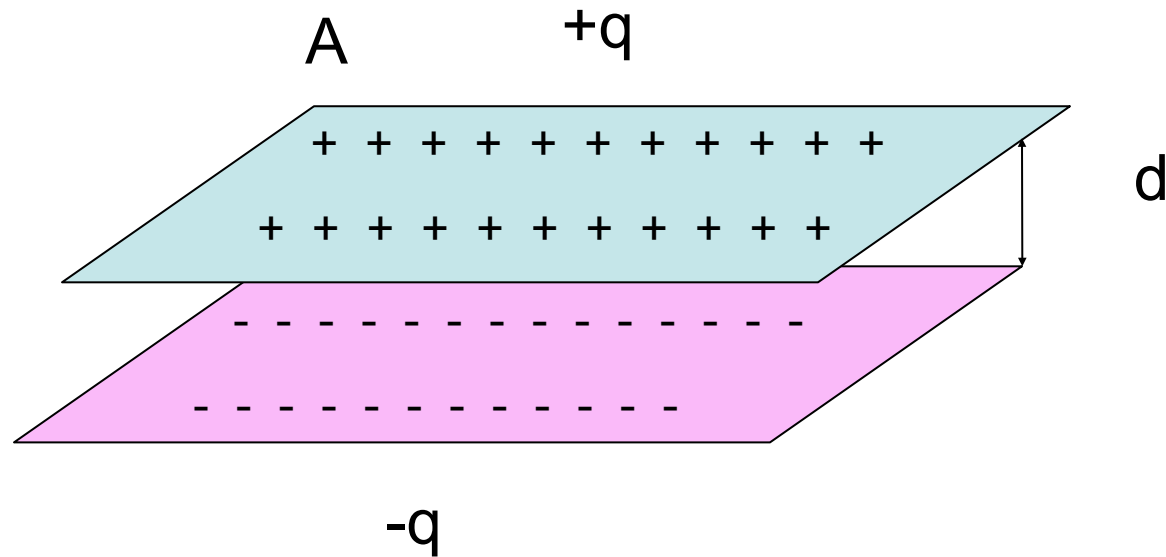
How do you stabilize the separated charge
i.e. make ΔV as small as possible for a given q
(high capacitance)



area A

distance d

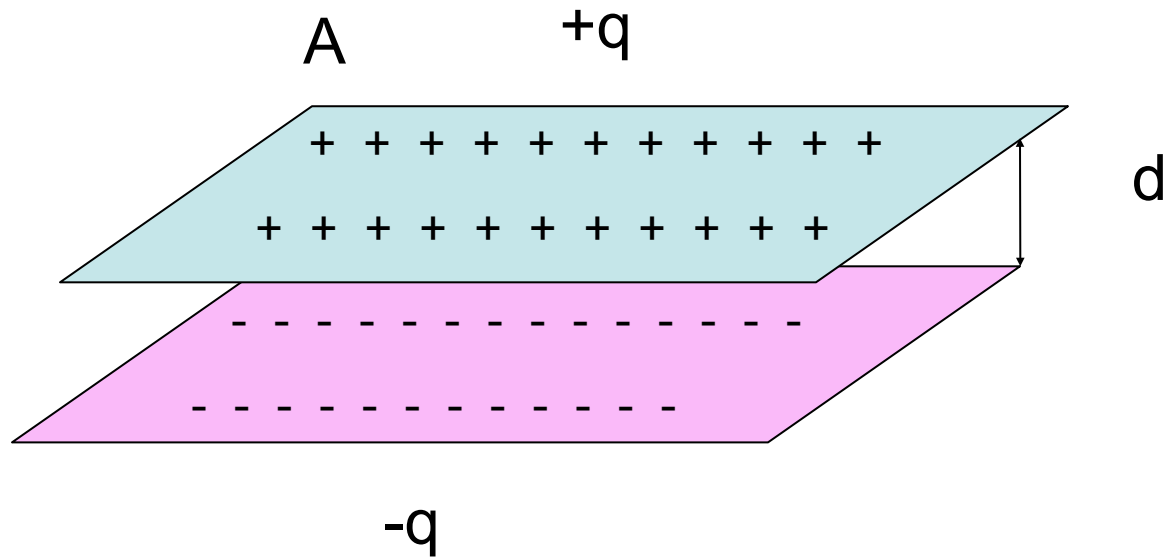
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area A as Large as possible

distance d

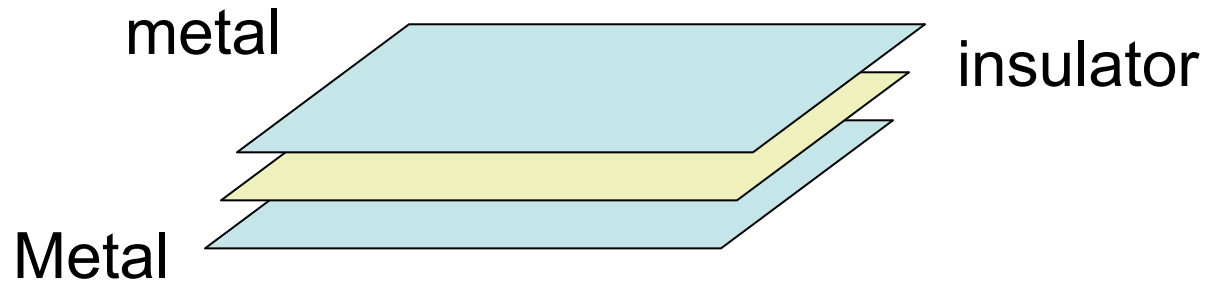
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area A as Large as possible
distance d as SMALL as possible

Thin film capacitors

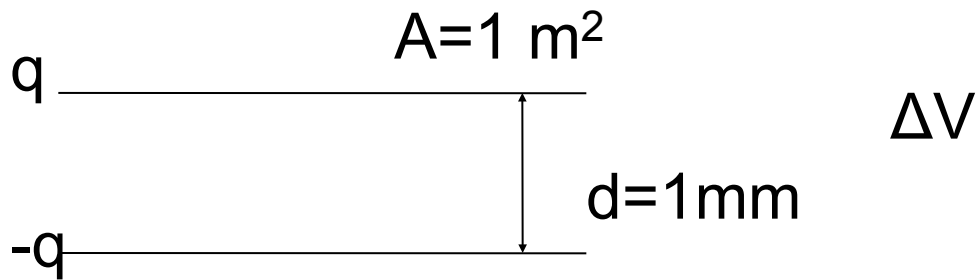
Metal film separated by thin insulators



Making the area large and the insulating gap small increases C

A parallel plate capacitor with 2 plates each with area 1.0 m^2 separated by a distance of 1.0 mm holds $+q, -q$, $q=10^{-6}\text{C}$

- (a) Find the capacitance. (b) Find the E field in the capacitor
(c) Find ΔV across the plates



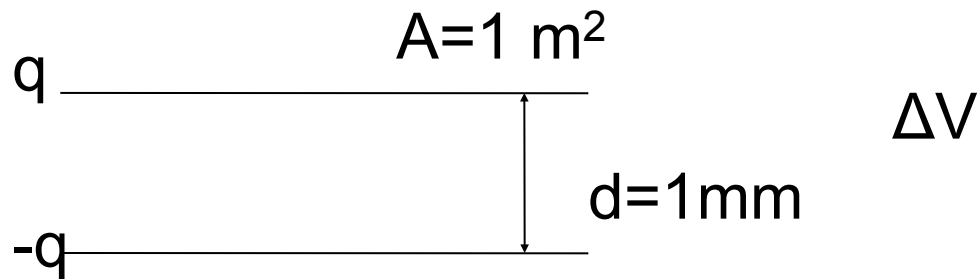
$C =$

$E =$

$\Delta V =$

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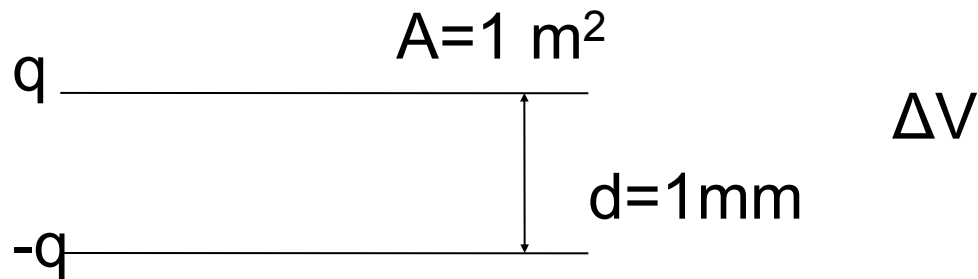
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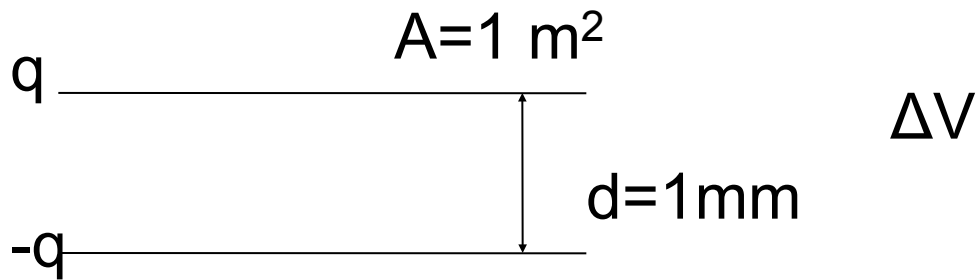
$$C = \frac{A\epsilon_0}{d} = \frac{1(8.9 \times 10^{-12})}{0.001} = 8.9 \times 10^{-9} \text{ F} = 8.9 \text{ nF}$$

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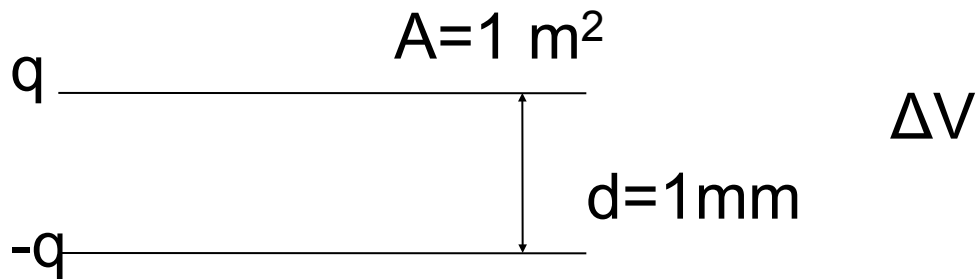
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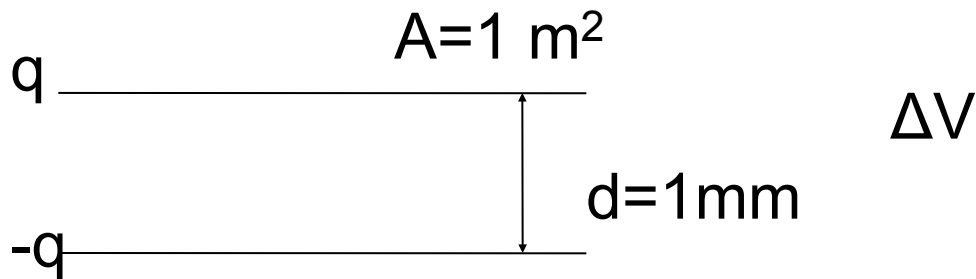
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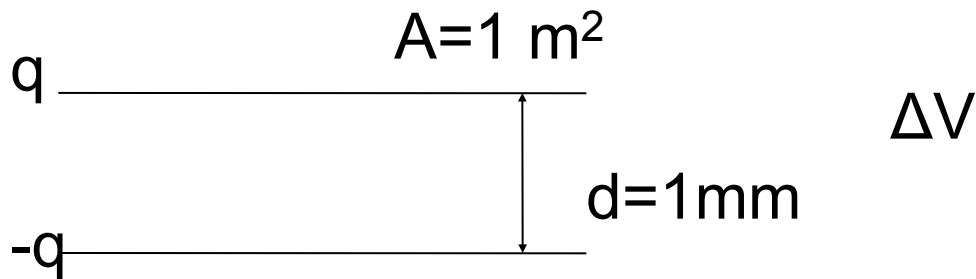
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$$\Delta V = Ed$$

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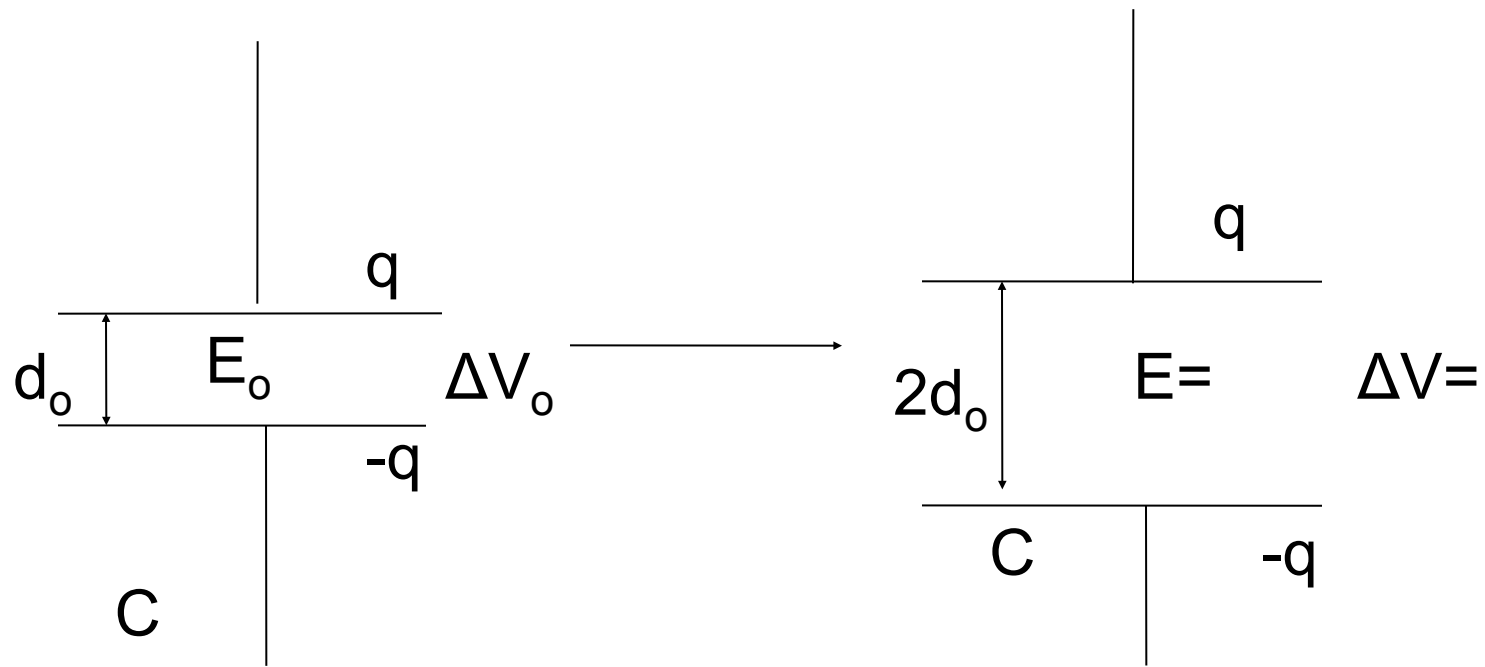


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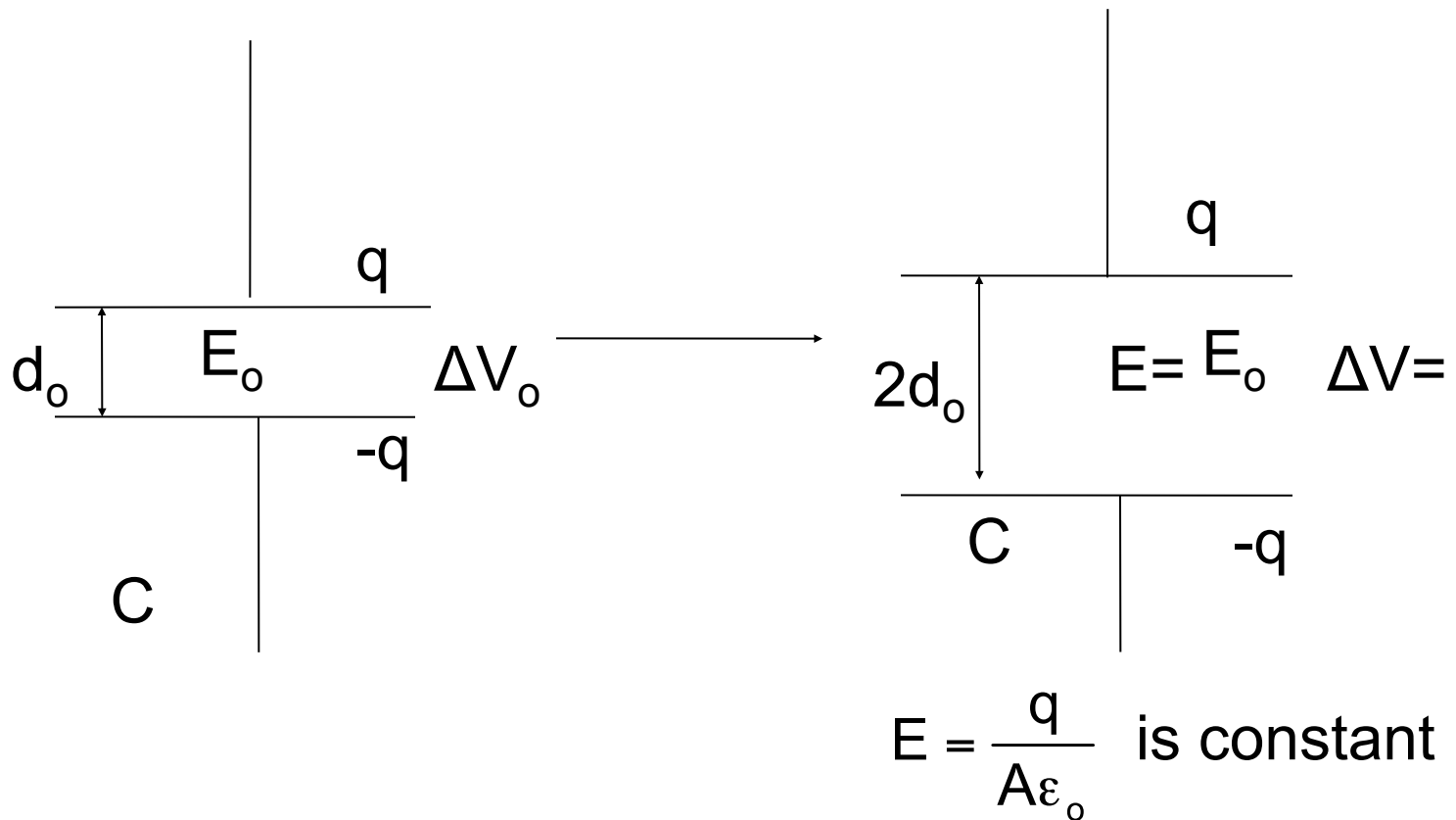
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$$\Delta V = Ed = 1.1 \times 10^5 (1 \times 10^{-3}) = 1.1 \times 10^2 \text{ V}$$

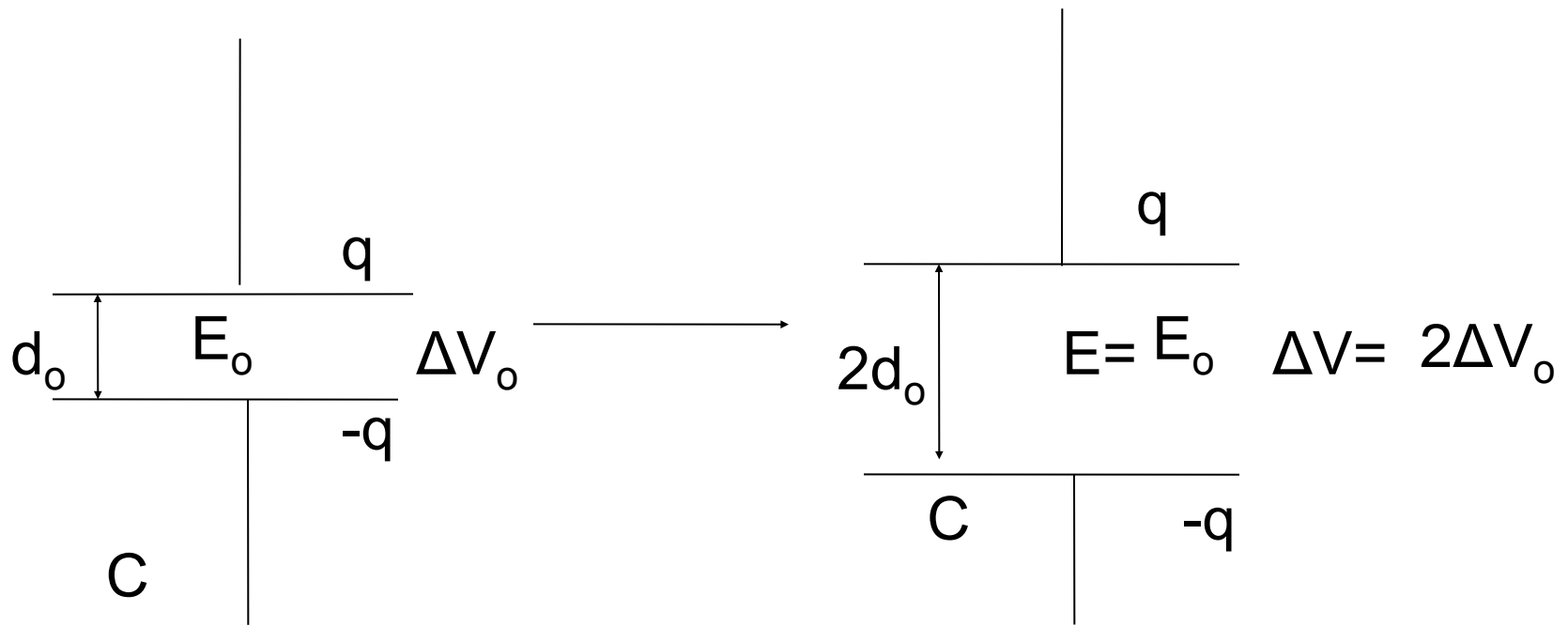
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 How does this change E and ΔV ?



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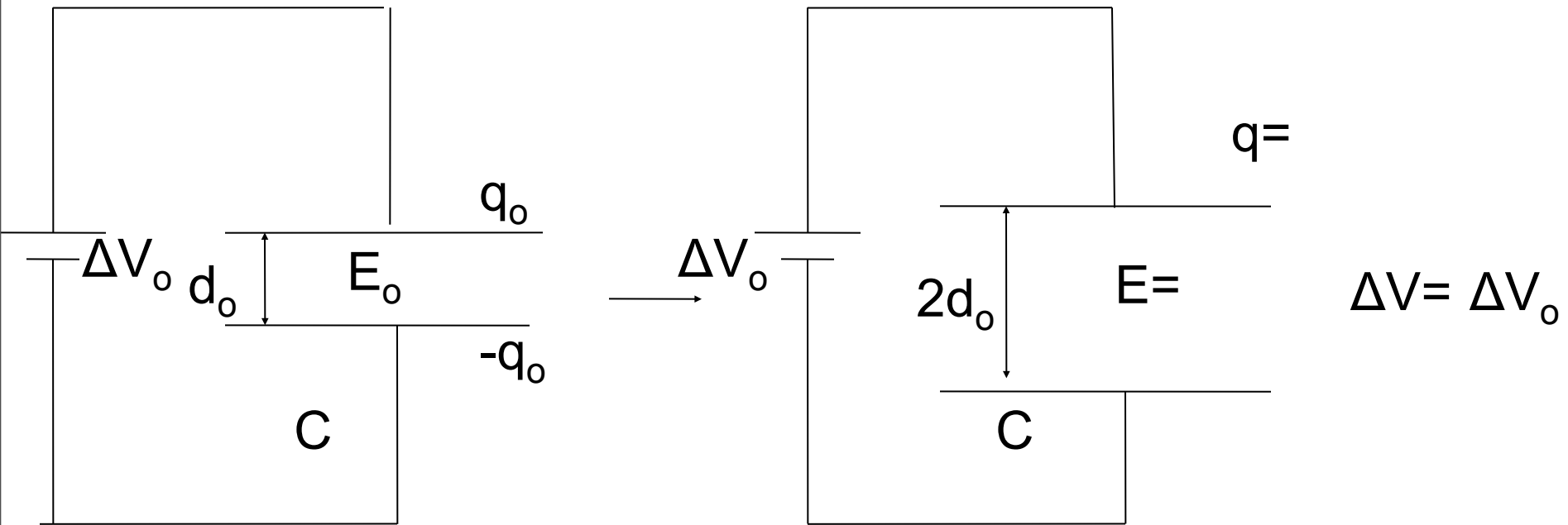
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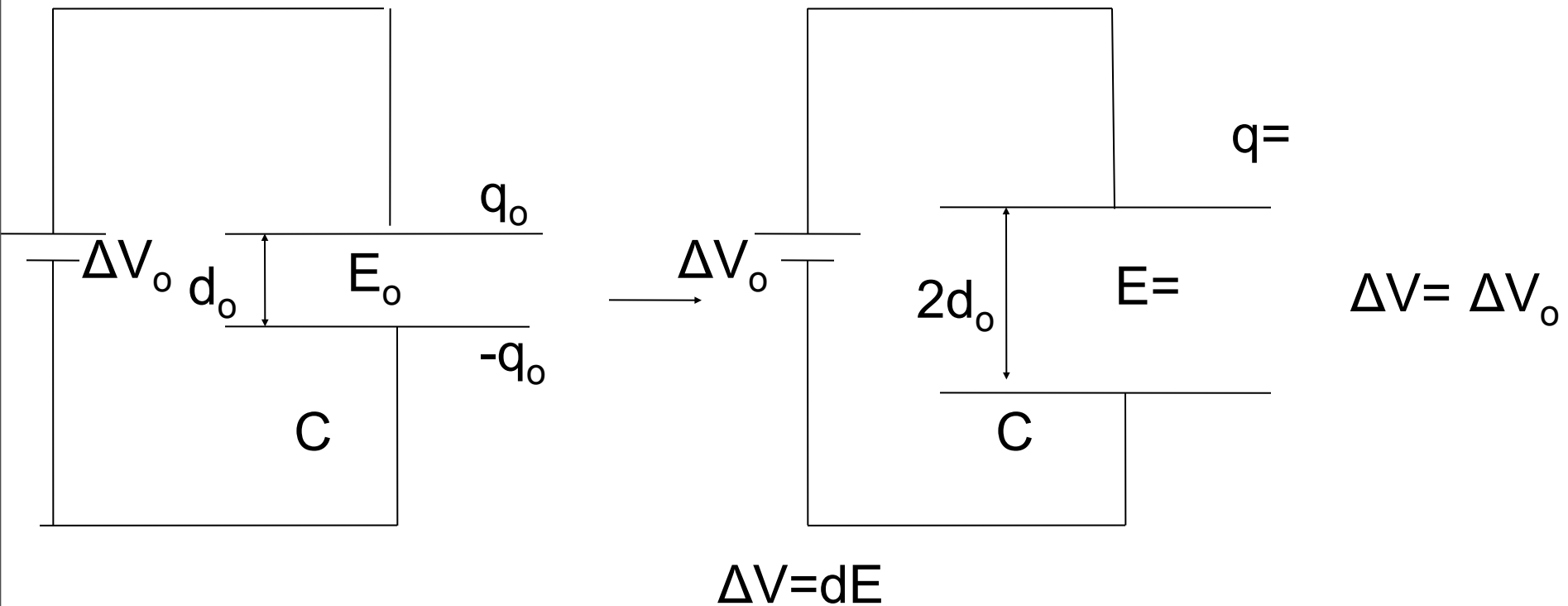
$$E = \frac{q}{A\epsilon_0} \text{ is constant}$$

$$\Delta V = dE = 2\Delta V_0$$

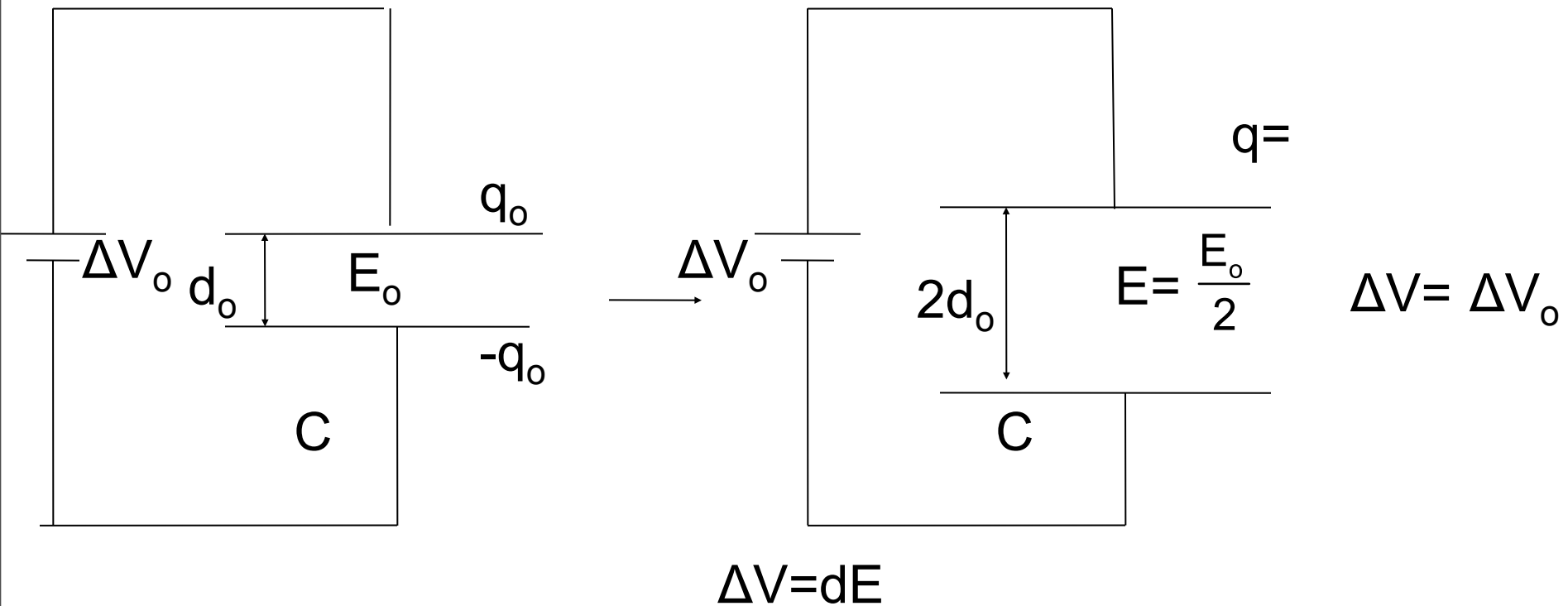
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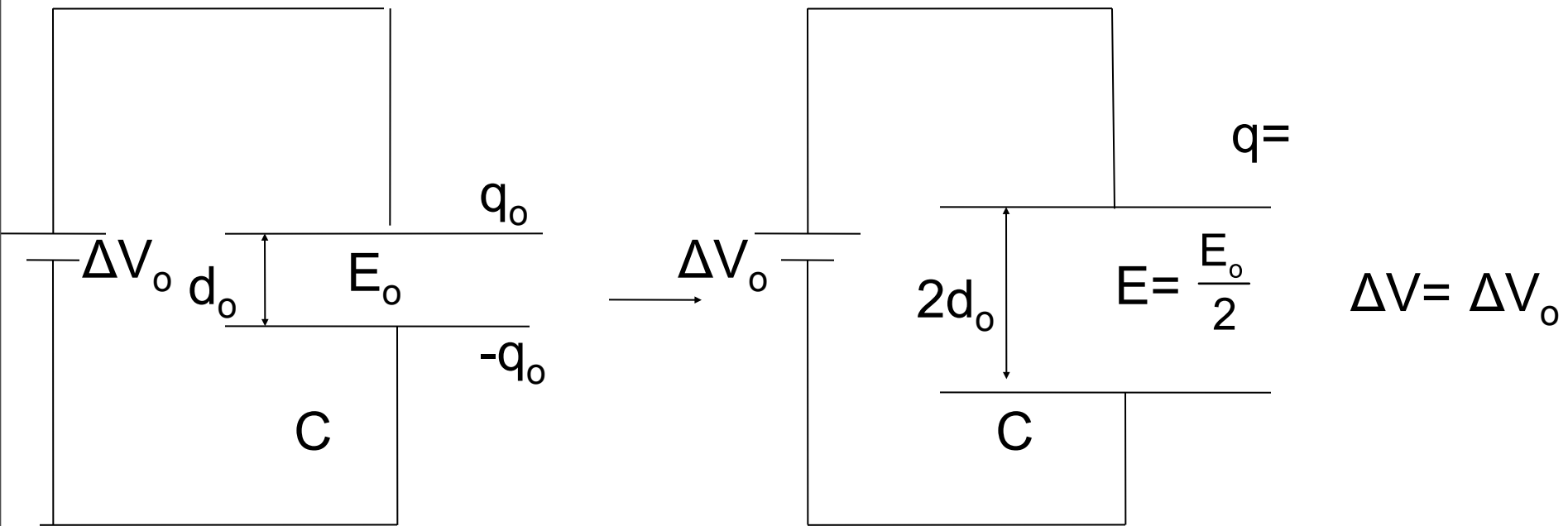
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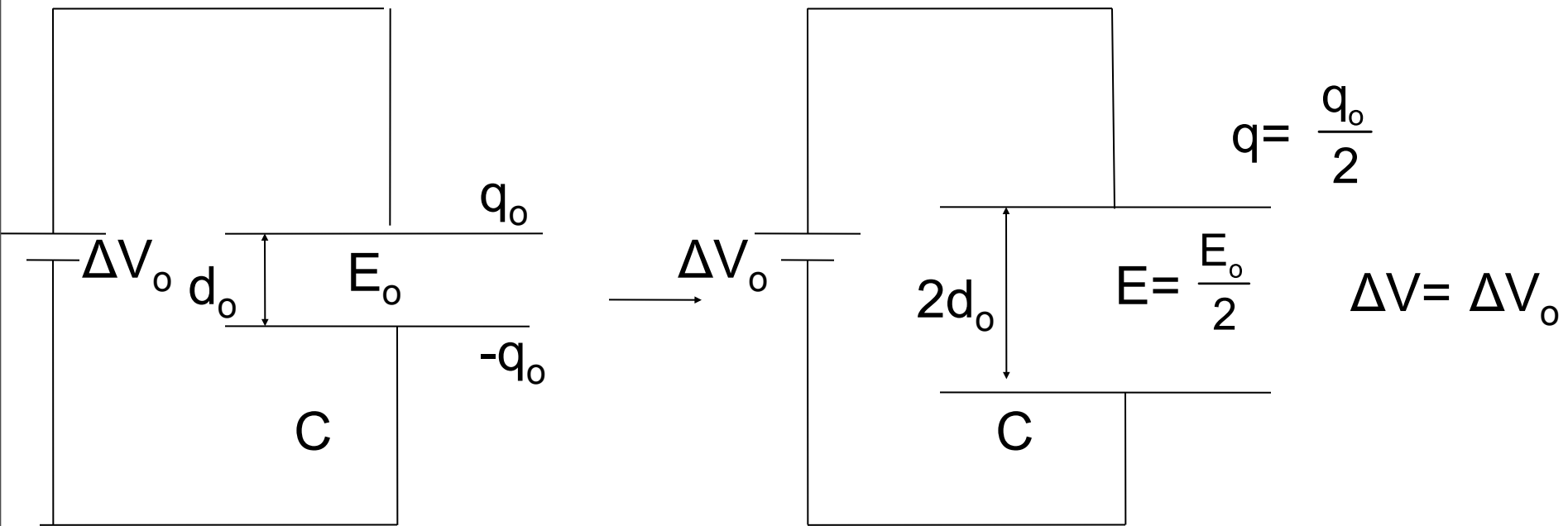
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$$\Delta V = dE$$

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Capacitor combinations

Capacitors connected in series
and parallel